Data Augmentation Policy Search for Long-Term Forecasting

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Abstract

Data augmentation serves as a popular regularization technique to combat overfitting challenges in neural networks. While automatic augmentation has demonstrated success in image classification tasks, its application to time-series problems, particularly in long-term forecasting, has received comparatively less attention. To address this gap, we introduce a time-series automatic augmentation approach named TSAA, which is both efficient and easy to implement. The solution involves tackling the associated bilevel optimization problem through a two-step process: initially training a non-augmented model for a limited number of epochs, followed by an iterative split procedure. During this iterative process, we alternate between identifying a robust augmentation policy through Bayesian optimization and refining the model while discarding suboptimal runs. Extensive evaluations on challenging univariate and multivariate forecasting benchmark problems demonstrate that TSAA consistently outperforms several robust baselines, suggesting its potential integration into prediction pipelines.

1 Introduction

Modern machine learning tools require large volumes of data to effectively solve challenging tasks. However, high-quality labeled data is difficult to obtain as manual labeling is costly and it may require human expertise (Shorten & Khoshgoftaar, 2019). Small datasets may lead to overfitting in overparameterized models, a phenomenon in which the model struggles with examples it has not seen before (Allen-Zhu et al., 2019). One of the effective methods to alleviate poor generalization issues is via *data augmentation* (DA). Data augmentation aims to generate artificial new examples whose statistical features match the true distribution of the data (Simard et al., 1998). In practice, DA has been shown to achieve state-of-the-art (SOTA) results in e.g., vision (Krizhevsky et al., 2012) and natural language (Wei & Zou, 2019) tasks.

Unfortunately, DA is not free from challenges. For instance, Tian et al. (2020b) showed that the effectivity of augmented samples depends on the downstream task. To this end, recent approaches explored automatic augmentation tools, where a good DA policy is searched for (Lemley et al., 2017; Cubuk et al., 2019). While automatic frameworks achieved impressive results on image classification tasks (Zheng et al., 2022) and other data modalities, problems with time-series data received significantly less attention. Toward bridging this gap, we propose in this work a new automatic data augmentation method, designed for *time-series forecasting* problems.

Time-series forecasting is a long-standing task in numerous scientific and engineering fields (Chatfield, 2000). While deep learning techniques achieved groundbreaking results on vision and NLP problems already a decade ago, time-series forecasting (TSF) was considered by many to be too challenging for deep models, up until recently (Oreshkin et al., 2020). While recent linear approaches showed interesting forecast results (Zeng et al., 2023), existing SOTA approaches for TSF are based on deep learning architectures that are structurally similar to vision models. In particular, current TSF deep models are overparameterized, and thus they may benefit from similar regularization techniques which were found effective for vision models, such as (automatic) data augmentation. Ultimately, our work is motivated by the limited availability of DA tools for time-series tasks (Wen et al., 2020).

The main contributions of our work can be summarized as follows: 1) We develop a novel automatic data augmentation approach for long-term time-series forecasting tasks. Our approach is based on a carefully

designed dictionary of time-series transformations, Bayesian optimization for policy search, and pruning tools that enforce early stopping of ineffective networks. While these components appear in existing work, their combination and adaptation to time-series forecasting was not done before, to the best of our knowledge. 2) We analyze the optimal policies our approach finds. Our analysis sheds light into the most effective transformations, and it may inspire others in designing effective data augmentation techniques for time-series data. 3) Our approach augments existing time-series forecasting baselines, and we extensively evaluated it on long-term forecasting univariate and multivariate TSF benchmarks with respect to several strong baseline architectures. We find that our framework enhances performance in most long-term forecast settings and across most datasets and baseline architectures.

2 Related Work

Time-series forecasting. Recently, several neural network approaches for TSF have been proposed. Based on recurrent neural networks, DeepAR (Salinas et al., 2020) produced probabilistic forecasts with uncertainty quantification. The N-BEATS (Oreshkin et al., 2020) model employs fully connected layers with skip connections, and subsequent work (Challu et al., 2022) improved long-term forecasting via pooling and interpolation. Another line of works based on the transformer architecture (Vaswani et al., 2017) used a sparse encoder and a generative decoder in the Informer (Zhou et al., 2021), trend-seasonality decomposition in the Autoformer (Wu et al., 2021), and Fourier and Wavelet transformations in the FEDformer (Zhou et al., 2022). Recently, Pyraformer (Liu et al., 2021) significantly reduced the complexity bottleneck of the attention mechanism, PatchTST (Nie et al., 2023) exchanges the point-wise attention input with a tokenized sub-series representation. Finally, Zeng et al. (2023) propose a single-layer MLP with a larger input lookback.

Data augmentation. DA techniques have appeared since the early rise of modern deep learning to promote labeled image invariance to certain transformations (Krizhevsky et al., 2012). Typical image augmentations include rotation, scaling, crop, and color manipulations. Recent methods focused on modality-agnostic methods which blend linearly the inputs and labels (Zhang et al., 2018). Other works produce augmented views in the feature space (DeVries & Taylor, 2017; Verma et al., 2019). In contrast to image and text data, augmenting arbitrary time-series (TS) data have received less attention in the literature (Wen et al., 2020; Iwana & Uchida, 2021). In the review (Wen et al., 2020), the authors consider three different tasks: TS classification, TS anomaly detection, and TS forecasting. Their analysis is based on common time-series augmentation approaches such as scaling, adding noise (Um et al., 2017), window cropping or slicing, and stretching of time intervals (Le Guennec et al., 2016), dynamic time warping (Ismail Fawaz et al., 2019), perturbations of the frequency domain (Gao et al., 2020; Chen et al., 2023), and utilizing surrogate data (Lee et al., 2019). In (Smyl & Kuber, 2016), the authors discuss additional TS augmentation approaches including generating new TS using the residuals of a statistical TS (Bergmeir et al., 2016). Another technique would be to sub-sample the parameters, residuals, and forecasting from MCMC Bayesian models. The survey (Iwana & Uchida, 2021) further details a large list of TS augmentations such as jittering, rotation, time warping, time masking, interpolation and others in the context of time-series classification. Finally, the authors in (Wen et al., 2020) propose the selection and combination of augmentations using automatic approaches as a promising avenue for future research, which is the focus of the current work. We show in Fig. 1 (top) two examples of DA policies we use.

Automatic DA. To avoid hand-tailored DA, recent efforts aimed for automatic tools, motivated by similar advances in neural architecture search (NAS) approaches (Zoph & Le, 2017). AutoAugment (Cubuk et al., 2019) used a recurrent controller along with reinforcement learning for the search process, yielding a highly effective but computationally intensive framework. Following works such as Fast AutoAugment employed Bayesian optimization and density matching (Lim et al., 2019). RandAugment (Cubuk et al., 2020) reduces the search space significantly by introducing stochasticity. Tian et al. (2020a) suggested partial training using augmentation-wise weight sharing (AWS). Further, recent approaches utilize gradients for the search problem, including the differentiable automatic DA (DADA) (Li et al., 2020b) and Deep AutoAugment (Zheng et al., 2022). Cheung & Yeung (2020) developed automatic DA that does not depend on the data-modality as it exploits latent transformations. In (Fons et al., 2021), the authors propose adaptive-weighting strategies which favor a subset of time-series DA for classification, based on their effect on the training loss.

3 Background

Below, we briefly describe background information on Bayesian optimization and pruning approaches which we use to find the best augmentation policy and improve model training efficiency, respectively.

Tree-structured Parzen Estimators and the Expected Improvement. Bayesian optimization relates to a family of techniques where an objective function $f(x) : \mathbb{R}^d \rightarrow \mathbb{R}^+$ is minimized, i.e.,

$$\min_x f(x) \ . \tag{1}$$

In the typical setting, f is costly to evaluate, its gradients are not available, and $d \leq 20$. For instance, finding the hyperparameters (x) of a neural network (f) is a common use case for Bayesian optimization (Bergstra et al., 2013). Unlike grid/random search, Bayesian optimization methods utilize past evaluations of f to maintain a surrogate model $p(y|x)$ for the objective function $y = f(x)$. Thus, Bayesian optimization solves equation 1 while limiting the costly evaluations of f to a minimum.

A practical realization of Bayesian optimization is given by Sequential Model-Based Optimization (SMBO) (Hutter et al., 2011). SMBO iterates between model fitting with the existing parameters (exploitation) to parameter selection using the current model (exploration). SMBO constructs a surrogate model $p(y|x)$, finds a set of parameters x that performs best on the $p(y|x)$ using an acquisition function, applies the objective function f on x to obtain the score y, updates the surrogate model, and repeats the last three steps until convergence. Most SMBO techniques differ in their choice of the surrogate model and acquisition function. We will focus on Tree-structured Parzen Estimator (TPE) for the surrogate model, combined with Expected Improvement for the acquisition function. The main idea behind TPE is to model the surrogate via two distributions, $l(x)$ and $g(x)$, corresponding to model evaluations that yield positive, and negative improvement. Formally,

$$p(x|y) = \begin{cases} l(x) & y < y^* \\ g(x) & y \geq y^* \end{cases} \ , \tag{2}$$

where y^* is a threshold score, and the surrogate model is obtained via Bayes rule. It can be shown that maximizing $l(x)/g(x)$ leads to an optimal Expected Improvement (EI) (Bergstra et al., 2011).

Asynchronous Successive Halving. While Bayesian optimization uses a minimal number of evaluations of f, the overall minimization is computationally demanding due to the high cost of f, e.g., if f is a neural network that needs to be trained. To alleviate some of these costs, Asynchronous Successive Halving (ASHA) (Jamieson & Talwalkar, 2016; Li et al., 2020a) enforces early stopping of poorly performing parameters x, whereas parameters with low $l(x)$, are trained to the fullest. In a fixed budget system, given a maximum resource R, minimum resource r, and a reduction factor η, ASHA works as follows. One creates model checkpoints during the training process at epochs η^j where $j = 1, \ldots, \lfloor \log_\eta R/r \rfloor$. Each checkpoint is referred

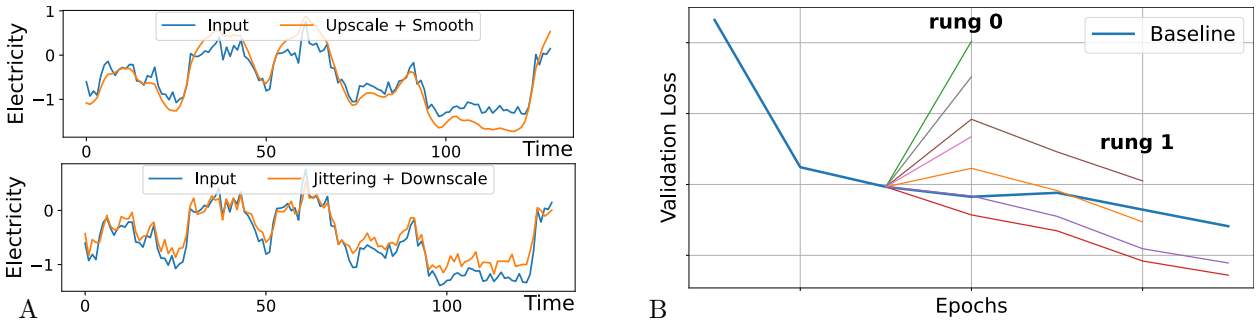

Figure 1: A) Two examples of sub-policies applied on Electricity data. B) The above plot demonstrates the behavior of ASHA with respect to the baseline model (blue). Some of the poorly performing runs are discontinued at the end of rungs, whereas the other runs train to completion.

