FEDFA: FEDERATED FEATURE AUGMENTATION

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ABSTRACT

Federated learning is a distributed paradigm that allows multiple parties to collaboratively train deep models without exchanging the raw data. However, the data distribution among clients is naturally non-i.i.d., which leads to severe degradation of the learnt model. The primary goal of this paper is to develop a robust federated learning algorithm to address *feature shift* in clients' samples, which can be caused by various factors, *e.g.*, acquisition differences in medical imaging. To reach this goal, we propose FEDFA to tackle federated learning from a distinct perspective of federated feature augmentation. FEDFA is based on a major insight that instance-level feature statistics (*i.e.*, mean and standard deviation) represent a special type of "features" that encodes domain-specific characteristics; hence, proper manipulations of the local feature statistics in the federation may beget novel domains, which can potentially alleviate local feature shift and benefit collaborative learning. Based on this insight, we model each feature statistic probabilistically via a Gaussian distribution, with the mean corresponding to the original statistic and the variance quantifying the augmentation scope, from which novel feature statistics can be drawn to fulfill augmentation. Key to our approach is the determination of a meaningful Gaussian variance, which is accomplished by taking into account not only biased data of each individual client, but also underlying feature statistics characterized by all participating clients. We demonstrate through extensive experiments that FEDFA can *significantly* advance federated learning in diverse scenarios. The code will be released.

1 INTRODUCTION

Federated learning (FL) (Konečný et al., 2016) is an emerging collaborative training framework that enables training on decentralized data residing devices like mobile phones. It comes with the promise of training centralized models using local data points such that the privacy of participating devices is preserved, and has attracted significant attention in critical fields like healthcare or finance. Since data coming different users, it is inevitable that the data of each user have a different underlying distribution, incurring large heterogeneity (non-iid-ness) among users' data. In this work, we focus on *feature shift* (Li et al., 2020b), which is common in many real-world cases, like medical data acquired from different devices or natural image collected in diverse environments.

While the problem of feature shift has been studied in classical centralized learning tasks like domain generalization, little is understood how to tackle it in federated learning. (Li et al., 2020b; Reisizadeh et al., 2020; Jiang et al., 2022; Liu et al., 2020a) are rare exceptions. FEDROBUST (Reisizadeh et al., 2020) and FEDBN (Li et al., 2020b) solve the problem through *client-dependent* learning by either fitting the shift with a client-specific affine distribution or learning unique BN parameters for each client. However, these algorithms may still suffer significant local dataset bias. Other works (Liu et al., 2020a; Jiang et al., 2022) learn robust models by adopting Sharpness Aware Minimization (SAM) (Foret et al., 2021) as the local optimizer, which, however, doubles the computational cost compared to SGD or Adam. In addition to model optimization, FEDHARMO (Jiang et al., 2022) has investigated image normalization techniques to mitigate feature shift in medical domains. Despite the progress, there leaves an alternative space – *data augmentation* – largely unexplored in federated learning scenarios, even that it has been extensively investigated in centralized setting to impose regularization and improve generalizibility (Wang et al., 2019; Zhou et al., 2021; Zhang et al., 2018).

While seemingly straightforward, it is non-trivial to perform effective data augmentation in federated learning because users have no direct access to external data of other users. Simply applying

conventional augmentation techniques to each client is sub-optimal since without injecting global information, augmented samples will most likely still suffer local dataset bias. To address this, FEDMIX (Yoon et al., 2021) generalizes Mixup (Zhang et al., 2018) into federated learning. It follows the basic idea of vanilla Mixup, and performs cross-client sample mixup by exchanging averaged data across clients. The method performs augmentation in the input level, which is naturally weak to create meaningful semantic transformations, *e.g.*, *make-bespectacled*. Moreover, allowing exchange of averaged data will suffer certain levels of privacy issues.

In this paper, we introduce a novel feature augmentation technique FEDFA for federated learning, based on a probabilistic modeling of *feature statistics* (*i.e.*, mean and standard deviation) over all participating clients. FEDFA is based on the insight that feature statistics can convey essential domain-aware characteristics (Huang & Belongie, 2017; Zhou et al., 2021; Li et al., 2021; 2022), and can be treated as "features of domain". Accordingly, we argue that no matter the shift of each local data distribution from the true distribution, or local distribution differences among clients, even test-time distribution shift, can be interpreted as the shift of feature statistics. This motivates us to turn the problem of *tackling feature shift* into *tackling feature statistic shift*, for which we propose FEDFA to perform feature statistic augmentation within each local client by incorporating more universal feature statistic information characterized by all clients in the federation.

In particular, we model each feature statistic in a probabilistic manner via a multi-variate Gaussian distribution. The Gaussian *mean* corresponds to the original statistic, and *variance* reflects the potential local distribution shift. In this manner, we can sample novel statistics effortlessly from the Gaussian distribution as augmented "features of domain". For effective augmentation, we determine a proper *variance* based on variances of feature statistics within each client, which are regulated by universal variances of feature statistics characterized by all participating clients. The augmentation in FEDFA allows the local model to be trained over samples drawn from more diverse feature distributions, facilitating local distribution shift alleviation and client-invariant representation learning, eventually contributing to a better global model.

FEDFA is a conceptually simple but surprisingly effective method. It is non-parametric, requires negligible additional computational resources, and can be seamlessly incorporated into arbitrary CNN architectures. We provide extensive empirical evaluations on competitive image classification and medical image segmentation benchmarks, and the results demonstrate that: i) FEDFA works favorably with extremely small local datasets; ii) it shows remarkable generalization performance to *unseen* test clients outside of the federation; iii) it outperforms traditional data augmentation techniques by solid margins, and can complement them quite well in the federated learning setup.

2 RELATED WORK

Federated Learning. Recent years have witnessed tremendous progress in federated learning (Konečnỳ et al., 2016), which opens the door for privacy-preserving deep learning (Shokri & Shmatikov, 2015), *i.e.*, train a global model on distributed datasets without disclosing private data information. FEDAVG (McMahan et al., 2017) is a milestone; it trains local models independently in multiple clients and then averages the resulting model updates via a central server once in a while. However, FEDAVG is designed for i.i.d. data and suffers in statistical accuracy or even diverge if deployed over non-i.i.d. client samples. To address this issue, numerous efforts have been devoted to handling heterogeneous federated environments, by, for example, adding a dynamic regularizer to local objectives in FEDPROX (Li et al., 2020a) and FEDDYN (Acar et al., 2021), correcting client drift through variance reduction in SCAFFOLD (Karimireddy et al., 2020), adaptive server optimization in FEDOPT (Reddi et al., 2021), local batch normalization in FEDBN (Li et al., 2020b), or training a perturbed loss in FEDSAM (Qu et al., 2022) and FEDROBUST (Reisizadeh et al., 2020).

FEDMIX (Yoon et al., 2021), as far as we know, is the only existing method that solves federated learning based on data augmentation. It adapts the well-known Mixup algorithm (Zhang et al., 2018) from centralized learning into the federated learning scenario. Nevertheless, FEDMIX requires exchanging local data (or averaged version) across clients for data interpolation, thereby suffering privacy issues. In addition, FEDMIX operates on the input level, while our approach focuses on latent feature statistic augmentation. Since deeper representations tend to disentangle the underlying factors of variation better (Bengio et al., 2013), traversing along latent space will potentially make

our method encounter more realistic samples. This is supported by the fact that FEDFA achieves consistent performance improvements over FEDMIX in diverse scenarios (see §4).