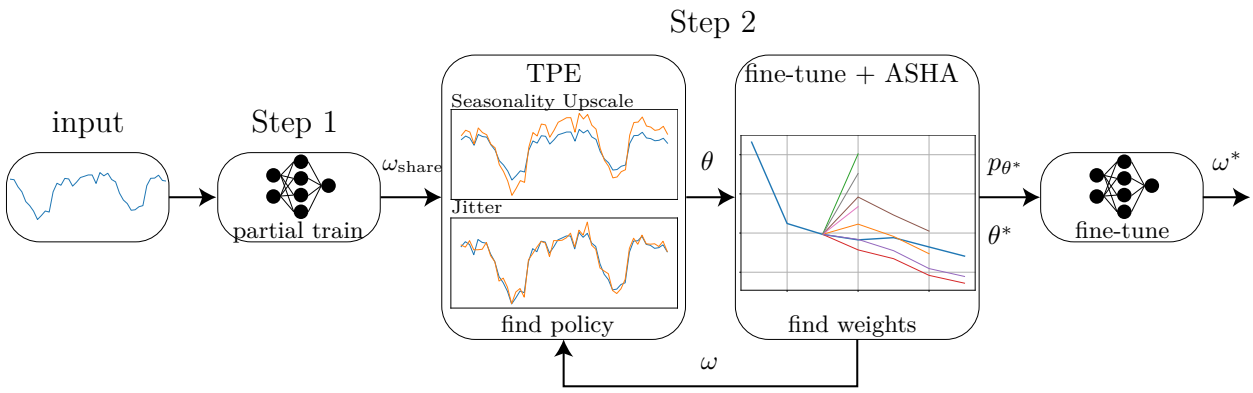

Figure 2: Our time-series automatic augmentation (TSAA) approach is based on a partial train of the model (Step 1), followed by an iterative process (Step 2) where we alternate between improving the augmentation policy θ to training the model weights ω. We find ω^* by fine-tuning over p_{θ^*}.

to as a *rung*, and at the end of each rung, one keeps only the best $\frac{1}{\eta}$ runs. To avoid waiting for all runs to reach the next rung, ASHA performs asynchronous evaluations to promote or halt runs on the go. We illustrate in Fig. 1 (bottom) an example of a baseline model with multiple different runs, administered by the ASHA policy.

4 Time-Series AutoAugment (TSAA)

Automatic augmentation via bi-level optimization. The task of finding data augmentations automatically during the training of a deep neural network model can be formulated as a bi-level optimization problem, see e.g., (Li et al., 2020b). Namely,

$$\min_{\theta} \quad \mathcal{L}_{\text{val}}(\omega, \theta) \tag{3}$$

$$\text{subject to} \quad \min_{\omega} \mathbb{E}_{p_\theta} \left[\mathcal{L}_{\text{tr}}(\omega, \theta) \right] \ , \tag{4}$$

where $\mathcal{L}_{\text{tr}}$ and $\mathcal{L}_{\text{val}}$ denote the train and validation losses, respectively, typically mean squared error for TSF. The parameters ω and $\theta \sim p_\theta$ correspond to the network weights and the augmentation policy. The above minimization is difficult to solve, and thus we relax it as detailed next.

TSAA overview. Our approach, which we call time-series automatic augmentation (TSAA), consists of two main steps, as illustrated in Fig. 2 and summarized in Alg. 1 in 4. In the first step, we partially train the model for a few epochs and construct a set of shared weights. The second step iterates between solving Eq. equation 3 in search of an augmentation policy using TPE and EI to solving Eq. equation 4 with fine-tuning and ASHA for an optimal model. A complexity analysis is given in App. D.

Step 1: compute shared weights. Solving Eq. equation 4 iteratively requires repeated trainings of the deep model, which is computationally prohibitive. To reduce these costs, we propose to partially train the baseline model and generate a shared set of weights ω_{share}. Doing so, Step 2 is reduced to an iterative process of fine-tuning models for a small number of epochs, where ω_{share} are shared across all augmentations policies. Beyond efficiency aspects, applying DA in the later stages of training is assumed to be more influential (Tian et al., 2020a). In practice, we partially train for $\lfloor \beta K \rfloor$ epochs, where $\beta = 0.5$ is a hyperparameter and K is the *active* number of train epochs. In our tests, $K \leq 10$, and it may be strictly less due to an early stopping scheduler. K is found by training the baseline model with no augmentation to completion and saving the weights after every epoch. Then, we define

$$\omega_{\text{share}} := \omega(\lfloor \beta K \rfloor) \ , \quad R := K - \lfloor \beta K \rfloor \ ,$$

where R is the maximum resource parameter, and $r = 1$ is the minimum resource, see Sec. 3.

Step 2: iterative split optimization. Given ω_{share}, it remains to solve Eqs. equation 3 and equation 4 to find the best augmentation policy θ^* and final weights ω^*. In TSAA, we propose to split this problem to an iterative process, where we alternate between exploring augmentation policies θ via Eq. equation 3 to exploiting the current policy and produce model weights ω via Eq. equation 4. Namely, for a fixed set of weights ω, the upper minimization finds the next policy θ to try by evaluating the validation set. Then, we fine-tune the model using a fixed θ with early stopping for a maximum of R epochs to produce the next ω. This procedure is repeated until a predefined number of trials $T_{\max}$ is reached. The k best-performing policies define p_{θ^*} from which θ^* is sampled, where we only allow policies that improve the baseline validation loss. Finally, we fine-tune the model again to obtain ω^*.

Solving Eq. equation 3. Existing work solved the upper problem using reinforcement learning (Cubuk et al., 2019; Tian et al., 2020a), grid search (Cubuk et al., 2020; Fons et al., 2021), and one-pass optimization (Li et al., 2020b; Zheng et al., 2022). Inspired by (Lim et al., 2019), we propose to use Tree-structured Parzen Estimator (TPE) with Expected Improvement (EI), see Sec. 3. In the context of TSAA, the parameters x in Eq. equation 1 represent the policy θ and f is $\mathcal{L}_{\text{val}}$. The Bayesian optimization is conducted over the policy search space and time-series augmentations we describe below.

Policy search space. The augmentation policies θ we consider are drawn from a distribution p_θ over k sub-policies $\Theta = \{\theta_1, \ldots, \theta_k\}$, i.e.,

$$\theta \sim p_\theta := \{p(\theta_j) | \theta_j \in \Theta\} \ . \tag{5}$$

Each sub-policy θ_j is composed of n transformations $T_{j,i}$, applied sequentially on the output data x_{i-1} of the previous transformation with x_0 being the input data and $m_{j,i}$ being the magnitude of the transformation. That is,

$$\theta_j = T_{j,n}(x_{n-1}, m_{j,n}) \circ \cdots \circ T_{j,1}(x_0, m_{j,1}) \ . \tag{6}$$

Time-series data augmentations. While natural images are invariant to geometric transformations as translation and rotation, arbitrary time-series data need not be invariant to a certain type of transformations. Moreover, capturing the invariance in regression problems such as TSF may be more challenging than in classification tasks including images. Finally, time-series data may include slow and fast phenomena such as bursts of electricity usage and seasonal peaks, for which some DA may be inapplicable. Thus, we propose to exploit DA that manipulate some features of the data and leave some features unchanged. For example, adjusting the trend while keeping the seasonality and noise components unaffected, or diversifying the time intervals in a way that the series mean and variance still stay the same. In particular, we suggest the following time-series transformations: identity, jittering, trend scaling, seasonality scaling, scaling, smoothing, noise scaling, flip, permutation, reverse, dynamic-time-stretching (DTS), window warping, and mixup. The magnitude of the augmentations can be controlled using a single parameter. The transformations are further elaborated in App. B and Tab. 4 in the appendix.

Solving Eq. equation 4. Finally, solving the bottom minimization may be achieved in a straightforward fashion via fine-tuning. However, as motivated in Sec. 4, doing so iteratively is costly. To prune runs, we augment our approach with Asynchronous Successive Halving (ASHA). Our choice to use ASHA over other techniques such as Bayesian Optimization HyperBand (BOHB) (Falkner et al., 2018) is motivated by the following reasons. First, BOHB has shown to be slightly inferior to ASHA (Li et al., 2020a). Second, In our setting $R \in \{1, 2, .., 5\}$ and η is set to be more aggresive. As a result, only two SHA brackets at most can be exploited in the HyperBand, thus limiting its effectiveness.

Algorithm 1 Time-Series AutoAugment (TSAA)

Inputs: partial train factor β, resources R, r, max trials $T_{\max}$, reduction factor η, and k best DA sub-policies

$\Lambda \leftarrow \emptyset$
$\omega_{\text{share}}, R \leftarrow$ partial solve Eq. equation 4 with β
for $i = 1$ **to** $T_{\max}$ **do**
  $\theta_i \leftarrow$ solve Eq. equation 3 with $\text{TPE}(\Theta, \omega_{i-1})$
  $w_i \leftarrow$ fine-tune Eq. equation 4 with ω_{share} and $\text{ASHA}(r, R, \eta)$
  $\Lambda \leftarrow \Lambda \cup \left\{[\theta_i,\ \mathcal{L}_{\text{val}}(\omega_i, \theta_i)]\right\}$
end for
$p_{\theta^*} \leftarrow k$ best sub-policies θ_i from Λ
$\omega^* \leftarrow$ fine-tune $\mathcal{L}_{\text{tr}}(\theta^* \sim p_{\theta^*})$
return $p_{\theta^*}, \theta^*, \omega^*$

5 Results

In what follows, we provide a comprehensive overview of our experimental setup, including models, datasets, and implementation details followed by evaluations of our approach. In the supplementary material, we offer additional information on hyperparameters (App. C), and extended results (App. E.1).

5.1 Models and datasets

We extensively evaluate the performance of our Time-Series AutoAugment (TSAA) framework. To this end, we selected some of the most recent prominent time-series forecasting models. We consider the baseline architectures: **N-BEATS** (Oreshkin et al., 2020), a deep neural architecture based on backward and forward residual links and a very deep stack of fully-connected layers. **Informer** (Zhou et al., 2021) adapts the Transformer (Vaswani et al., 2017) architecture to time-series forecasting tasks, with a new attention mechanism. **Autoformer** (Wu et al., 2021) exchanges the self-attention module for an auto-correlation mechanism and introduces time-series decomposition as part of the model's encoding. Finally, **FEDformer** (Zhou et al., 2022) enables capturing more important details in time-series through frequency domain mapping.

For each of the given baseline models, we apply TSAA on six commonly-used datasets in the literature of long-term time-series forecasting: (1) **ETTm2** (Zhou et al., 2021) contains electricity transformer oil temperature data alongside 6 power load features. (2) **Electricity** (Zhou et al., 2021) is a collection of hourly electricity consumption data over the span of 2 years. (3) **Exchange** (Lai et al., 2018) consists of 17 years of daily foreign exchange rate records representing different currency pairs. (4) **Traffic** (Zhou et al., 2021) is an hourly reported sensor data containing information about road occupancy rates. (5) **Weather** (Zhou et al., 2021) contains 21 different meteorological measurements, recorded every 10 minutes for an entire year. (6) **ILI** (Wu et al., 2021) includes weekly recordings of influenza-like illness patients.

We summarize in Tab.5.1 the different datasets and their attributes such as their sampling *frequency*, *variates* which determine the number of channels in each example, the total number of *timesteps* in each dataset, the different *horizon* lengths used for forecasting, and lastly the *lookback* period which is the input length used for the prediction.

5.2 Implementation details

Baselines. We train all models based on the implementation and architecture details as they appear in (Oreshkin et al., 2020) for N-BEATS and (Zhou et al., 2021; Wu et al., 2021; Zhou et al., 2022) for the Transformer-based models. The model weights are optimized with respect to the mean squared error (MSE) using the ADAM optimizer (Kingma & Ba, 2015) with an initial learning rate of 10^{-3} for N-BEATS and 10^{-4} for Transformer-based models. The maximum number of epochs is set to 10 allowing early-stopping with a patience parameter of 3. The reported baseline results are obtained using our environment and hardware,

Dataset Summary					
dataset	frequency	variates	total timesteps	horizon	lookback period
ETTm2	15 minutes	7	69,680	96, 192, 336, 720	96
Electricity	hourly	321	26,304	96, 192, 336, 720	96
Exchange	daily	8	7,588	96, 192, 336, 720	96
Traffic	hourly	862	17,544	96, 192, 336, 720	96
Weather	10 minutes	21	52,696	96, 192, 336, 720	96
ILI	weekly	7	966	24, 36, 48, 60	36

and they may slightly differ from the reported values for the respective methods. Every experiment is run on three different seed numbers, and the results are averaged over the runs. The Pytorch library (Paszke et al., 2019) is used for all model implementations, and executed with NVIDIA GeForce RTX 3090 24GB.

Table 1: Multivariate long-term time-series forecasting results on six datasets in comparison to five baseline models. Low MSE and MAE values are better, and high relative improvement MSE% and MAE% scores are better. Boldface text highlights the best performing models.

		Informer		Autoformer		FEDformer-w		FEDformer-f		TSAA			
		MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE↓	MAE↓	MSE%↑	MAE%↑
ETTm2	96	0.545	0.588	0.231	0.310	0.205	0.290	0.189	0.282	**0.187**	**0.274**	**1.058**	**2.837**
	192	1.054	0.808	0.289	0.346	0.270	0.329	0.258	0.326	**0.255**	**0.314**	**1.163**	**3.681**
	336	1.523	0.948	0.341	0.375	0.328	0.364	0.323	0.363	**0.304**	**0.350**	**5.882**	**3.581**
	720	3.878	1.474	0.444	0.434	0.433	0.425	0.425	0.421	**0.398**	**0.403**	**6.353**	**4.276**
Electricity	96	0.336	0.416	0.200	0.316	0.196	0.310	0.185	0.300	**0.183**	**0.297**	**1.081**	**1.000**
	192	0.360	0.441	0.217	0.326	0.199	0.310	0.201	0.316	**0.195**	**0.309**	**2.010**	**0.323**
	336	0.356	0.439	0.258	0.356	0.217	0.334	0.214	0.329	**0.208**	**0.323**	**2.804**	**1.824**
	720	0.386	0.452	0.261	0.363	0.248	0.357	0.246	0.353	**0.238**	**0.348**	**3.252**	**1.416**
Exchange	96	1.029	0.809	0.150	0.281	0.151	0.282	**0.142**	**0.271**	0.143	0.272	-0.704	-0.369
	192	1.155	0.867	0.318	0.409	0.284	0.391	0.278	0.383	**0.270**	**0.378**	**2.878**	**1.305**
	336	1.589	1.011	0.713	0.616	**0.442**	**0.493**	0.450	0.497	0.459	0.504	-3.846	-2.231
	720	3.011	1.431	1.246	0.872	1.227	0.868	**1.181**	**0.841**	1.213	0.842	-2.710	-0.119
Traffic	96	0.744	0.420	0.615	0.384	0.584	0.368	0.577	0.361	**0.565**	**0.352**	**2.080**	**2.493**
	192	0.753	0.426	0.670	0.421	0.596	0.375	0.610	0.379	**0.571**	**0.351**	**4.195**	**6.400**
	336	0.876	0.495	0.635	0.392	0.590	0.365	0.623	0.385	**0.584**	**0.359**	**1.017**	**1.644**
	720	1.011	0.578	0.658	0.402	0.613	0.375	0.632	0.388	**0.607**	**0.368**	**0.979**	**1.867**
Weather	96	0.315	0.382	0.259	0.332	0.269	0.347	0.236	0.316	**0.180**	**0.256**	**23.729**	**18.987**
	192	0.428	0.449	0.298	0.356	0.357	0.412	0.273	0.333	**0.252**	**0.311**	**7.692**	**6.607**
	336	0.620	0.554	0.357	0.394	0.422	0.456	0.332	0.371	**0.296**	**0.355**	**10.843**	**4.313**
	720	0.975	0.722	0.422	0.431	0.629	0.570	0.408	0.418	**0.382**	**0.395**	**6.373**	**5.502**
ILI	24	5.349	1.582	3.549	1.305	**2.752**	1.125	3.268	1.257	2.760	**1.123**	-0.291	**0.178**
	36	5.203	1.572	2.834	1.094	**2.318**	**0.980**	2.648	1.068	2.362	0.984	-1.898	-0.408
	48	5.286	1.594	2.889	1.122	2.328	1.006	2.615	1.072	**2.264**	**0.988**	**2.749**	**1.789**
	60	5.419	1.620	2.818	1.118	2.574	1.081	2.866	1.158	**2.520**	**1.062**	**2.098**	**1.758**

Method. We use Optuna (Akiba et al., 2019) for the implementations of TPE and ASHA. The number of trials $T_{\max}$ is set to 100. For TPE, In order to guarantee aggressive exploration at the beginning, we run the first 30% of trials with random search. For ASHA, r and η are set globally to 1 and 3 respectively. The maximum resource parameter R, representing the epochs, is set differently for each experiment, due to the baseline's early-stopping.

After the augmentation policy search is finalized, a maximum of k best policies are selected to obtain p_{θ^*} , where $k = 3$, and the final model is *fine-tuned* with $\theta^* \sim p_{\theta^*}$ using the shared weights ω_{share}. We opt to fine-tune the model and not re-train from random weights so that the final model training matches our optimization process as close as possible. Indeed, Cubuk et al. (Cubuk et al., 2020) discuss the potential differences between the final model behavior in comparison to the performance of the intermediate proxy tasks, i.e., the models obtained during optimization. As the similarity in performance between these models and the final model is not guaranteed, a natural choice is to similarly train the proxy tasks and the final model, as we propose.

Table 2: Univariate long-term time-series forecasting results on five datasets in comparison to five baseline models. Low MSE and MAE values are better, and high relative improvement MSE% and MAE% scores are better. Boldface text highlights the best performing models.

		Informer		Autoformer		FEDformer-f		N-BEATS-I		N-BEATS-G		TSAA			
		MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE	MSE↓	MAE↓	MSE%↑	MAE%↑
ETTm2	96	0.085	0.225	0.123	0.270	**0.068**	0.198	0.080	0.213	0.080	0.210	**0.068**	**0.192**	**0.000**	**3.030**
	192	0.130	0.282	0.141	0.289	**0.096**	0.238	0.103	0.240	0.110	0.250	**0.096**	**0.237**	**0.000**	**0.420**
	336	0.161	0.314	0.170	0.319	**0.138**	**0.286**	0.162	0.312	0.172	0.320	0.139	0.290	-0.725	-1.399
	720	0.221	0.373	0.206	0.353	0.189	**0.335**	0.199	0.347	0.201	0.353	**0.187**	0.336	**1.058**	-0.299
Electricity	96	0.261	0.367	0.454	0.508	**0.244**	0.364	0.326	0.402	0.324	0.397	**0.244**	**0.354**	**0.000**	**2.747**
	192	0.285	0.386	0.511	0.532	**0.276**	0.382	0.350	0.417	0.363	0.420	0.277	**0.368**	-0.362	**3.665**
	336	0.324	0.417	0.739	0.651	0.347	0.432	0.393	0.440	0.392	0.443	**0.310**	**0.394**	**4.321**	**5.516**
	720	0.632	0.612	0.673	0.610	0.408	0.473	0.458	0.490	0.489	0.502	**0.378**	**0.447**	**7.353**	**5.497**
Exchange	96	0.490	0.554	0.149	0.308	0.133	0.284	0.210	0.344	0.223	0.351	**0.093**	**0.236**	**30.075**	**16.901**
	192	0.790	0.721	0.290	0.415	0.292	0.419	1.130	0.840	0.783	0.675	**0.215**	**0.352**	**25.862**	**15.181**
	336	2.146	1.223	0.708	0.662	**0.477**	**0.532**	1.587	1.047	2.622	1.266	0.532	0.572	-11.530	-7.519
	720	1.447	1.008	1.324	0.892	1.304	0.882	0.870	0.747	2.588	1.303	**0.527**	**0.594**	**39.425**	**20.482**
Traffic	96	0.262	0.348	0.266	0.372	0.210	0.318	0.181	0.268	0.159	0.240	**0.158**	**0.239**	**0.629**	**0.417**
	192	0.294	0.376	0.272	0.379	0.206	0.311	0.177	0.263	0.181	0.264	**0.160**	**0.243**	**9.605**	**7.605**
	336	0.308	0.390	0.261	0.374	0.217	0.322	0.180	0.271	**0.155**	**0.239**	0.156	0.244	-0.645	-2.092
	720	0.364	0.440	0.269	0.372	0.243	0.342	0.226	0.316	0.212	0.304	**0.189**	**0.279**	**10.849**	**8.224**
Weather	96	0.005	0.048	0.009	0.078	0.009	0.073	0.003	0.044	0.003	0.043	**0.001**	**0.024**	**66.667**	**44.186**
	192	0.004	0.051	0.009	0.068	0.007	0.067	0.004	0.046	0.004	0.047	**0.001**	**0.027**	**75.000**	**41.304**
	336	0.003	0.043	0.006	0.058	0.006	0.062	0.004	0.048	0.005	0.054	**0.002**	**0.035**	**33.333**	**18.605**
	720	0.004	0.049	0.007	0.063	0.006	0.060	0.004	0.049	0.004	0.048	**0.002**	**0.034**	**50.000**	**29.167**

Augmentations. Each transformation includes a different increasing or decreasing magnitude range which are all mapped to the range $[0, 1]$. This way, $m = 0$ implies the identity and $m = 1$ is the maximum scale. To eliminate cases of the identity being repeatedly chosen, we replace the lower bound in the range with an $\epsilon > 0$ such that for all transformations in the search space only $m > 0$ is possible. The transformations *Trend scale* and *Seasonality scale* require computing the seasonality and trend components; we pre-compute these factors using the decomposition in STL (Cleveland et al., 1990) and treat it as part of the input data. Each augmentation is applied before the input is fed to the model, namely, on the input x and the target y of the train data batches.