Data Augmentation. Data augmentation has a long and rich history in machine learning. Early studies (Schölkopf et al., 1996; Kukačka et al., 2017) focus on *label-preserving* transformations to employ regularization via data, alleviating overfitting and improving generalization. For image data, some techniques, like random horizontal flipping and cropping are commonly used for training of advanced neural networks (He et al., 2016). In addition, there is a recent trend for *label-perturbing* augmentation, *e.g.*, Mixup (Zhang et al., 2018) or Cutmix (Yun et al., 2019). Separate from these input-level augmentation techniques are feature augmentation methods (Verma et al., 2019; Li et al., 2021; Zhou et al., 2021) that make augmentation in latent feature space. These various data augmentation techniques have shown great successes to learn domain-invariant models in the centralized setup. Our method is an instance of label-preserving feature augmentation, designed for federated learning. It is inspired by recent efforts on implicit feature augmentation (Li et al., 2021; Zhou et al., 2021) that synthesize samples of novel domains by swapping or mixing instance-level *feature statistics*. In these works, feature statistics are treated as 'features', which capture essential domain-specific characteristics. In FEDFA, instead of linearly combining feature statistics, we estimate appropriate variances of feature statistics from a federated perspective, and draw novel statistics probablistically from a distribution spanning with the variances. FEDFA avoids statistics mixing of instances from different clients, as done in (Li et al., 2021; Zhou et al., 2021) and recent federated method FEDMIX, thus can better preserve data privacy.

3 OUR APPROACH

3.1 PRELIMINARY: FEDERATED LEARNING

We assume a standard federated learning setup with a server that can transmit and receive messages from M client devices. Each client $m \in [M]$ has access to N_m training instances $\{(x_i, y_i)\}_{i=1}^{N_m}$ in the form of image $x_i \in \mathcal{X}$ and corresponding labels $y_i \in \mathcal{Y}$ that are drawn i.i.d. from a device-indexed joint distribution, *i.e.*, $(x_i, y_i) \sim \mathbb{P}_m(x, y)$. The goal of standard federated learning is to learn a deep neural network: $f(\boldsymbol{w}_g, \boldsymbol{w}_h) \triangleq g(\boldsymbol{w}_g) \circ h(\boldsymbol{w}_h)$, where $h : \mathcal{X} \to \mathcal{Z}$ is a feature extractor with K convolutional stages: $h = h^K \circ h^{K-1} \circ \cdots \circ h^1$, and $g : \mathcal{Z} \to \mathcal{Y}$ is a classifier. To learn network parameters $\boldsymbol{w} = \{\boldsymbol{w}_g, \boldsymbol{w}_h\}$, the empirical risk minimization (ERM) is widely used:

$$\mathcal{L}^{\text{ERM}}(\boldsymbol{w}) \triangleq \frac{1}{M} \sum_{m \in [M]} \mathcal{L}_m(\boldsymbol{w}), \quad \text{where } \mathcal{L}_m(\boldsymbol{w}) = \mathbb{E}_{(x_i, y_i) \sim \mathbb{P}_m}[\ell_i(g \circ h(x_i), y_i; \boldsymbol{w})]. \tag{1}$$

Here the global objective $\mathcal{L}^{\text{ERM}}$ is decomposable as a sum of device-level empirical loss objectives (*i.e.*, $\{\mathcal{L}_m\}_m$). Each $\mathcal{L}_m$ is computed based on a per-data loss function ℓ_i. Due to the separation of clients' data, $\mathcal{L}^{\text{ERM}}(\boldsymbol{w})$ cannot be solved directly. FEDAVG (McMahan et al., 2017) is a leading algorithm to address this. It starts with *client training* of all the clients in parallel, with each client optimizing $\mathcal{L}_m$ independently. After local client training, FEDAVG performs *model aggregation* to average all client models into a updated global model, which will be distributed back to the clients for the next round of client training. Here the *client training* objective in FEDAVG is equivalent to empirically approximating the local distribution $\mathbb{P}_m$ by a finite N_m number of examples, *i.e.*, $\mathbb{P}_m^e(x, y) = {}^1/_{N_m} \sum_{i=1}^{N_m} \delta(x = x_i, y = y_i)$, where $\delta(x = x_i, y = y_i)$ is a Dirac mass centered at (x_i, y_i).

3.2 MOTIVATION

While the ERM-based formulation has achieved great success, it is straightforward to see that the solution would strongly depend on how each approximated local distribution $\mathbb{P}_m^e$ mimics the underlying universal distribution $\mathbb{P}$. In real-world federated learning setup however, in all but trivial cases each $\mathbb{P}_m^e$ exhibits a unique distribution shift from $\mathbb{P}$, which causes not only inconsistency between local and global empirical losses (Acar et al., 2021; Wang et al., 2020), but also generalization issues (Yuan et al., 2022). In this work, we circumvent this issue by fitting each local dataset a *richer* distribution (instead of the delta distribution) in the *vicinal region* of each sample (x_i, y_i) so as to estimate a more informed risk. This is precisely the principle behind vicinal risk minimization (VRM) (Chapelle et al., 2000). Particularly, for data point (x_i, y_i), a vicinity distribution $\mathbb{V}_m(\hat{x}_i, \hat{y}_i | x_i, y_i)$ is defined, from which novel virtual samples can be generated to enlarge the

support of the local data distribution. In this way, we obtain an improved approximation of $\mathbb{P}_m$ as $\mathbb{P}_m^v = {}^1/_{N_m} \sum_{i=1}^{N_m} \mathbb{V}_m(\hat{x}_i, \hat{y}_i | x_i, y_i)$. In centralized learning scenarios, various successful instances of $\mathbb{V}_m$, *e.g.*, Mixup (Zhang et al., 2018), Cutmix (Yun et al., 2019), have been developed. Simply applying them to local clients, though allowing for performance improvements (see Table 5), is sub-optimal since, without injecting any global information, $\mathbb{P}_m^v$ only provides a better approximation to the local distribution $\mathbb{P}_m$, rather than the true distribution $\mathbb{P}$. We solve this by introducing a dedicated method FEDFA to estimate more reasonable $\mathbb{V}_m$ in federated learning.

3.3 FEDFA: FEDERATED FEATURE AUGMENTATION

FEDFA belongs to the family of label-preserving feature augmentation (Xie et al., 2020). During training, it estimates a vicinity distribution $\mathbb{V}_m^k$ at each layer h^k to augment hidden features in client m. Considering $\boldsymbol{X}_m^k \in \mathbb{R}^{B \times C \times H \times W}$ as the intermediate feature representation of B mini-batch images, with spatial size $(H \times W)$ and channel number (C), and Y_m^k as corresponding label. $\mathbb{V}_m^k$ is label-preserving in the sense that $\mathbb{V}_m^k(\hat{\boldsymbol{X}}_m^k, \hat{Y}_m | \boldsymbol{X}_m^k, Y_m) \triangleq \mathbb{V}_m^k(\hat{\boldsymbol{X}}_m^k | \boldsymbol{X}_m^k)\delta(\hat{Y}_m = Y_m)$, *i.e.*, it only transforms the latent feature $\boldsymbol{X}_m^k$ to $\hat{\boldsymbol{X}}_m^k$, but preserves the original label Y_m^k.

Probabilistic Feature Statistic Modeling. Instead of pursuing an explicit modeling of $\mathbb{V}_m^k(\hat{\boldsymbol{X}}_m^k | \boldsymbol{X}_m^k)$, our method performs feature augmentation in an implicit manner by augmenting channel-wise feature *statistics*. Specifically, for $\boldsymbol{X}_m^k$, its channel-wise statistics, *i.e.*, mean μ_m^k and standard deviation σ_m^k are given as follows:

$$\mu_m^k = \frac{1}{HW} \sum_{h=1}^{H} \sum_{w=1}^{W} \boldsymbol{X}_m^k \quad \in \mathbb{R}^{B \times C}, \qquad \sigma_m^k = \sqrt{\frac{1}{HW} \sum_{h=1}^{H} \sum_{w=1}^{W} (\boldsymbol{X}_m^k - \mu_m^k)^2} \quad \in \mathbb{R}^{B \times C}. \tag{2}$$

As the abstract of latent features, these feature statistics carry domain-specific information (*e.g.*, style). They are instrumental to image generation (Huang & Belongie, 2017), and has been recently used for data augmentation in deep recognition (Li et al., 2021). In heterogeneous federated learning scenarios, the feature statistics among local clients will be inconsistent, and exhibit uncertain feature statistic shifts from the statistics of the true distribution. Our method explicitly captures such shift via probabilistic modeling. Specifically, we hypothesize that each feature statistic follows a multi-variate Gaussian distribution, *i.e.*, $\mu_m^k \sim \mathcal{N}(\mu_m^k, \hat{\Sigma}_{\mu_m^k}^2)$ and $\sigma_m^k \sim \mathcal{N}(\sigma_m^k, \hat{\Sigma}_{\sigma_m^k}^2)$, where each Gaussian's center corresponds to the original statistic, and the variance is an estimation of the potential feature statistic shift from the true distribution.