5.3 Main results

In our experiments, we employ a similar setup to (Wu et al., 2021; Zhou et al., 2022), where the input length is 96 and the evaluated forecast horizon corresponds to $96, 192, 336$, or 720. For ILI, we use input length 36 and horizons $24, 36, 48, 60$. For a fair comparison, we re-produce all baseline results on our system, and the augmentations are applied on the same generated batches as the baseline. Our main results are summarized in Tab. 1 and Tab. 2 including all the baseline results and TSAA. For TSAA, we include the best performing model trained on all baseline architectures. The full results for every architecture with and without TSAA are provided in the appendix spanning tables 6-14. We detail the mean absolute error (MAE) and mean squared error (MSE) (Oreshkin et al., 2020). Lower values are better, and boldface text highlights the best performing model for each dataset and metric. For TSAA, we also include the *relative improvement* percentage, i.e., $100 \cdot (e_b - e_n)/e_b$, where e_b is the best baseline error and e_n is our result. We denote by MSE% and MAE% the relative improvement of MSE and MAE, respectively. A higher improvement is better.

Multivariate time-series forecasting results. Based on the results in Tab. 1, we observe that most datasets benefit from automatic augmentation, where in the vast majority of cases, TSAA improves the baseline scores. It is apparent that TSAA yields stronger performance in particular in the long-horizon settings with **6.35%** (0.425 → 0.398) reduction in ETTm2, **3.25%** (0.246 → 0.238) reduction in Electricity, and **2.1%** (2.328 → 2.264) reduction in ILI. One of the more prominent results appears for Weather 96 and 336 with reductions in MSE of **23.73%** (0.236 → 0.180) and **10.84%** (0.332 → 0.296), respectively. For the Exchange dataset, TSAA obtains slightly higher errors with respect to the FEDformer-w baseline. Overall,

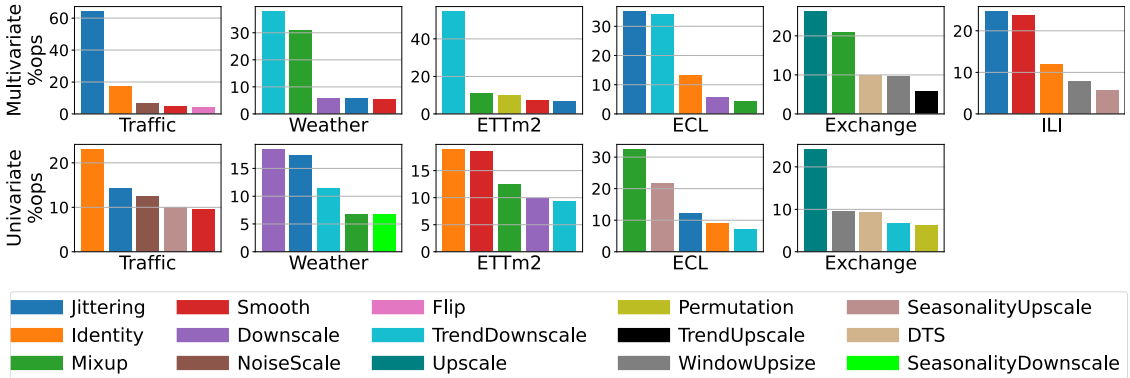

Figure 3: The best five performing transformations per dataset attained with TSAA, measured with the percentage proportion of the selected operations (%ops). Each colored bar represents a transformation and the y-axis represents the percentage proportion the given transformation accounts for.

TSAA achieves the *best results* in 39 error metrics, in comparison to FEDformer-f and FEDformer-w with 4 and 5 best models, respectively.

Univariate time-series forecasting results. Similar to the multivariate results, most long horizon settings benefit from TSAA. With a 21.74% average reduction across all datasets with a horizon of 720. Furthermore, the results that stand out the most are the MSE and MAE reductions in Weather, with a $66\%, 75\%, 33, 50\%\%$, and respectively $44.2\%, 41.3\%, 17.6\%, 29.2\%$ performance improvements corresponding to the $96, 192, 336$,and 720 horizons. Further, it is evident in Tabs. 10-14, that the improvements in the Weather dataset are not limited to a specific baseline architecture. In contrast to the multivariate setting, TSAA achieves significantly better scores on the Exchange dataset with average improvements of 21% and 11.27% for the MSE and MAE metrics. Notably, the results in the univariate case are slightly more involved than the multivariate setting such that that only Weather always benefits from TSAA, whereas the results for other datasets are mixed. Still, TSAA shows a positive advantage over all baseline models. In particular, TSAA obtained the best models for 32 error metrics, whereas FEDformer-f and N-BEATS-G are better in 9 and 2 measures.

Policy analysis. The most noticeable selected transformations are illustrated in Fig. 3. It is evident that the transformations Trend Downscale, Jittering, Mixup, and Smoothing are some of the prominent selections in the overall setup. Trend Downscale accounts for more than 30% of the operations in ETTm2, Weather and Electricity; this may indicate that the deep models tend to overestimate the trend, and thus it requires downscaling. Jittering and Smoothing on the other hand, do not violate time-series characteristics such as trend or seasonality but still promote diversity within the given dataset, where Smoothing is approximately the opposite of Jittering. Notably, Mixup appeared as one of the five most important transformations for four and three datasets in the multivariate and univariate settings, respectively. We believe that Mixup is beneficial to TSF since it samples from a vicinal distribution whose variability is higher than the original train set. We show in Fig. 5 the outcome with and without TSAA compared to the ground truth, showing that employing custom policies per signal may significantly improve forecasting.

6 Ablation and Analysis

6.1 Parameter selection

Choice of β. In what follows, we motivate our choice for the β hyperparameter which dictates for how many epochs we pre-train the baseline architecture to obtain ω_{share}. To this end, we investigate the effect of utilizing different values of β. We consider four different settings: 1) full training with augmentation, i.e., $\beta = 0.0$, 2) half training with augmentation, i.e., $\beta = 0.5$, 3) augmentation applied only in the last

epoch, 4) baseline training with no augmentation, i.e., $\beta = 1.0$. We used TSAA on the ILI with respect to N-BEATS-G in the univariate setting, and Informer, Autoformer and FEDformer-f in the multivariate case, as well as on multivariate ETTm2 with Autoformer and FEDformer-f. We plot the averaged results of these architectures in Fig. 4A, showing four colored curves corresponding to the various forecasting horizons 24/96, 36/192, 48/336 and 60/720 with colors blue, orange, green and red, respectively. The best models are obtained for $\beta = 0.0$ and $\beta = 0.5$, that is, full- and half-augmented training. Somewhat surprisingly, two of the four best forecasting horizons (36/192, 48/336) are obtained for $\beta = 0.5$. Overall, the fully augmented model (i.e., $\beta = 1.0$) attains a **5.1%** average improvement over the baseline, whereas using $\beta = 0.5$ yields a **5.3%** average improvement. Thus, fully training with augmentation achieves similar performance to half training, while requiring significantly more resources. Indeed, Tian et al. (2020a) employs a similar strategy, and thus, we propose to generate ω_{share} after training for *half* of the active epochs, and we fine-tune the model using optimal augmentation policies.

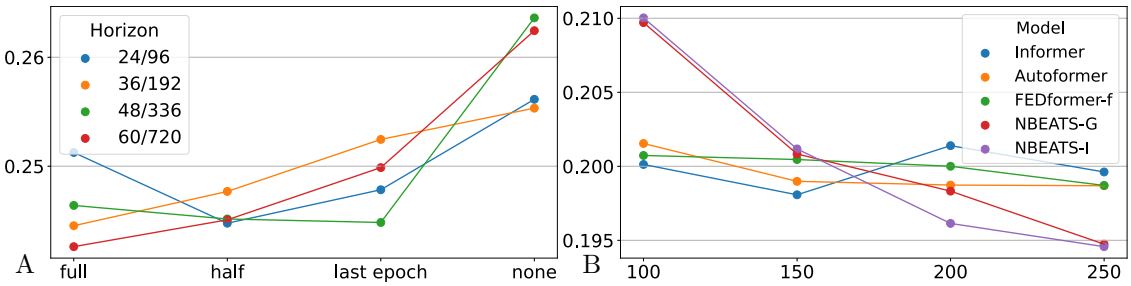

Figure 4: A) The normalized average performance measures as a function of different β values. Our results indicate that $\beta = 0.5$ (half) attains the best computational resources to performance gain ratio. B) We plot the normalized average performance measures as a function of different $T_{\max}$ values. As the number of trials grows, we observe better overall performance.

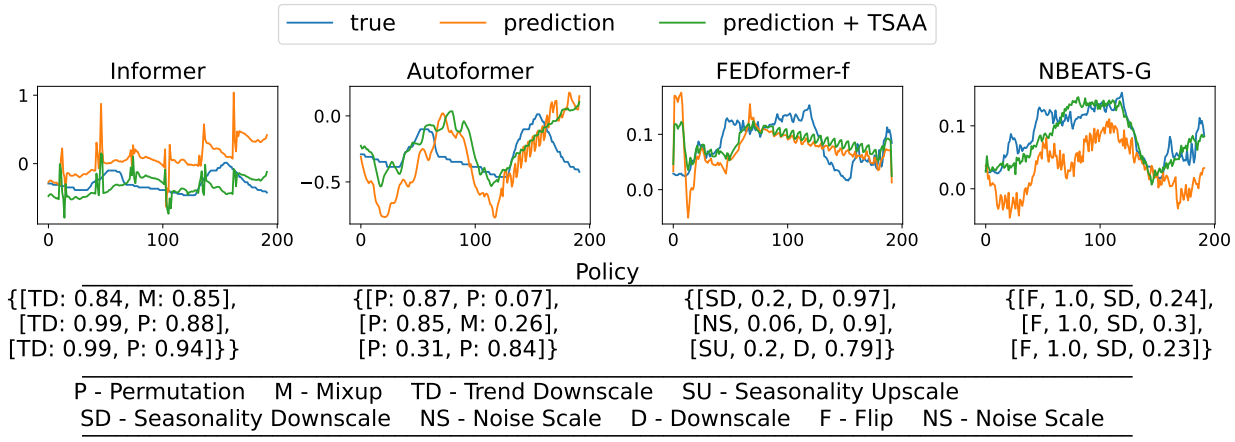

Figure 5: The ground truth, prediction, and prediction with augmentation attained with TSAA applied to the same forecast target in ETTm2 with Informer, Autoformer multivariate, and Weather with FEDformer-f and NBEATS-G univariate. It is shown that augmentation can assist the different models to achieve more accurate predictions. The attained policies are given underneath each plot.