Determining an appropriate variant range is challenging since each client has access to only the data itself, and has no sense of its statistic bias. Recent research (Wang et al., 2019; Upchurch et al., 2017) shows that deep feature space contain many semantic directions, and feature variances provide a reasonable measurement to potential meaningful semantic changes along the directions. This motivates us to estimate the variance of Gaussian from *the variance of feature statistics*.

Client Specific Statistic Variances. In client-side, we compute *client-specific* variances of feature statistics based on the information within each mini-batch:

$$\Sigma_{\mu_m^k}^2 = \frac{1}{B} \sum_{b=1}^{B} (\mu_m^k - \mathbb{E}[\mu_m^k])^2 \quad \in \mathbb{R}^C, \qquad \Sigma_{\sigma_m^k}^2 = \frac{1}{B} \sum_{b=1}^{B} (\sigma_m^k - \mathbb{E}[\sigma_m^k])^2 \quad \in \mathbb{R}^C, \tag{3}$$

where $\Sigma_{\mu_m^k}^2$ and $\Sigma_{\sigma_m^k}^2$ denote the variance of feature mean μ_m^k and standard deviation σ_m^k that are specific to each client. Each value in $\Sigma_{\mu_m^k}^2$ or $\Sigma_{\sigma_m^k}^2$ is the variance of feature statistics in a particular channel, and its magnitude manifests how the channel will change potentially in the particular client.

Client Sharing Statistic Variances. The client specific statistic variances are solely computed based on the data in each client, and thus likely biased due to local dataset bias. To solve this, we further estimate client sharing feature statistic variances taking information of all clients into account. Particularly, we maintain a momentum version of feature statistics for each client, which are online estimated during training:

$$\bar{\mu}_m^k \leftarrow \alpha \bar{\mu}_m^k + (1-\alpha) \frac{1}{B} \sum_{b=1}^{B} \mu_m^k \quad \in \mathbb{R}^C, \qquad \bar{\sigma}_m^k \leftarrow \alpha \bar{\sigma}_m^k + (1-\alpha) \frac{1}{B} \sum_{b=1}^{B} \sigma_m^k \quad \in \mathbb{R}^C, \tag{4}$$

where $\bar{\mu}_m^k$ and $\bar{\sigma}_m^k$ are the momentum updated feature statistics of layer h^k in client m, and they are initialized as C-dimensional all-zero and all-one vectors, respectively. α is a momentum coefficient. We set a same α for both updating, and found no benefit to set it differently. In each communication, these accumulated local feature statistics are sent to the server along with model parameters. Let $\bar{\mu}^k = [\bar{\mu}_1^k, \cdots, \bar{\mu}_M^k] \in \mathbb{R}^{M \times C}$ and $\bar{\sigma}^k = [\bar{\sigma}_1^k, \cdots, \bar{\sigma}_M^k] \in \mathbb{R}^{M \times C}$ denote collections of accumulated feature statistics of all clients, the client sharing statistic variances are determined by:

$$\Sigma^2_{\mu^k} = \frac{1}{M}\sum_{m=1}^{M}(\bar{\mu}_m^k - \mathbb{E}[\bar{\mu}^k])^2 \ \in \mathbb{R}^C, \quad \Sigma^2_{\sigma^k} = \frac{1}{M}\sum_{m=1}^{M}(\bar{\sigma}_m^k - \mathbb{E}[\bar{\sigma}^k])^2 \ \in \mathbb{R}^C. \tag{5}$$

Along with the aggregated model parameters in FEDAVG, these variances are distributed back to each client to inform a global estimation of feature statistic variances. Note that $\{\Sigma^2_{\mu^k}, \Sigma^2_{\sigma^k}\}$ are shared by all participating clients.

Adaptive Variance Fusion. Client sharing estimations $\{\Sigma^2_{\mu^k}, \Sigma^2_{\sigma^k}\}$ provide a quantification of distribution difference among clients, and larger values imply potentials of more significant changes of corresponding channels in the true feature statistic space. Therefore, for each client, we weight the client specific statistic variances $\{\Sigma^2_{\mu_m^k}, \Sigma^2_{\sigma_m^k}\}$ by $\{\Sigma^2_{\mu^k}, \Sigma^2_{\sigma^k}\}$, so that each client has a sense of such difference. In addition, it is intuitive that some channels are more potentially to change than others, and it will be favorable to highlight these channels to enable a sufficient and reasonable exploration of the space of feature statistics. To this end, we further modulate client sharing estimations with a *Student's t-distribution* (Student, 1908; Van der Maaten & Hinton, 2008) with one degree of freedom to convert the variances to probabilities. The *t-distribution* has heavier tails than other alternatives such as Gaussian distribution, allowing to highlight the channels with larger statistic variance, at the same time, avoiding overly penalizing the others. Formally, the client sharing feature statistic variances of the jth channel at layer h^k turn into:

$$\gamma^{(j)}_{\mu^k} = \frac{C(1 + {}^{1}/_{\Sigma^{2,(j)}_{\mu^k}})^{-1}}{\sum_{c=1}^{C}(1 + {}^{1}/_{\Sigma^{2,(j)}_{\mu^c}})^{-1}}, \quad \gamma^{(j)}_{\sigma^k} = \frac{C(1 + {}^{1}/_{\Sigma^{2,(j)}_{\sigma^k}})^{-1}}{\sum_{c=1}^{C}(1 + {}^{1}/_{\Sigma^{2,(j)}_{\sigma^c}})^{-1}}. \tag{6}$$

In this way, the channels with higher variances in $\Sigma^2_{\mu^k}$ or $\Sigma^2_{\sigma^k}$ will be assigned with even higher importance than other channels, which enables more extensive augmentation along those directions. To avoid overly modification of client specific statistic variances, we add a residual connection for fusion, yielding an estimation of Gaussian ranges as follows:

$$\hat{\Sigma}^2_{\mu_m^k} = (\gamma_{\mu^k} + 1)\Sigma^2_{\mu_m^k}, \quad \hat{\Sigma}^2_{\sigma_m^k} = (\gamma_{\sigma^k} + 1)\Sigma^2_{\sigma_m^k}. \tag{7}$$

Implementation of Feature Augmentation. After establishing the Gaussian distribution, we synthesize novel feature $\hat{\boldsymbol{X}}_m^k$ in the vicinity of $\boldsymbol{X}_m^k$ as follows:

$$\hat{\boldsymbol{X}}_m^k = \hat{\sigma}_m^k \frac{\boldsymbol{X}_m^k - \mu_m^k}{\sigma_m^k} + \hat{\mu}_m^k, \quad \text{where } \hat{\mu}_m^k \sim \mathcal{N}(\mu_m^k, \hat{\Sigma}^2_{\mu_m^k}), \hat{\sigma}_m^k \sim \mathcal{N}(\sigma_m^k, \hat{\Sigma}^2_{\sigma_m^k}). \tag{8}$$

Here $\boldsymbol{X}_m^k$ is first normalized with its original statistics by ${}^{(\boldsymbol{X}_m^k - \mu_m^k)}/_{\sigma_m^k}$, and further scaled with novel statistics $\{\hat{\mu}_m^k, \hat{\sigma}_m^k\}$ that are randomly sampled from corresponding Gaussian distribution. To make the sampling differentiable, we apply the re-parameterization trick (Kingma & Welling, 2013) in our implementation:

$$\hat{\mu}_m^k = \mu_m^k + \epsilon_\mu \hat{\Sigma}_{\mu_m^k}, \quad \hat{\sigma}_m^k = \sigma_m^k + \epsilon_\sigma \hat{\Sigma}_{\sigma_m^k}, \tag{9}$$

where $\epsilon_\mu \sim \mathcal{N}(0, 1)$ and $\epsilon_\sigma \sim \mathcal{N}(0, 1)$ follow the normal Gaussian distribution.

The proposed federated feature augmentation (FFA) operation in Eq. 8 is a plug-and-play layer, which can be inserted at arbitrary positions of the feature extractor h to facilitate latent semantic augmentation. In our implementation, we add a FFA layer after each convolutional stage in AlexNet or U-Net (see Table 8 and Table 12 for detailed network structures). During training, we follow the stochastic learning strategy (Verma et al., 2019; Zhou et al., 2021) to activate each FFA layer with a probability of p, which allows for more diverse augmentation from iteration to iteration (based on the activated FFA layers). At test time, no augmentation is performed. In the Appendix, we provide detailed descriptions of FEDFA in Algorithm 1 and the FFA layer in Algorithm 2.

4 EXPERIMENT

We examine the efficacy of FEDFA against relevant algorithms (*e.g.*, FEDAVG, FEDPROX, FEDBN, FEDSAM, FEDMIX) on three datasets (*i.e.*, Office-Caltech 10, DomainNet, ProstateMRI) in two tasks, *i.e.*, image classification and medical image segmentation.

4.1 EXPERIMENTAL SETUP

Datasets. We conduct extensive experiments on three datasets, *i.e.*, Office-Caltech 10 (Gong et al., 2012) and DomainNet (Peng et al., 2019) for image classification, ProstateMRI (Liu et al., 2020b) for medical image segmentation. **Office-Caltech 10** has four data sources, three from Office-31 (Saenko et al., 2010) and one from Caltech-256 (Griffin et al., 2007). They are collected from different camera devices or in diverse environments with different background. **DomainNet** contains images from six domains (clipart, infograph, painting, real, and sketch), which are collected by searching a category name along with a domain name in different search engines. **ProstateMRI** is a multi-site prostate segmentation dataset consisting of six data sources of T2-weighted MRI from different medical institutions. For all the three datasets, we regard each data source as a client, and thus real-world feature shift exists among clients.

Baselines. For comprehensive evaluation, we compare FEDFA against several state-of-the-art federated learning techniques, including FEDAVG (McMahan et al., 2017) and some variants such as FEDAVGM (Hsu et al., 2019), FEDPROX (Li et al., 2020a), FEDSAM (Qu et al., 2022), FEDBN (Li et al., 2020b). We also compare with FEDMIX (Yoon et al., 2021) that generalizes mixup into the federated learning scenarios. Moreover, we compare with a specialized algorithm FEDHARMO (Jiang et al., 2022) designed for medical image applications in ProstateMRI.

In addition, to gain more insights into FEDFA, we design two baseline variants: FEDFA-R(ANDOM) and FEDFA-C(LIENT). FEDFA-R randomly perturbs feature statistics based on Gaussian distribution with a same standard deviation for all channels, *i.e.*, $\hat{\Sigma}_{\mu_m^k} = \hat{\Sigma}_{\sigma_m^k} = \lambda$, where λ is set to 0.5. FEDFA-C performs augmentation based only on client specific statistic variances, *i.e.*, Eq. 7 turns into $\hat{\Sigma}^2_{\mu_m^k} = \Sigma^2_{\mu_m^k}, \hat{\Sigma}^2_{\sigma_m^k} = \Sigma^2_{\sigma_m^k}$.

Metrics. As conventions, we use top-1 accuracy for image classification and Dice coefficient for medical image segmentation, respectively. We report the performance only for the global model.

Implementation Details. We use PyTorch to implement FEDFA and other baselines. Two learning models are adopted for the two tasks: i) AlexNet (Krizhevsky et al., 2017) on Office-Caltech 10 and DomainNet using the SGD optimizer with learning rate 0.01 and batch size 32 and ii) U-Net (Ronneberger et al., 2015) on ProstateMRI using Adam as the optimizer with learning rate 1e-4 and batch size 16. The communication rounds are 400 for Office-Caltech 10 and DomainNet, and 500 for ProstateMRI, with the number of local update epoch setting to 1 in all cases. We run each experiment for **five times** with different seeds and report the mean performance. For all experiments, we set α and p to 0.99 and 0.5 by default. More details are provided in Appendices B-C.

4.2 MAIN RESULTS

We first present the overall results on the three benchmarks, *i.e.*, Office-Caltech 10 and DomainNet in Table 1 and Fig. 1, ProstateMRI in Table 2 and Fig. 2.

Results on Office-Caltech 10 and DomainNet. FEDFA *yields solid improvements over competing methods for image classification.* As presented in Table 1, FEDFA leads to consistent performance gains over the competitors across the benchmarks. The improvements over FEDAVG can be as large as **4.6%** and **3.7%** on Office-Caltech 10 and DomainNet, respectively. Moreover, in comparison to prior data augmentation-based algorithm FEDMIX, FEDFA also brings solid gains, *i.e.*, **3.3%** on Office-Caltech 10 and **2.2%** on DomainNet. This is en-

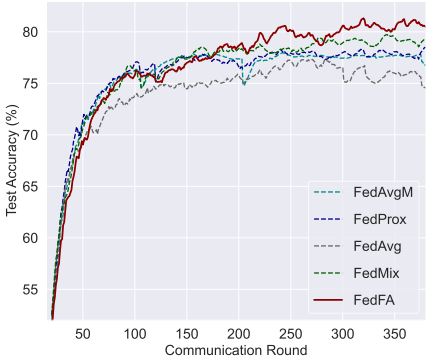

Figure 1: **Test accuracy versus communication rounds** on Office-Caltech 10.

Table 1: **Image classification performance on Office-Caltech 10 and DomainNet `test`.** Top-1 accuracy (%) is reported. Office-Caltech 10 has four clients: A(mazon), C(altech), D(SLR), and W(ebcam), while DomainNet has six: C(lipart), I(nfograph), P(ainting), Q(uickdraw), R(eal), and S(ketch). See §4.2 for details.

Algorithm	Office-Caltech 10 (Gong et al., 2012)					DomainNet (Peng et al., 2019)						
	A	C	D	W	Average	C	I	P	Q	R	S	Average
FEDAVG	84.4	66.7	75.0	88.1	78.5	71.5	33.2	57.8	76.5	72.9	65.2	62.8
FEDPROX	84.9	64.0	78.1	88.1	78.8	70.9	32.9	61.2	74.1	71.1	67.9	63.0
FEDSAM	81.7	63.1	50.0	81.4	69.1	60.1	30.1	53.0	64.8	61.9	47.3	52.9
FEDAVGM	85.9	64.0	71.9	94.9	79.2	79.8	33.3	58.8	72.6	72.8	66.1	62.5
FEDBN	82.3	63.6	81.2	94.9	80.5	72.4	32.7	64.3	74.0	69.9	70.8	64.0
FEDMIX	81.7	63.1	81.3	93.2	79.8	75.9	34.1	61.7	73.8	69.4	70.6	64.3
FEDFA	88.0	65.8	90.6	88.1	**83.1**	77.4	34.9	61.2	78.8	73.2	73.5	**66.5**

Table 2: **Medical image segmentation accuracy on *mini*-ProstateMRI `test`** (Liu et al., 2020b) with small-size local datasets. Dice score (%) is reported. The dataset consists of data from six medical institutions: B(IDMC), H(K), I(2CVB), (B)M(C), R(UNMC) and U(CL). The number in the bracket denotes the number of training samples in each client. See §4.2 for more details.