Reduction factor and linked operations. In Sec. 3, we introduced the reduction factor η that controls the number of kept runs in ASHA. Additionally, we discuss in Sec. 4 that every sub-policy is composed of n linked operations of time-series augmentations. Here, we would like to empirically justify our choices for these two hyperparameters. Our ablation study uses the ILI dataset on the $36, 48, 60$ forecasting tasks, with N-BEATS-G for the univariate case, and Informer, Autoformer, and FEDformer-f for the multivariate

configuration. We test the values $\eta \in \{2, 3\}$ and $n \in \{1, 2\}$. Every experiment is repeated three times, and we analyze the average results.

Overall, we propose to use the values $\eta = 3$ and $n = 2$ due to the following observations arising from our experiments. The improvement difference between $\eta = 2$ and $\eta = 3$ is only **0.12%** in favor of $\eta = 2$, thus suggesting that neither exhibits a statistically-dominant performance advantage. Nevertheless, $\eta = 3$ is resource efficient as it reduces the amount of kept runs $1/\eta$ by 16.67%. Moreover, a single operation $n = 1$ attains a **6.4%** average improvement compared to the baseline, whereas two linked operations $n = 2$ yield a **7.4%** average improvement.

Convergence of TSAA. In our experiments, we look for good augmentation policies for $T_{\max} = 100$ iterations. Here, we explore the effect of this value on the performance of the resulting models. We evaluate our framework on the ILI dataset with the architectures Informer, Autoformer, FEDformer-f, N-BEATS-G and N-BEATS-I using varying values for $T_{\max} \in \{100, 150, 200, 250\}$. Intuitively, greater $T_{\max}$ values may result in an improved convergence and a better overall performance as the framework can explore and exploit a larger variety of configurations from the search space. Indeed, we show in Fig. 4B the normalized average MSE values obtained for the various tests. We observe an MSE reduction of **1%** for the transformer-based models when increasing $T_{\max} = 100$ to $T_{\max} = 250$. The N-BEATS architecture benefited more and achieved a **7.25%** reduction. In conclusion, the hyperparameter $T_{\max}$ presents a natural trade-off to the practitioner: higher $T_{\max}$ values generally lead to better performance at a higher computational cost, whereas lower values are less demanding computationally but present inferior performance.

Table 3: Comparison of automatic augmentation approaches including TSAA, Fast AutoAugment and RandAugment. We denote by %AI the average improvement in percentage.

		Best Baseline		Fast AA		RandAugment		TSAA	
	Metric	MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE
ETTm2	96	0.189	0.282	0.197	0.279	0.192	0.282	**0.187**	**0.274**
	192	0.258	0.326	0.262	0.319	0.257	0.323	**0.255**	**0.314**
	336	0.323	0.363	0.322	0.356	0.326	0.364	**0.311**	**0.350**
	720	0.425	0.421	0.415	0.407	0.427	0.420	**0.406**	**0.403**
Traffic	96	**0.577**	**0.361**	0.655	0.410	0.590	0.376	**0.577**	0.362
	192	0.610	0.379	0.652	0.408	0.622	0.390	**0.601**	**0.371**
	336	0.623	0.385	0.674	0.421	0.626	0.392	**0.619**	**0.383**
	720	**0.632**	**0.388**	0.705	0.427	0.643	0.396	**0.632**	**0.388**
Weather	96	0.236	0.316	**0.191**	**0.252**	0.203	0.275	0.207	0.285
	192	0.273	0.333	**0.240**	**0.290**	0.267	0.332	0.252	0.311
	336	0.332	0.371	**0.290**	**0.321**	0.328	0.364	0.313	0.355
	720	0.408	0.418	**0.363**	**0.367**	0.398	0.413	0.382	0.395
ILI	24	3.268	1.257	4.671	1.603	3.160	1.234	**3.150**	**1.219**
	36	2.648	1.068	3.835	1.375	**2.457**	**1.019**	2.578	1.049
	48	2.615	1.072	3.694	1.359	**2.558**	**1.045**	2.609	1.069
	60	2.866	1.158	3.855	1.410	**2.775**	**1.108**	2.805	1.140
%AI		0.0	0.0	-9.5	-4.88	1.67	1.22	**3.33**	**3.1**

6.2 AutoAugment Method Comparison

We compare TSAA to other efficient AutoAugment methods via an experiment that shows that both Fast AutoAugment (Lim et al., 2019) and RandAugment (Cubuk et al., 2020) are *inconsistent* and thus inferior to TSAA. In this experiment, we tested the performance of deploying Fast AutoAugment and RandAugment with the same search space, with the exception of discretized magnitude ranges so RandAugment falls in line with the original method. The given methods were tested on Autoformer and FEDformer-f multivariate together with datasets: ETTm2, Traffic, Weather, and ILI. The results are provided in Tab. 3. For Fast AutoAugment we set $K = 3$ folds which control the number of subsets, each subset explores and exploits 100 augmentation trials. For RandAugment, we discretize the magnitude range to 8 bins and utilize the partial train scheme with the same β as in TSAA, to allow RandAugment to benefit from the same approach. While it is shown

that Fast AutoAugment and RandAugment are superior on Weather and ILI respectively, they attain inferior results on the other datasets. Nevertheless, TSAA is shown to be most effective on Traffic and ETTm2 and second-best on ILI and Weather. Additionally, TSAA maintains a consistent improvement across all datasets providing a 3.33% average MSE reduction as opposed to RandAugment which offers approximately half of that, or Fast AutoAugment with a negative average MSE reduction. In conclusion, TSAA is more consistent with better overall performance when compared to prominent AutoAugment methods in the time-series domain.

7 Discussion

In this work, we study the task of data augmentation in the setting of time-series forecasting. While recent approaches based on automatic augmentation achieved state-of-the-art results in image classification tasks, problems involving arbitrary time-series information received less attention. Thus, we propose a novel time-series automatic augmentation (TSAA) method that relaxes a difficult bilevel optimization. In practice, our framework performs a partial training of the baseline architecture, followed by an iterative split process. Our iterations alternate between finding the best DA policy for a given set of model weights, to fine-tuning the model based on a specific policy. In comparison to several strong methods on multiple univariate and multivariate benchmarks, our framework improves the baseline results in the majority of prediction settings.

In the future, we would like to explore better ways for relaxing the bilevel optimization, allowing to train an end-to-end model (Li et al., 2020b; Zheng et al., 2022). Further, we believe that our approach would benefit from stronger time-series augmentation transformations. Thus, one possible direction forward is to incorporate learnable DA modules, similar in spirit to filters of convolutional models.

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A Appendix

In what follows, we present additional details the transformations used in our method (App. B), hyperparameter values (App. C), complexity analysis of TSAA (App. D), and lastly, we provide extended result tables for every baseline alongside TSAA (App. E.1).

B Time-series transformations

In this section, we offer a detailed description of the different time-series transformations, which can be found in Tab. 4 and depicted in Fig. 6 with $m = 0.85$ compared to the original signal. For each of the transformations *Trend scale*, *Scale*, *Seasonality scale*, *Window warping*, we use two separate and independent transformations to demonstrate an increase or decrease of the given effect.

Table 4: Our search space is composed of the following time-series transformations and their associated magnitude range.

Transformation	Description	Range of magnitudes
Jittering	Adds white noise with σ controlled by m (Um et al., 2017). *	[0,0.1]
Trend scale	Multiplies the trend component by m. *	[1,10], [0,1]
Scale	Multiplies the entire series by m (Um et al., 2017).	[1,3], [0.3,1]
Seasonality scale	Multiplies the seasonality component by m.	[1,3], [0,1]
Smooth	Performs low-pass filtering with a convolution kernel, where m controls the kernel size.	[0,11]
Noise scale	Performs high-pass filtering with a second-order convolution kernel to extract the difference, which is then multiplied by m and added back to the original series.	[0,1]
Permutation	Exchanges two non-overlapping time intervals, such that the interval size is controlled by m. (Um et al., 2017).	[0,0.3]
Dynamic time stretching	Manipulates the length of different non-overlapping time intervals, where m controls the manipulation magnitude. (Nguyen et al., 2020).	[1,5]
Window warping	Manipulates the length of the entire window (Um et al., 2017).	[1,1.5], [0.5,1]
Mixup	Linearly interpolates between two series, m controls the contribution of each series (Zhang et al., 2018).	[0,0.5]
Identity	Returns the original series.	None
Flip	Flip the series relative to the value location by multiplying by (-1) (Iwana & Uchida, 2021). *	{0,1}
Reverse	Change the relative location of the time steps to span from end to start.	{0,1}

* marks a transformation implemented with min-max scaling to ensure equal relative changes.

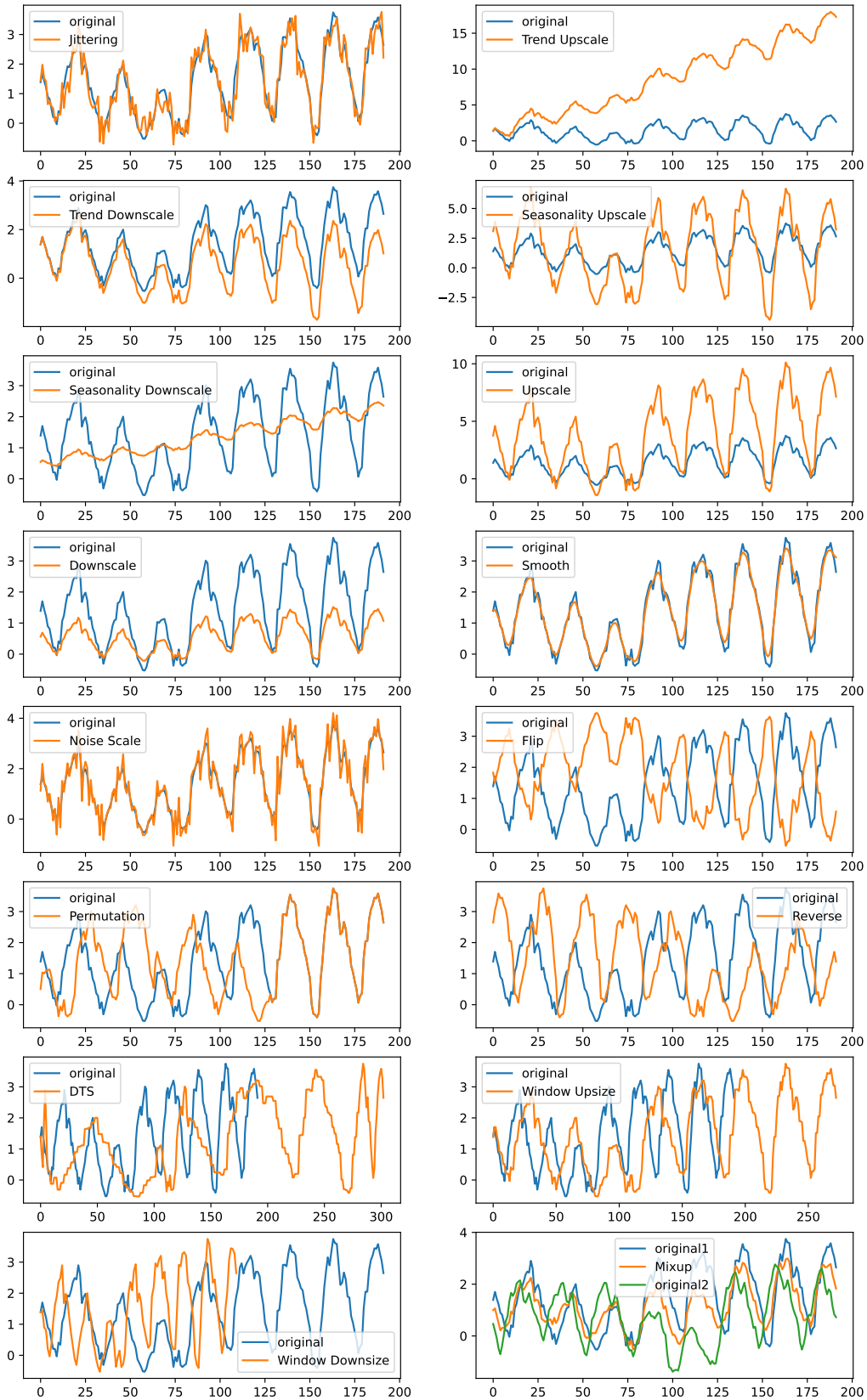

Figure 6: We demonstrate the effect of different transformations when applied to the same example from the Electricity dataset. Blue and orange represent the original signal and its transformed version, respectively.

C TSAA hyperparameters

We detail in Tab. 5 the hyperparameter values we used in the evaluation of TSAA.

Table 5: Hyperparameter values used in the evaluation of TSAA.

Model Parameters - TSAA								
T_{max}	exploration trials fraction	m range	n	η	r	resource type	β	k
100	0.3	(0,1]	2	3	1	epoch	0.5	3

D Complexity

A straightforward upper bound of our method is given by $\mathcal{O}((1-\beta)KT_{max})$ evaluated in epochs, where K, $(1-\beta)$, and T_{max} correspond to the number of active epochs the model trains for, the fraction of K to be used for fine-tuning, and the maximum number of trials, respectively. However, for TSAA to practically reach such an upper bound when $K > 2$ would require each trial to outperform the preceding trials, thus avoiding being pruned by ASHA. This setup is very unlikely for the following reasons: (1) a fraction size 0.3 of T_{max} of starting trials are manually dedicated to random search to promote aggressive exploration at the start. (2) To the best of our knowledge Bayesian Optimization does not guarantee monotonic improvement and inherently promotes exploration (Bergstra et al., 2011). (3) $\mathcal{L}_{\text{val}}(\theta, w^*)$ is not promised to be convex with respect to θ, making it even more difficult to attain a monotonic improvement. In our empirical evaluations, we have observed different operations with different transformations being selected, as opposed to a single policy being repeatedly selected, which strengthens our claim. Further, we would like to share a solid example from our empirical experiments with FEDformrer-w applied to Electricity with a horizon of 336. This setup is considered resource expensive as one epoch may take as long as 20 minutes on a single RTX3090. In the given setup, K was set to 8 and $\beta = 0.5$ as defined in the hyperparameter table Tab. 5. Therefore, according to the bound mentioned above, the total number of epochs would be 400 epochs. However, the use of ASHA with Bayesian optimization reduced it to 170, proving the computational impact. For comparison, applying a naive approach without ASHA and β will result in a total number of 800 training epochs.

E Extended results

In this section, we provide the performance of TSAA for each individual model featured in Tab. 1 and Tab. 2 in the main text. We can observe from the multivariate results that Informer benefits the most from TSAA, with the 720 horizon in particular. On the other end, TSAA struggles to achieve significant improvements in FEDformer-f, especially for the Exchange dataset. In the univariate setting, unlike the multivariate setting, the models NBEATS-G and NBEATS-I gain large improvement rates in Exchange thanks to TSAA. Overall, we can conclude that all models and datasets exhibit a degree of improvement with the support of TSAA.

E.1 TSF results

Tabs. 6, 7, 8, 9, 10, 11, 12, 13, 14 detail the extended results for every baseline architecture and dataset we considered in the main text.

Table 6: Informer multivariate

		Informer		TSAA			
		MSE	MAE	MSE↓	MAE↓	MSE%↑	MAE%↑
ETTm2	96	0.545	0.588	**0.224**	**0.321**	**58.899**	**45.408**
	192	1.054	0.808	**0.270**	**0.355**	**74.383**	**56.064**
	336	1.523	0.948	**0.304**	**0.374**	**80.039**	**60.549**
	720	3.878	1.474	**0.398**	**0.435**	**89.737**	**70.488**
Electricity	96	0.336	0.416	**0.324**	**0.407**	**3.571**	**2.163**
	192	0.360	0.441	**0.336**	**0.419**	**6.667**	**4.989**
	336	0.356	0.439	**0.347**	**0.429**	**2.528**	**2.278**
	720	0.386	0.452	**0.381**	**0.448**	**1.295**	**0.885**
Exchange	96	1.029	0.809	**0.512**	**0.569**	**50.243**	**29.666**
	192	1.155	0.867	**0.791**	**0.696**	**31.515**	**19.723**
	336	1.589	1.011	**1.040**	**0.763**	**34.550**	**24.530**
	720	3.011	1.431	**1.213**	**0.842**	**59.714**	**41.160**
Traffic	96	0.744	0.420	**0.723**	**0.408**	**2.823**	**2.857**
	192	0.753	0.426	**0.735**	**0.414**	**2.390**	**2.817**
	336	0.876	0.495	**0.811**	**0.462**	**7.420**	**6.667**
	720	1.011	0.578	**0.985**	**0.566**	**2.572**	**2.076**
Weather	96	0.315	0.382	**0.180**	**0.256**	**42.857**	**32.984**
	192	0.428	0.449	**0.253**	**0.331**	**40.888**	**26.281**
	336	0.620	0.554	**0.296**	**0.361**	**52.258**	**34.838**
	720	0.975	0.722	**0.392**	**0.426**	**59.795**	**40.997**
ILI	24	5.349	1.582	**5.313**	**1.559**	**0.673**	**1.454**
	36	**5.203**	**1.572**	5.260	1.581	-1.096	-0.573
	48	**5.286**	**1.594**	5.415	1.623	-2.440	-1.819
	60	5.419	1.620	**5.300**	**1.593**	**2.196**	**1.667**

Table 7: Autoformer multivariate

		Autoformer		TSAA			
		MSE	MAE	MSE↓	MAE↓	MSE%↑	MAE%↑
ETTm2	96	0.231	0.310	**0.211**	**0.293**	**8.658**	**5.484**
	192	0.289	0.346	**0.269**	**0.327**	**6.920**	**5.491**
	336	0.341	0.375	**0.322**	**0.359**	**5.572**	**4.267**
	720	0.444	0.434	**0.410**	**0.407**	**7.658**	**6.221**
Electricity	96	0.200	0.316	**0.188**	**0.302**	**6.000**	**4.430**
	192	**0.217**	**0.326**	0.221	0.328	-1.843	-0.613
	336	0.258	0.356	**0.252**	**0.352**	**2.326**	**1.124**
	720	0.261	0.363	**0.248**	**0.351**	**4.981**	**3.306**
Exchnage	96	0.150	0.281	**0.143**	**0.272**	**4.667**	**3.203**
	192	**0.318**	**0.409**	0.344	0.425	-8.176	-3.912
	336	**0.713**	**0.616**	0.742	0.641	-4.067	-4.058
	720	**1.246**	**0.872**	1.997	1.170	-60.273	-34.174
Traffic	96	0.615	0.384	**0.602**	**0.375**	**2.114**	**2.344**
	192	0.670	0.421	**0.663**	**0.416**	**1.045**	**1.188**
	336	0.635	0.392	**0.627**	**0.387**	**1.260**	**1.276**
	720	**0.658**	**0.402**	0.662	0.405	-0.608	-0.746
Weather	96	0.259	0.332	**0.216**	**0.292**	**16.602**	**12.048**
	192	0.298	0.356	**0.278**	**0.336**	**6.711**	**5.618**
	336	0.357	0.394	**0.341**	**0.381**	**4.482**	**3.299**
	720	0.422	0.431	**0.397**	**0.410**	**5.924**	**4.872**
ILI	24	**3.549**	1.305	3.565	**1.302**	-0.451	**0.230**
	36	2.834	1.094	**2.754**	**1.068**	**2.823**	**2.377**
	48	2.889	1.122	**2.856**	**1.114**	**1.142**	**0.713**
	60	**2.818**	**1.118**	2.826	**1.118**	-0.284	**0.000**

Table 8: FEDformer-f multivariate

		FEDformer-f		TSAA			
		MSE	MAE	MSE↓	MAE↓	MSE%↑	MAE%↑
ETTm2	96	0.189	0.282	**0.187**	**0.274**	**1.058**	**2.837**
	192	0.258	0.326	**0.255**	**0.314**	**1.163**	**3.681**
	336	0.323	0.363	**0.311**	**0.350**	**3.715**	**3.581**
	720	0.425	0.421	**0.406**	**0.403**	**4.471**	**4.276**
Electricity	96	**0.185**	**0.300**	**0.185**	**0.300**	**0.000**	**0.000**
	192	**0.201**	**0.316**	**0.201**	**0.316**	**0.000**	**0.000**
	336	**0.214**	**0.329**	**0.214**	**0.329**	**0.000**	**0.000**
	720	**0.246**	**0.353**	**0.246**	**0.353**	**0.000**	**0.000**
Exchange	96	**0.142**	**0.271**	0.149	0.277	-4.930	-2.214
	192	0.278	0.383	**0.273**	**0.380**	**1.799**	**0.783**
	336	**0.450**	**0.497**	0.517	0.540	-14.889	-8.652
	720	**1.181**	**0.841**	2.440	1.343	-106.605	-59.691
Traffic	96	**0.577**	**0.361**	**0.577**	0.362	**0.000**	-0.277
	192	0.610	0.379	**0.601**	**0.371**	**1.475**	**2.111**
	336	0.623	0.385	**0.619**	**0.383**	**0.642**	**0.519**
	720	**0.632**	**0.388**	**0.632**	**0.388**	**0.000**	**0.000**
Weather	96	0.236	0.316	**0.207**	**0.285**	**12.288**	**9.810**
	192	0.273	0.333	**0.252**	**0.311**	**7.692**	**6.607**
	336	0.332	0.371	**0.313**	**0.355**	**5.723**	**4.313**
	720	0.408	0.418	**0.382**	**0.395**	**6.373**	**5.502**
ILI	24	3.268	1.257	**3.150**	**1.219**	**3.611**	**3.023**
	36	2.648	1.068	**2.578**	**1.049**	**2.644**	**1.779**
	48	2.615	1.072	**2.609**	**1.069**	**0.229**	**0.280**
	60	2.866	1.158	**2.805**	**1.140**	**2.128**	**1.554**