Algorithm	B (32)	H (32)	I (46)	M (38)	R (41)	U (32)	Average
FEDAVG	81.2	90.8	86.1	84.0	91.0	86.2	86.5
FEDPROX	82.8	89.1	89.8	79.5	89.8	85.6	86.1
FEDAVGM	80.3	91.6	88.2	82.2	91.2	86.5	86.7
FEDSAM	82.7	92.5	91.8	83.6	92.6	88.1	88.5
FEDMIX	86.3	91.6	89.6	88.1	89.8	85.2	88.4
FEDHARMO	86.7	91.6	92.7	84.2	92.5	84.6	88.7
FEDFA	85.7	92.6	91.0	85.4	92.9	89.2	**89.5**

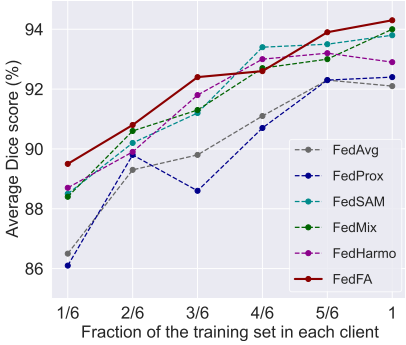

Figure 2: **Segmentation performance** w.r.t local data size (*i.e.*, fraction of training samples over the whole training set).

couraging since our approach in nature better preserves privacy than FEDMIX, which requires exchanging averaged data across clients. Moreover, Fig. 1 depicts the convergence curves of comparative methods on Office-Caltech 10. At the early training stage ($0 \sim 200$ rounds), FEDFA shows similar training efficiency as other baselines like FEDPROX and FEDMIX. But as the training goes, FEDFA is able to converge to a more optimal solution.

Results on ProstateMRI. FEDFA *shows leading performance with extremely small local datasets.* In some practical scenarios like healthcare, the size of local dataset can be very small, which poses a challenge for federated learning. To examine the performance of federated learning algorithms in this scenario, we build *mini*-ProstateMRI by randomly sampling only $1/6$ of all training samples in each client for training. Results are summarized in Table 2. FEDFA outperforms FEDAVG by significant margins (*i.e.*, **3.0%**) and it even performs better than FEDHARMO, which is specially designed for medical scenarios. In addition, Fig. 2 shows how the performance of methods varies with respect to the size of local dataset. We train methods with different fractions (*i.e.*, $1/6$, $2/6$, $3/6$, $4/6$, $5/6$, 1) of training samples . FEDFA shows promising performance in all cases.

4.3 FEDERATED DOMAIN GENERALIZATION PERFORMANCE

Federated learning are dynamic systems, in which novel clients may enter the system after model training, most possibly with test-time distribution shift. However, most prior federated learning algorithms focus only on improving model performance on the participating clients, while neglecting model generalizability to unseen non-participating clients. Distribution shift often occurs during deployment, thus it is essential to evaluate the generalizability of federated learning algorithms. With a core of data augmentation, FEDFA is supposed to enforce regularization to neural network learning, which could improve generalization capability.

To verify this, we perform experiments for federated domain generalization based on the *leave-one-client-out* strategy, *i.e.*, training on $M-1$ distributed clients and testing on the held-out unparticipating client. The results are presented in Table 3. As seen, FEDFA achieves leading gen-

Table 3: **Comparison of generalization performance to unseen test clients** on the three benchmarks (§4.2).

Algorithm	Office-Caltech 10					DomainNet							ProstateMRI						
	A	C	D	W	Avg	C	I	P	Q	R	S	Avg	B	H	I	M	R	U	Avg
FEDAVG	64.6	49.3	71.9	55.9	60.4	63.1	27.5	49.6	44.7	51.7	48.2	47.5	60.7	85.3	78.4	67.2	83.0	59.0	72.3
FEDPROX	63.0	50.7	68.7	**62.7**	61.3	62.2	26.9	49.6	42.4	50.5	48.9	46.8	61.5	86.2	**79.3**	68.6	84.5	62.4	73.8
FEDMIX	65.1	52.6	73.8	58.9	62.6	63.3	28.0	**50.1**	45.9	53.3	56.8	49.6	62.1	86.7	78.1	76.8	87.7	65.6	76.2
FEDFA	**65.6**	**54.2**	**78.1**	59.3	**64.3**	**64.1**	**28.8**	49.4	**47.5**	**56.6**	**61.0**	**51.2**	**64.0**	**88.3**	75.9	**79.0**	**89.1**	**68.8**	**77.5**

eralization performance on most unseen clients. For example, it yields consistent improvements as compared to FEDMIX, *i.e.*, **1.7%** on Office-Caltech 10, **1.6%** on DomainNet, and **1.3%** on ProstateMRI, in terms of average performance. Despite the improved performance, we find by comparing to the results reported in Table 1 and Table 2 that, current federated learning algorithms still encounter significant participation gap (Yuan et al., 2022), *i.e.*, the performance difference between participating and non-participating clients, which is a critical issue that should be tackled in future.

4.4 DIAGNOSTIC EXPERIMENT

We conduct a set of ablative experiments to enable a deep understanding of FEDFA.

FEDFA vs. FEDFA-C and FEDFA-R. We first verify the efficacy of FEDFA against the two baseline variants mentioned in §4.1. Both variants involve only device-dependent augmentation of feature statistics, without explicitly considering any global information as done in FEDFA. As shown in Table 4, by randomly perturbing feature statistics, FEDFA-R shows no improvements or even suffers performance degradation on DomainNet and ProstateMRI against FEDAVG; FEDFA-C yields promising performance gains by taking into account client-specific feature statistic variances; by comparing FEDFA and FEDFA-C, we confirm the significance of client-sharing feature statistic information in federated augmentation.

Table 4: Efficacy of FEDFA over FEDFA-C and FEDFA-R.

Variant	Office	DomainNet	ProstateMRI
FEDAVG	78.5	62.8	86.5
FEDFA-R	78.6	61.0	86.1
FEDFA-C	79.5	63.7	87.8
FEDFA	**83.1**	**66.5**	**89.5**

FEDFA vs. traditional augmentation methods. Furthermore, we compare FEDFA with four conventional data/feature augmentation techniques, *i.e.*, Mixup (Zhang et al., 2018), Manifold Mixup (Verma et al., 2019), MixStyle (Zhou et al., 2021) and MoEx (Li et al., 2021). The results are presented in Table 5. We show that i) all the four techniques yield non-trivial improvements over FEDAVG, and some of them (*e.g.*, MoEx) even outperform well-designed federated learning algorithms (as compared to Tables 1-2); by accounting for global feature statistics, FEDFA surpasses all of them, yielding **2.9%**/**1.9%**/**1.0%** improvements over the second-best results on Office/DomainNet/ProstateMRI, respectively; iii) combining FEDFA with these techniques allows further performance uplifting, verifying the complementary roles of FEDFA to them.

Table 5: Efficacy of FEDFA against augmentation techniques.

Algorithm	Office	DomainNet	ProstateMRI
FEDAVG	78.5	62.8	86.5
Mixup	79.2	63.4	87.0
M-Mixup	79.6	63.5	87.6
MixStyle	79.9	64.1	88.5
MoEx	80.2	64.6	88.3
FEDFA	**83.1**	**66.5**	**89.5**
FEDFA+Mixup	83.7	67.0	89.9
FEDFA+M-Mixup	83.6	66.9	90.2
FEDFA+MixStyle	84.0	67.2	90.2
FEDFA+MoEx	83.9	67.0	90.1

Adaptive Variance Fusion. Next, we examine the effect of adaptive variance fusion in Eqs. 6-7. We design a baseline "Direct Fusion" that directly combines the client-specific and client-sharing statistic variances as: $\hat{\Sigma}^2_{\mu^k_m} = (\Sigma^2_{\mu^k} + 1)\Sigma^2_{\mu^k_m}$, $\hat{\Sigma}^2_{\sigma^k_m} = (\Sigma^2_{\sigma^k} + 1)\Sigma^2_{\sigma^k_m}$. We find from Table 6 that the baseline encounters severe performance degradation across all three benchmarks. A possible reason is that the two types of variances are mostly mis-matched, and the simple fusion strategy may cause significant changes of client-specific statistic variances, which would be harmful for local model learning.

Table 6: Effectiveness of adaptive variance fusion.

Variant	Office	DomainNet	ProstateMRI
Direct Fusion	80.6	64.1	86.9
Adaptive Fusion	83.1	66.5	89.5

Estimation of Client Specific Statistic Variances Beyond mini-Batch. The client specific statistic variances are computed based on feature statistics of a mini-batch (Eq. 3), however, this may be inaccurate in cases of small batch size. To deal with such situations, we investigate an extension of FEDFA by equipping it an external memory bank (He et al., 2020; Wu et al., 2018) that stores the feature statistics in past mini-batches. This allows FEDFA to estimate variances from a larger number of samples, even with a small batch size. Table 7 summarizes the results of FEDFA with respect to different combinations of batch size and memory size on Office-Caltech 10. The default model with $(\text{bs} = 32, \text{ms} = 0)$ achieves a score of 83.1%. It is not surprising to see the improvements after increasing the batch size to 64 or 96. But it is indeed appealing that FEDFA delivers comparable performance by using the external memory bank (ms$=$ 32 or 64) to mimic the behavior of large batch sizees.