Table 9: FEDformer-w multivariate

		FEDformer-w		TSAA			
		MSE	MAE	MSE↓	MAE↓	MSE%↑	MAE%↑
ETTm2	96	0.205	0.290	**0.199**	**0.280**	**2.927**	**3.448**
	192	0.270	0.329	**0.255**	**0.314**	**5.556**	**4.559**
	336	0.328	0.364	**0.316**	**0.352**	**3.659**	**3.297**
	720	0.433	0.425	**0.410**	**0.404**	**5.312**	**4.941**
Electricity	96	0.196	0.310	**0.183**	**0.297**	**6.633**	**4.194**
	192	0.199	0.310	**0.195**	**0.309**	**2.010**	**0.323**
	336	0.217	0.334	**0.208**	**0.323**	**4.147**	**3.293**
	720	0.248	0.357	**0.238**	**0.348**	**4.032**	**2.521**
Exchange	96	0.151	0.282	**0.144**	**0.272**	**4.636**	**3.546**
	192	0.284	0.391	**0.270**	**0.378**	**4.930**	**3.325**
	336	**0.442**	**0.493**	0.459	0.504	-3.846	-2.231
	720	**1.227**	**0.868**	1.952	1.167	-59.087	-34.447
Traffic	96	0.584	0.368	**0.565**	**0.352**	**3.253**	**4.348**
	192	0.596	0.375	**0.571**	**0.351**	**4.195**	**6.400**
	336	0.590	0.365	**0.584**	**0.359**	**1.017**	**1.644**
	720	0.613	0.375	**0.607**	**0.368**	**0.979**	**1.867**
Weather	96	0.269	0.347	**0.213**	**0.291**	**20.818**	**16.138**
	192	0.357	0.412	**0.274**	**0.339**	**23.249**	**17.718**
	336	0.422	0.456	**0.335**	**0.379**	**20.616**	**16.886**
	720	0.629	**0.570**	**0.406**	**0.423**	**35.453**	**25.789**
ILI	24	**2.752**	1.125	2.760	**1.123**	-0.291	**0.178**
	36	**2.318**	**0.980**	2.362	0.984	-1.898	-0.408
	48	2.328	1.006	**2.264**	**0.988**	**2.749**	**1.789**
	60	2.574	1.081	**2.520**	**1.062**	**2.098**	**1.758**

Table 10: Informer univariate

		Informer		TSAA			
		MSE	MAE	MSE↓	MAE↓	MSE%↑	MAE%↑
ETTm2	96	**0.085**	**0.225**	**0.085**	0.226	**0.000**	-0.444
	192	0.130	0.282	**0.128**	**0.279**	**1.538**	**1.064**
	336	**0.161**	**0.314**	0.164	0.317	-1.863	-0.955
	720	0.221	0.373	**0.221**	**0.371**	**0.000**	**0.536**
Electricity	96	0.261	0.367	**0.245**	**0.356**	**6.130**	**2.997**
	192	**0.285**	**0.386**	0.297	0.401	-4.211	-3.886
	336	**0.324**	**0.417**	0.433	0.485	-33.642	-16.307
	720	**0.632**	**0.612**	0.707	0.644	-11.867	-5.229
Exchange	96	0.490	0.554	**0.149**	**0.307**	**69.592**	**44.585**
	192	0.790	0.721	**0.260**	**0.402**	**67.089**	**44.244**
	336	2.146	1.223	**0.744**	**0.671**	**65.331**	**45.135**
	720	1.447	1.008	**0.527**	**0.594**	**63.580**	**41.071**
Traffic	96	0.262	0.348	**0.254**	**0.342**	**3.053**	**1.724**
	192	0.294	0.376	**0.284**	**0.367**	**3.401**	**2.394**
	336	0.308	0.390	**0.300**	**0.384**	**2.597**	**1.538**
	720	0.364	0.440	**0.326**	**0.409**	**10.440**	**7.045**
Weather	96	0.005	0.048	**0.003**	**0.043**	**40.000**	**10.417**
	192	0.004	0.051	**0.003**	**0.038**	**25.000**	**25.490**
	336	**0.003**	**0.043**	0.004	0.047	-33.333	-9.302
	720	0.004	0.049	**0.003**	**0.043**	**25.000**	**12.245**

Table 11: Autoformer univariate

		Autoformer		TSAA			
		MSE	MAE	MSE↓	MAE↓	MSE%↑	MAE%↑
ETTm2	96	0.123	0.270	**0.106**	**0.250**	**13.821**	**7.407**
	192	0.141	0.289	**0.126**	**0.273**	**10.638**	**5.536**
	336	0.170	0.319	**0.139**	**0.290**	**18.235**	**9.091**
	720	0.206	0.353	**0.187**	**0.338**	**9.223**	**4.249**
Electricity	96	0.454	0.508	**0.388**	**0.456**	**14.537**	**10.236**
	192	0.511	0.532	**0.463**	**0.509**	**9.393**	**4.323**
	336	0.739	0.651	**0.493**	**0.517**	**33.288**	**20.584**
	720	0.673	0.610	**0.532**	**0.549**	**20.951**	**10.000**
Exchange	96	0.149	0.308	**0.146**	**0.295**	**2.013**	**4.221**
	192	**0.290**	**0.415**	0.298	0.416	-2.759	-0.241
	336	**0.708**	0.662	0.712	**0.643**	-0.565	**2.870**
	720	**1.324**	**0.892**	2.703	1.390	-104.154	-55.830
Traffic	96	0.266	0.372	**0.248**	**0.351**	**6.767**	**5.645**
	192	0.272	0.379	**0.249**	**0.353**	**8.456**	**6.860**
	336	0.261	0.374	**0.239**	**0.347**	**8.429**	**7.219**
	720	0.269	0.372	**0.237**	**0.343**	**11.896**	**7.796**
Weather	96	0.009	0.078	**0.003**	**0.039**	**66.667**	**50.000**
	192	0.009	0.068	**0.003**	**0.040**	**66.667**	**41.176**
	336	0.006	0.058	**0.004**	**0.046**	**33.333**	**20.690**
	720	0.007	0.063	**0.004**	**0.046**	**42.857**	**26.984**

Table 12: FEDformer-f univariate

		FEDformer-f		TSAA			
		MSE	MAE	MSE↓	MAE↓	MSE%↑	MAE%↑
ETTm2	96	**0.068**	**0.198**	**0.068**	**0.198**	**0.000**	**0.000**
	192	**0.096**	**0.238**	**0.096**	**0.238**	**0.000**	**0.000**
	336	**0.138**	**0.286**	0.140	0.290	-1.449	-1.399
	720	**0.189**	**0.335**	0.190	0.336	-0.529	-0.299
Electricity	96	0.244	0.364	**0.244**	**0.356**	**0.000**	**2.198**
	192	**0.276**	0.382	0.277	**0.381**	-0.362	**0.262**
	336	**0.347**	**0.432**	**0.347**	**0.432**	**0.000**	**0.000**
	720	**0.408**	**0.473**	**0.408**	**0.473**	**0.000**	**0.000**
Exchange	96	**0.133**	**0.284**	0.145	0.293	-9.023	-3.169
	192	**0.292**	**0.419**	0.313	0.434	-7.192	-3.580
	336	**0.477**	**0.532**	0.575	0.595	-20.545	-11.842
	720	**1.304**	**0.882**	2.852	1.453	-118.712	-64.739
Traffic	96	0.210	0.318	**0.191**	**0.292**	**9.048**	**8.176**
	192	0.206	0.311	**0.197**	**0.301**	**4.369**	**3.215**
	336	0.217	0.322	**0.204**	**0.309**	**5.991**	**4.037**
	720	0.243	0.342	**0.219**	**0.318**	**9.877**	**7.018**
Weather	96	0.009	0.073	**0.002**	**0.033**	**77.778**	**54.795**
	192	0.007	0.067	**0.002**	**0.034**	**71.429**	**49.254**
	336	0.006	0.062	**0.002**	**0.036**	**66.667**	**41.935**
	720	0.006	0.060	**0.002**	**0.039**	**66.667**	**35.000**

Table 13: NBEATS-I univariate

		NBEATS-I		TSAA			
		MSE	MAE	MSE↓	MAE↓	MSE%↑	MAE%↑
ETTm2	96	0.080	0.213	**0.075**	**0.202**	**6.250**	**5.164**
	192	0.103	0.240	**0.102**	**0.237**	**0.971**	**1.250**
	336	**0.162**	**0.312**	0.171	0.321	-5.556	-2.885
	720	**0.199**	**0.347**	0.231	0.376	-16.080	-8.357
Electricity	96	0.326	0.402	**0.270**	**0.360**	**17.178**	**10.448**
	192	0.350	0.417	**0.277**	**0.368**	**20.857**	**11.751**
	336	0.393	0.440	**0.310**	**0.394**	**21.120**	**10.455**
	720	0.458	0.490	**0.394**	**0.453**	**13.974**	**7.551**
Exchange	96	0.210	0.344	**0.093**	**0.238**	**55.714**	**30.814**
	192	1.130	0.840	**0.215**	**0.352**	**80.973**	**58.095**
	336	1.587	1.047	**0.532**	**0.572**	**66.478**	**45.368**
	720	0.870	0.747	**0.744**	**0.665**	**14.483**	**10.977**
Traffic	96	**0.181**	**0.268**	0.183	0.270	-1.105	-0.746
	192	0.177	0.263	**0.176**	**0.263**	**0.565**	**0.000**
	336	**0.180**	0.271	**0.180**	**0.270**	**0.000**	**0.369**
	720	0.226	0.316	**0.224**	**0.311**	**0.885**	**1.582**
Weather	96	0.003	0.044	**0.001**	**0.024**	**66.667**	**45.455**
	192	0.004	0.046	**0.001**	**0.027**	**75.000**	**41.304**
	336	**0.004**	0.048	**0.004**	**0.035**	**0.000**	**27.083**
	720	0.004	0.049	**0.002**	**0.034**	**50.000**	**30.612**

Table 14: NBEATS-G univariate

		NBEATS-G		TSAA			
		MSE	MAE	MSE↓	MAE↓	MSE%↑	MAE%↑
ETTm2	96	0.080	0.210	**0.071**	**0.192**	**11.250**	**8.571**
	192	0.110	0.250	**0.109**	**0.246**	**0.909**	**1.600**
	336	**0.172**	**0.320**	0.176	0.323	-2.326	-0.938
	720	**0.201**	**0.353**	0.218	0.366	-8.458	-3.683
Electricity	96	0.324	0.397	**0.263**	**0.354**	**18.827**	**10.831**
	192	0.363	0.420	**0.278**	**0.368**	**23.416**	**12.381**
	336	0.392	0.443	**0.350**	**0.422**	**10.714**	**4.740**
	720	0.489	0.502	**0.378**	**0.447**	**22.699**	**10.956**
Exchange	96	0.223	0.351	**0.093**	**0.236**	**58.296**	**32.764**
	192	0.783	0.675	**0.215**	**0.352**	**72.542**	**47.852**
	336	2.622	1.266	**1.167**	**0.861**	**55.492**	**31.991**
	720	2.588	1.303	**1.687**	**1.033**	**34.815**	**20.721**
Traffic	96	0.159	0.240	**0.158**	**0.239**	**0.629**	**0.417**
	192	0.181	0.264	**0.160**	**0.243**	**11.602**	**7.955**
	336	**0.155**	**0.239**	0.156	0.244	-0.645	-2.092
	720	0.212	0.304	**0.189**	**0.279**	**10.849**	**8.224**
Weather	96	0.003	0.043	**0.002**	**0.031**	**33.333**	**27.907**
	192	0.004	0.047	**0.002**	**0.028**	**50.000**	**40.426**
	336	0.005	0.054	**0.004**	**0.037**	**20.000**	**31.481**
	720	0.004	0.048	**0.002**	**0.036**	**50.000**	**25.000**

E.2 Main results with standard deviation

The following tables Tabs. 15, 16 augment the tables presented in Sec. 5 in the main text with standard deviation measures computed over three different seed numbers.