Table 7: Impacts of batch size (bs) and memory size (ms) on Office-Caltech 10.

(bs, ms)	(32, 0)	(64, 0)	(32, 32)	(96, 0)	(32, 64)
FEDFA	83.1	84.5	84.3	86.8	86.1

Hyper-parameter analysis. FEDFA includes two hyper-parameters, *i.e.*, momentum coefficient α in Eq. 4 and stochastic learning probability p to apply feature statistic augmentation during training. As illustrated in Fig. 3, i) the model is overall robust to α. Notably, the model yields promising performance at $\alpha = 0$, in which the model only uses limited client information, *i.e.*, the feature statistics of the last mini-batch in each local epoch, to compute client-sharing statistic variances. This result reveals that FEDFA is insensitive to errors of client sharing statistic variances. ii) For the probability p, we see that FEDFA significant promotes the baseline (*i.e.*, $p = 0$), even with a very small probability (*e.g.*, $p = 0.1$). The model achieves the best performance at $p = 0.5$, and its performance is relatively stable when p varies from 0.1 to 1.0.

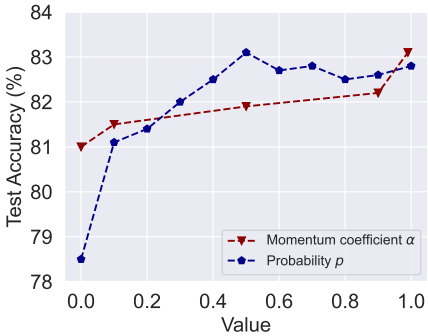

Figure 3: **Hyper-parameter analysis.**

4.5 COMPLEXITY ANALYSIS

Computation and memory costs. FEDFA involves only several basic matrix operations, thus incurring negligible extra computation cost. Compared to FEDAVG, it requires only 18 KB and 15.5 KB more GPU memory allocation to store $\{\bar{\mu}_m^k, \bar{\sigma}_m^k\}_{k=1}^K$ and $\{\Sigma_{\mu^k}^2, \Sigma_{\sigma^k}^2\}_{k=1}^K$ in AlexNet and U-Net, respectively. For comparison, FEDMIX requires around twice more GPU memory than FEDAVG. The low computation/memory costs make FEDFA favorable for edge devices such as mobile phones.

Communication cost. In each communication round, FEDFA incurs additional communication costs since it requires the sending 1) *from client to server* the momentum feature statistics $\bar{\mu}_m^k \in \mathbb{R}^C$ and $\bar{\sigma}_m^k \in \mathbb{R}^C$ (Eq. 4), as well as 2) *from server to client* the client sharing feature statistic variances $\Sigma_{\mu^k}^2 \in \mathbb{R}^C$ and $\Sigma_{\sigma^k}^2 \in \mathbb{R}^C$ (Eq. 5). Thus, for each layer, it requires to transmit $4C \times 32$ bit or $16C$ Byte additional data in each round. In our implementation, we add one FFA layer after each convolutional stage of the feature extractors in AlexNet and U-Net. *Please see Table 8 and Table 12 in Appendix for detailed architectures.* This leads to additional communication costs of **18 KB** and **15.5 KB** for AlexNet and U-Net, respectively. However, we note that these additional costs are quite minor in comparison with the costs for exchanging model parameters, which are **99 MB** for AlexNet and **59.2 MB** for U-Net. More details are provided in Appendix §D.

5 CONCLUSION

This work solves federated learning from a unique perspective of feature augmentation, yielding a new algorithm FEDFA that shows strong performance across various federated learning scenarios. FEDFA is based on a probabilistic (precisely Gaussian) modeling of feature statistics, where Gaussian variances are estimated in a federated manner, based on both local feature statistic distribution within each client, as well as more universal feature statistic distribution across clients. Feature augmentation is implicitly achieved by sampling novel feature statistics from the Gaussian distribution. We evaluate FEDFA across a suite of federated datasets, and the results confirm its superiority.

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This appendix provides additional details and more results for the ICLR 2023 submission – FEDFA: FEDERATED FEATURE AUGMENTATION. It is organized as follows:

- §A summarizes the algorithms of FEDFA in Algorithm 1 and the FFA layer in Algorithm 2;
- §B provides additional experimental details for image classification task;
- §C provides additional results and experimental details for medical image segmentation task;
- §D provides a more detailed analysis of extra communication cost required by FEDFA.

A DETAILED ALGORITHM

In Algorithm 1, we illustrate the detailed training procedure of our FEDFA. It is consistent with algorithms such as FEDAVG (McMahan et al., 2017). In each communication round, the client performs local model training of the feature extractor $h(\boldsymbol{w}_h)$ and classifier $g(\boldsymbol{w}_g)$. We append a FFA layer (Algorithm 2) after each convolutional stage h^k. Each client additionally maintains a pair of momentum feature statistics $\{\bar{\mu}_m, \bar{\sigma}_m\}$, which is updated in a momentum manner during training. The parameters from local training (*i.e.*, $\boldsymbol{w} = \{\boldsymbol{w}_h, \boldsymbol{w}_g\}$), which are omitted in Algorithm 1, along with the momentum feature statistics are sent to server for model aggregation and computation of client-sharing statistic variances, which will be distributed back to clients for the next round of local training.

Algorithm 1 FEDFA: federated training phase. (We omit the parameter updating procedure, which is exactly same to FEDAVG.)

Input: Number of clients M; number of communication rounds T; neural network $f = g \circ h$; each $\hat{\boldsymbol{X}}_m^0$ represents the collection of training images in corresponding clients;
Output: $\gamma_{\mu^k}, \gamma_{\sigma^k}$;

for $t = 1, 2, \ldots, T$ **do**
  for each client $m \in [M]$ **do**
    $\bar{\mu}_m = \mathbf{0}, \bar{\sigma}_m = \mathbf{1}$ ▷ Initialize averaged feature statistics for the client
    for each layer $k \in [K]$ **do**
      $\boldsymbol{X}_m^k = h^k(\hat{\boldsymbol{X}}_m^{k-1})$ ▷ Run the k-th layer of the feature extractor h
      $\hat{\boldsymbol{X}}_m^k, \bar{\mu}_m^k, \bar{\sigma}_m^k = \text{FFA}(\boldsymbol{X}_m^k, \bar{\mu}_m^k, \bar{\sigma}_m^k)$ ▷ FFA layer in Algorithm 2
    $Y = g(\hat{\boldsymbol{X}}_m^K)$ ▷ Run classifer g to get predictions
    Run loss computation and backward optimization
  $\Sigma^2_{\mu^k} = \frac{1}{M}\sum_{m=1}^{M}(\bar{\mu}_m^k - \mathbb{E}[\bar{\mu}^k])^2$ ▷ Compute client sharing statistic variance (Eq. 5)
  $\Sigma^2_{\sigma^k} = \frac{1}{M}\sum_{m=1}^{M}(\bar{\sigma}_m^k - \mathbb{E}[\bar{\sigma}^k])^2$
  for each channel $j \in [C]$ **do** ▷ Compute adaptive fusion coefficients (Eq. 6)
    $\gamma_{\mu^k}^{(j)} = \frac{C(1+1/\Sigma^{2,(j)}_{\mu^k})^{-1}}{\sum_{c=1}^{C}(1+1/\Sigma^{2,(j)}_{\mu^k})^{-1}}$
    $\gamma_{\sigma^k}^{(j)} = \frac{C(1+1/\Sigma^{2,(j)}_{\sigma^k})^{-1}}{\sum_{c=1}^{C}(1+1/\Sigma^{2,(j)}_{\sigma^k})^{-1}}$
return $\gamma_{\mu^k}, \gamma_{\sigma^k}$

B EXPERIMENTAL DETAILS FOR IMAGE CLASSIFICATION

Network Architecture. For the image classification tasks on Office-Caltech 10 (Gong et al., 2012) and DomainNet (Peng et al., 2019), we use an adapted AlexNet (Krizhevsky et al., 2017), with the detailed network architecture shown in Table 8.

Training Details. For each training image in Office-Caltech10 and DomainNet, we reshape its size into 256×256. We train AlexNet with the SGD optimizier with a learning rate of 0.01, a mini-batch size of 32, using the standard cross-entropy loss. The total number of communication round is set to 400, with one local epoch per round by default. Two basic data augmentation techniques are also applied for training, *i.e.*, random horizontal flipping and random rotation with degree in $[-30, 30]$. The dataset splits of Office-Caltech 10 and DomainNet in our experiments are summarized in Table 9 and Table 10, respectively.

Algorithm 2 Algorithm description of FFA for the kth layer in client m.

Input: Original feature $\boldsymbol{X}_m^k \in \mathbb{R}^{B\times C\times H\times W}$; momentum $\alpha = 0.99$; probability $p = 0.5$;
Client-sharing fusion coefficients $\gamma_{\mu^k} \in \mathbb{R}^C$ and $\gamma_{\sigma^k} \in \mathbb{R}^C$ downloaded from the server;
Accumulated feature statistics $\bar{\mu}_m^k \in \mathbb{R}^C$ and $\bar{\sigma}_m^k \in \mathbb{R}^C$;

Output: Augmented feature $\hat{\boldsymbol{X}}_m^k, \bar{\mu}_m^k, \bar{\sigma}_m^k$;

if np.random.random() $< p$ **then**

$\mu_m^k = \frac{1}{HW}\sum_{h=1}^{H}\sum_{w=1}^{W}\boldsymbol{X}_m^k$ ▷ Compute channel-wise feature statistics (Eq. 2)

$\sigma_m^k = \sqrt{\frac{1}{HW}\sum_{h=1}^{H}\sum_{w=1}^{W}(\boldsymbol{X}_m^k - \mu_m^k)^2}$

$\Sigma^2_{\mu_m^k} = \frac{1}{B}\sum_{b=1}^{B}(\mu_m^k - \mathbb{E}[\mu_m^k])^2$ ▷ Compute client specific statistic variances (Eq. 3)

$\Sigma^2_{\sigma_m^k} = \frac{1}{B}\sum_{b=1}^{B}(\sigma_m^k - \mathbb{E}[\sigma_m^k])^2$

$\hat{\Sigma}^2_{\mu_m^k} = (\gamma_{\mu^k} + 1)\Sigma^2_{\mu_m^k}$ ▷ Adaptive variance fusion (Eq. 7)

$\hat{\Sigma}^2_{\sigma_m^k} = (\gamma_{\sigma^k} + 1)\Sigma^2_{\sigma_m^k}$

$\hat{\mu}_m^k = \mu_m^k + \epsilon_\mu \hat{\Sigma}_{\mu_m^k}$ ▷ Sampling novel feature statistics (Eq. 9)

$\hat{\sigma}_m^k = \sigma_m^k + \epsilon_\sigma \hat{\Sigma}_{\sigma_m^k}$

$\hat{\boldsymbol{X}}_m^k = \hat{\sigma}_m^k \frac{\boldsymbol{X}_m^k - \mu_m^k}{\sigma_m^k} + \hat{\mu}_m^k$ ▷ Transform original feature based on novel statistics (Eq. 8)

$\bar{\mu}_m^k \leftarrow \alpha\bar{\mu}_m^k + (1-\alpha)\frac{1}{B}\sum_{b=1}^{B}\mu_m^k$ ▷ Momentum updating feature statistics (Eq. 5)

$\bar{\sigma}_m^k \leftarrow \alpha\bar{\sigma}_m^k + (1-\alpha)\frac{1}{B}\sum_{b=1}^{B}\sigma_m^k$

return $\hat{\boldsymbol{X}}_m^k, \bar{\mu}_m^k, \bar{\sigma}_m^k$

Table 8: **Network architecture of AlexNet** for Office-Caltech10 and DomainNet experiments. For convolutional layer (Conv2D), we list parameters with sequence of input and output dimension, kernal size, stride and padding. For max pooling layer (MaxPool2D), we list kernal and stride. For fully connected layer (FC), we list input and output dimension. For Batch Normalization layer (BN), we list the channel dimension. Note that **FA** denotes the proposed feature augmentation layer, and we list the dimension of its input feature.

Layer	Details
1	Conv2D(3, 64, 11, 4, 2), BN(64), ReLU, MaxPool2D(3, 2)
2	**FFA**(64)
3	Conv2D(64, 192, 5, 1, 2), BN(192), ReLU, MaxPool2D(3, 2)
4	**FFA**(192)
5	Conv2D(192, 384, 3, 1, 1), BN(384), ReLU
6	**FFA**(384)
7	Conv2D(384, 256, 3, 1, 1), BN(256), ReLU
8	**FFA**(256)
9	Conv2D(256, 256, 3, 1, 1), BN(256), ReLU, MaxPool2D(3, 2)
10	**FFA**(256)
11	AdaptiveAvgPool2D(6, 6)
12	FC(9216, 1024), BN(1024), ReLU
13	FC(1024, 1024), BN(1024), ReLU
14	FC(1024, num_class)

Table 9: Numbers of samples in the training, validation, and testing sets of each client in Office-Caltech 10 used in our experiments.

Split	Amazon	Caltech	DSLR	Webcam
`train`	459	538	75	141
`val`	307	360	50	95
`test`	192	225	32	59

Table 10: Numbers of samples in the training, validation, and testing sets of each client in DomainNet used in our experiments.

Split	Clipart	Infograph	Painting	Quickdraw	Real	Sketch
`train`	672	840	791	1280	1556	708
`val`	420	525	494	800	972	442
`test`	526	657	619	1000	1217	554

Table 11: Numbers of samples in the training, validation, and testing sets of each client in ProstateMRI used in our experiments.

Split	BIDMC	HK	I2CVB	BMC	RUNMC	UCL
`train`	156	94	280	230	246	105
`val`	52	31	93	76	82	35
`test`	52	31	93	76	82	35

C EXPERIMENTAL DETAILS FOR MEDICAL IMAGE SEGMENTATION

Network Architecture. For medical image segmentation on ProstateMRI (Liu et al., 2020b), we use a vanilla U-Net architecture, as presented in Table 12 and Table 13.

Training Details. Following FEDHARMO, we use a combination of standard cross-entropy and Dice loss to train the network, using the Adam optimizer with learning rate 1e-4, batch size 16, and weight decay 1e-4. No any data augmentation techniques are applied. The dataset splits of ProstateMRI used in our experiments are summarized in Table 11

Additional Results. Table 14 provides a detailed performance statistic of different methods on ProstateMRI, w.r.t. different fractions ($1/6$, $2/6$, $3/6$, $4/6$, $5/6$, 1) of training samples used in each client. The table corresponds to the plot in Fig. 2.

Table 12: **Network architecture of U-Net** for medical image segmentation experiments on ProstateMRI. The structure of 'Block' module is provided in Table 13. Note that **FA** denotes the proposed feature augmentation layer, and we list the dimension of its input feature.

Layer	Details
1	Block(in_features=3, features=32, name="encoder1"), MaxPool2D(2, 2)
2	FFA(32)
3	Block(in_features=32, features=64, name="encoder2"), MaxPool2D(2, 2)
4	FFA(64)
5	Block(in_features=64, features=128, name="encoder3"), MaxPool2D(2, 2)
6	FFA(128)
7	Block(in_features=128, features=256, name="encoder4"), MaxPool2D(2, 2)
8	FFA(256)
9	Block(in_features=256, features=512, name="bottleneck")
10	FFA(512)
11	Block(in_features=512, features=256, name="decoder4")
12	Block(in_features=256, features=128, name="decoder3")
13	Block(in_features=128, features=64, name="decoder2")
14	Block(in_features=64, features=32, name="decoder1")
15	Conv2d(32, num_class, 1, 1)

Table 13: **Detailed structure** of the 'Block' module in U-Net (Table 12)

Layer	Details
1	Conv2d(in_features, features, 3, 1)
2	BatchNorm2d(features)
3	ReLU
4	Conv2d(features, features, 3, 1)
5	BatchNorm2d(features)
6	ReLU

D ANALYSIS OF ADDITIONAL COMMUNICATION COST IN FEDFA

In each communication round, FEDFA incurs additional communication costs over FEDAVG, since it requires the sending 1) *from client to server* the averaged feature statistics $\bar{\mu}_m^k \in \mathbb{R}^C$ and $\bar{\sigma}_m^k \in \mathbb{R}^C$ (Eq. 4), as well as 2) *from server to client* the client-sharing statistic variances $\Sigma^2_{\mu^k} \in \mathbb{R}^C$ and $\Sigma^2_{\sigma^k} \in \mathbb{R}^C$ (Eq. 5). Thus, for each layer, it requires to transmit $4C \times 32$ bit or $16C$ Byte additional data in each round. As presented in Table 8 and Table 12, we append one FFA layer after each convolutional stage of feature extractors in AlexNet and U-Net. Hence, the total additional communication costs for AlexNet and U-Net are:

$$\begin{aligned} \text{AlexNet:} \quad & 16 \times (64 + 192 + 384 + 256 + 256)/1024 = 18 \text{ KB}, \\ \text{U-Net:} \quad & 16 \times (32 + 64 + 128 + 256 + 512)/1024 = 15.5 \text{ KB}. \end{aligned} \tag{10}$$

However, it should be noted that these additional costs are minor in comparison with the cost required for exchanging model parameters, which are 2×49.5 MB and 2×29.6 MB for AlexNet and U-Net, respectively.

Table 14: **Segmentation performance on ProstateMRI `test`** (Liu et al., 2020b) in terms of Dice score (%). We sample different fractions ([1/6, 2/6, 3/6, 4/6, 5/6, 1]) of training samples over the original training set in each client to study the effects of methods w.r.t the variations of local training size. *The table provides a detailed statistic for Fig. 2.*

Algorithm	BIDMC	HK	I2CVB	BMC	RUNMC	UCL	Average
fraction of training samples over the whole training set: 1/6							
FedAvg (McMahan et al., 2017)	81.2	90.8	86.1	84.0	91.0	86.2	86.5
FedProx (Li et al., 2020a)	82.8	89.1	89.8	79.4	89.8	85.6	86.1
FedAvgM (Hsu et al., 2019)	80.3	91.6	88.2	82.2	91.2	86.5	86.7
FedSAM (Qu et al., 2022)	82.7	92.5	91.8	83.6	92.6	88.1	88.5
FedHarmo (Jiang et al., 2022)	86.7	91.6	92.7	84.2	92.5	84.6	88.7
FedMix (Yoon et al., 2021)	86.3	91.6	89.6	88.1	89.8	85.2	88.4
FedFA-R	78.9	91.3	87.0	81.9	90.6	86.6	86.1
FedFA-C	80.5	92.4	89.2	83.7	92.1	89.4	87.9
FedFA	85.7	92.6	91.0	85.4	92.9	89.2	**89.5**
fraction of training samples over the whole training set: 2/6							
FedAvg (McMahan et al., 2017)	83.5	92.4	90.1	86.5	93.7	89.4	89.3
FedProx (Li et al., 2020a)	83.9	92.7	93.7	86.2	94.0	88.6	89.8
FedAvgM (Hsu et al., 2019)	80.8	91.8	91.7	83.5	93.5	86.1	87.9
FedSAM (Qu et al., 2022)	83.6	93.7	94.3	86.6	94.7	88.2	90.2
FedHarmo (Jiang et al., 2022)	85.6	90.8	92.5	88.5	94.3	87.6	89.9
FedMix (Yoon et al., 2021)	88.6	92.7	93.3	90.0	91.7	87.3	90.6
FedFA-R	81.5	92.1	90.9	84.2	93.1	89.4	88.5
FedFA-C	81.1	92.0	92.9	85.2	94.0	86.9	88.7
FedFA	87.8	92.3	92.9	86.6	95.1	89.8	**90.8**
fraction of training samples over the whole training set: 3/6							
FedAvg (McMahan et al., 2017)	84.2	90.9	93.9	87.0	93.8	89.1	89.8
FedProx (Li et al., 2020a)	82.0	92.5	92.0	84.7	92.3	88.1	88.6
FedAvgM (Hsu et al., 2019)	81.8	92.0	94.4	85.7	93.5	88.7	89.3
FedSAM (Qu et al., 2022)	85.1	92.9	95.0	88.2	95.4	90.3	91.2
FedHarmo (Jiang et al., 2022)	92.2	90.9	96.3	89.8	95.0	86.7	91.8
FedMix (Yoon et al., 2021)	87.2	92.8	94.9	90.1	92.5	90.0	91.3
FedFA-R	82.7	92.8	94.4	87.0	94.7	88.2	90.0
FedFA-C	87.0	91.1	93.5	90.3	93.9	89.4	90.9
FedFA	87.4	93.5	95.6	90.6	95.6	91.4	**92.4**
fraction of training samples over the whole training set: 4/6							
FedAvg (McMahan et al., 2017)	86.4	92.3	95.7	87.7	95.2	89.3	91.1
FedProx (Li et al., 2020a)	87.2	92.9	94.0	85.8	94.5	89.7	90.7
FedAvgM (Hsu et al., 2019)	85.6	93.0	95.0	84.9	94.8	87.3	90.1
FedSAM (Qu et al., 2022)	91.3	93.8	95.8	91.1	96.0	92.5	**93.4**
FedHarmo (Jiang et al., 2022)	91.0	94.2	94.3	90.3	95.8	92.2	93.0
FedMix (Yoon et al., 2021)	90.0	94.2	95.5	91.7	93.2	91.5	92.7
FedFA-R	84.9	91.1	95.2	86.0	95.4	91.2	90.6
FedFA-C	87.4	93.6	95.2	88.8	95.4	91.4	92.0
FedFA	91.1	93.6	95.1	89.5	95.3	91.2	92.6
fraction of training samples over the whole training set: 5/6							
FedAvg (McMahan et al., 2017)	89.2	94.2	94.8	89.0	95.1	91.3	92.3
FedProx (Li et al., 2020a)	88.7	94.7	94.8	88.9	95.6	91.1	92.3
FedAvgM (Hsu et al., 2019)	87.7	94.6	94.3	89.3	95.2	90.4	91.9
FedSAM (Qu et al., 2022)	91.9	95.2	96.1	90.7	96.3	91.2	93.5
FedHarmo (Jiang et al., 2022)	89.8	94.5	95.6	91.0	96.0	92.1	93.2
FedMix (Yoon et al., 2021)	91.6	92.9	94.4	92.8	94.0	92.0	93.0
FedFA-R	89.9	94.6	95.6	88.8	95.7	91.4	92.7
FedFA-C	90.3	94.7	95.5	88.7	95.8	91.5	92.7
FedFA	93.2	95.1	96.4	91.2	96.3	91.3	**93.9**
fraction of training samples over the whole training set: 1							
FedAvg (McMahan et al., 2017)	89.5	94.0	95.6	87.5	95.1	91.1	92.1
FedProx (Li et al., 2020a)	88.2	94.1	95.6	88.8	95.9	91.6	92.4
FedAvgM (Hsu et al., 2019)	92.1	94.2	96.0	87.4	95.0	90.6	92.6
FedSAM (Qu et al., 2022)	92.0	95.4	96.6	90.1	96.3	92.2	93.8
FedHarmo (Jiang et al., 2022)	87.4	95.0	95.5	91.2	96.1	92.2	92.9
FedMix (Yoon et al., 2021)	93.7	95.2	95.7	91.9	94.8	92.8	94.0
FedFA-R	87.1	92.5	95.0	86.9	95.7	90.8	91.3
FedFA-C	91.5	93.4	96.5	88.9	95.4	91.6	92.9
FedFA	93.7	95.4	96.0	92.2	96.2	92.5	**94.3**