Table 15: Multivariate long-term time-series forecasting results with the standard deviation.

		Informer		Autoformer		FEDformer-w		FEDformer-f	
		MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE
ETTm2	96	0.545 ± 0.024	0.588 ± 0.014	0.231 ± 0.004	0.31 ± 0.0	0.205 ± 0.001	0.29 ± 0.0	0.189 ± 0.001	0.282 ± 0.001
	192	1.054 ± 0.044	0.808 ± 0.018	0.289 ± 0.013	0.346 ± 0.01	0.27 ± 0.0	0.329 ± 0.0	0.258 ± 0.002	0.326 ± 0.001
	336	1.523 ± 0.036	0.948 ± 0.014	0.341 ± 0.008	0.375 ± 0.004	0.328 ± 0.0	0.364 ± 0.0	0.323 ± 0.004	0.363 ± 0.004
	720	3.878 ± 0.072	1.474 ± 0.004	0.444 ± 0.005	0.434 ± 0.005	0.433 ± 0.005	0.425 ± 0.005	0.425 ± 0.008	0.421 ± 0.001
Electricity	96	0.336 ± 0.013	0.416 ± 0.007	0.2 ± 0.007	0.316 ± 0.007	0.196 ± 0.002	0.31 ± 0.002	0.185 ± 0.001	0.3 ± 0.001
	192	0.36 ± 0.015	0.441 ± 0.012	0.217 ± 0.0	0.326 ± 0.002	0.199 ± 0.001	0.31 ± 0.002	0.201 ± 0.007	0.316 ± 0.008
	336	0.356 ± 0.007	0.439 ± 0.006	0.258 ± 0.024	0.356 ± 0.013	0.217 ± 0.001	0.334 ± 0.001	0.214 ± 0.002	0.329 ± 0.002
	720	0.386 ± 0.012	0.452 ± 0.01	0.261 ± 0.002	0.363 ± 0.004	0.248 ± 0.004	0.357 ± 0.004	0.246 ± 0.002	0.353 ± 0.0
Exchange	96	1.029 ± 0.038	0.809 ± 0.02	0.15 ± 0.005	0.281 ± 0.005	0.151 ± 0.004	0.282 ± 0.004	0.142 ± 0.004	0.271 ± 0.004
	192	1.155 ± 0.038	0.867 ± 0.015	0.318 ± 0.012	0.409 ± 0.008	0.284 ± 0.003	0.391 ± 0.002	0.278 ± 0.003	0.383 ± 0.001
	336	1.589 ± 0.048	1.011 ± 0.011	0.713 ± 0.516	0.616 ± 0.243	0.442 ± 0.003	0.493 ± 0.001	0.45 ± 0.003	0.497 ± 0.001
	720	3.011 ± 0.302	1.431 ± 0.067	1.246 ± 0.007	0.872 ± 0.002	1.227 ± 0.024	0.868 ± 0.011	1.181 ± 0.018	0.841 ± 0.002
Traffic	96	0.744 ± 0.006	0.42 ± 0.006	0.615 ± 0.015	0.384 ± 0.009	0.584 ± 0.005	0.368 ± 0.005	0.577 ± 0.001	0.361 ± 0.002
	192	0.753 ± 0.01	0.426 ± 0.011	0.67 ± 0.068	0.421 ± 0.045	0.594 ± 0.007	0.372 ± 0.007	0.61 ± 0.003	0.379 ± 0.004
	336	0.876 ± 0.024	0.495 ± 0.013	0.635 ± 0.027	0.392 ± 0.014	0.59 ± 0.001	0.365 ± 0.002	0.623 ± 0.005	0.385 ± 0.004
	720	1.011 ± 0.032	0.578 ± 0.018	0.658 ± 0.011	0.402 ± 0.01	0.613 ± 0.006	0.375 ± 0.003	0.632 ± 0.006	0.388 ± 0.007
Weather	96	0.315 ± 0.004	0.382 ± 0.004	0.259 ± 0.014	0.332 ± 0.011	0.269 ± 0.011	0.347 ± 0.008	0.236 ± 0.024	0.316 ± 0.028
	192	0.428 ± 0.005	0.449 ± 0.012	0.298 ± 0.012	0.356 ± 0.012	0.357 ± 0.001	0.412 ± 0.002	0.273 ± 0.013	0.333 ± 0.012
	336	0.62 ± 0.027	0.554 ± 0.009	0.357 ± 0.01	0.394 ± 0.011	0.422 ± 0.008	0.456 ± 0.006	0.332 ± 0.016	0.371 ± 0.016
	720	0.975 ± 0.035	0.722 ± 0.009	0.422 ± 0.011	0.431 ± 0.01	0.629 ± 0.008	0.57 ± 0.004	0.408 ± 0.009	0.418 ± 0.008
ILI	24	5.349 ± 0.229	1.582 ± 0.052	3.549 ± 0.33	1.305 ± 0.068	2.752 ± 0.023	1.125 ± 0.005	3.268 ± 0.04	1.257 ± 0.014
	36	5.203 ± 0.129	1.572 ± 0.029	2.834 ± 0.166	1.094 ± 0.032	2.318 ± 0.017	0.98 ± 0.006	2.648 ± 0.034	1.068 ± 0.009
	48	5.286 ± 0.049	1.594 ± 0.018	2.889 ± 0.178	1.122 ± 0.033	2.328 ± 0.043	1.006 ± 0.013	2.615 ± 0.019	1.072 ± 0.004
	60	5.419 ± 0.103	1.62 ± 0.019	2.818 ± 0.157	1.118 ± 0.039	2.574 ± 0.052	1.081 ± 0.016	2.866 ± 0.031	1.158 ± 0.008

		TSAA	
		MSE	MAE
ETTm2	96	0.187 ± 0.000	0.274 ± 0.000
	192	0.255 ± 0.001	0.314 ± 0.001
	336	0.304 ± 0.009	0.350 ± 0.002
	720	0.398 ± 0.007	0.403 ± 0.002
Electricity	96	0.183 ± 0.001	0.297 ± 0.001
	192	0.195 ± 0.001	0.309 ± 0.002
	336	0.208 ± 0.002	0.323 ± 0.002
	720	0.238 ± 0.003	0.348 ± 0.003
Exchange	96	0.143 ± 0.012	0.272 ± 0.012
	192	0.27 ± 0.002	0.378 ± 0.002
	336	0.459 ± 0.007	0.504 ± 0.007
	720	1.213 ± 0.056	0.842 ± 0.008
Traffic	96	0.565 ± 0.005	0.352 ± 0.004
	192	0.572 ± 0.002	0.351 ± 0.001
	336	0.584 ± 0.004	0.359 ± 0.005
	720	0.607 ± 0.002	0.368 ± 0.002
Weather	96	0.18 ± 0.024	0.256 ± 0.024
	192	0.252 ± 0.001	0.311 ± 0.002
	336	0.296 ± 0.001	0.355 ± 0.005
	720	0.382 ± 0.006	0.395 ± 0.007
ILI	24	2.76 ± 0.063	1.123 ± 0.016
	36	2.362 ± 0.024	0.984 ± 0.008
	48	2.264 ± 0.074	0.988 ± 0.012
	60	2.52 ± 0.064	1.062 ± 0.022

Table 16: Univariate long-term time-series forecasting results with the standard deviation.

		Informer		Autoformer		FEDformer-f		N-BEATS-I	
		MSE	MAE	MSE	MAE	MSE	MAE	MSE	MAE
ETTm2	96	0.085 ± 0.004	0.225 ± 0.006	0.123 ± 0.017	0.27 ± 0.018	0.068 ± 0.001	0.198 ± 0.002	0.08 ± 0.003	0.213 ± 0.006
	192	0.13 ± 0.007	0.282 ± 0.008	0.141 ± 0.01	0.289 ± 0.01	0.096 ± 0.001	0.238 ± 0.001	0.103 ± 0.004	0.24 ± 0.006
	336	0.161 ± 0.008	0.314 ± 0.006	0.17 ± 0.046	0.319 ± 0.042	0.138 ± 0.013	0.286 ± 0.014	0.162 ± 0.009	0.312 ± 0.009
	720	0.221 ± 0.006	0.373 ± 0.007	0.206 ± 0.02	0.353 ± 0.017	0.189 ± 0.002	0.335 ± 0.002	0.199 ± 0.007	0.347 ± 0.007
Electricity	96	0.261 ± 0.005	0.367 ± 0.002	0.454 ± 0.014	0.508 ± 0.014	0.244 ± 0.001	0.364 ± 0.002	0.326 ± 0.006	0.402 ± 0.004
	192	0.285 ± 0.006	0.386 ± 0.003	0.511 ± 0.05	0.532 ± 0.027	0.276 ± 0.004	0.382 ± 0.004	0.35 ± 0.008	0.417 ± 0.005
	336	0.324 ± 0.004	0.417 ± 0.004	0.739 ± 0.086	0.651 ± 0.042	0.347 ± 0.007	0.432 ± 0.006	0.393 ± 0.008	0.44 ± 0.003
	720	0.632 ± 0.049	0.612 ± 0.028	0.673 ± 0.082	0.61 ± 0.037	0.408 ± 0.025	0.473 ± 0.015	0.458 ± 0.008	0.49 ± 0.002
Exchange	96	0.49 ± 0.065	0.554 ± 0.034	0.149 ± 0.004	0.308 ± 0.006	0.133 ± 0.015	0.284 ± 0.018	0.21 ± 0.047	0.344 ± 0.036
	192	0.79 ± 0.039	0.721 ± 0.016	0.29 ± 0.005	0.415 ± 0.004	0.292 ± 0.002	0.419 ± 0.003	1.13 ± 0.392	0.84 ± 0.153
	336	2.146 ± 0.25	1.223 ± 0.084	0.708 ± 0.108	0.662 ± 0.053	0.477 ± 0.002	0.532 ± 0.002	1.587 ± 0.219	1.047 ± 0.077
	720	1.447 ± 0.105	1.008 ± 0.038	1.324 ± 0.005	0.892 ± 0.002	1.304 ± 0.003	0.882 ± 0.0	0.87 ± 0.088	0.747 ± 0.015
Traffic	96	0.262 ± 0.006	0.348 ± 0.006	0.266 ± 0.005	0.372 ± 0.01	0.21 ± 0.006	0.318 ± 0.009	0.181 ± 0.004	0.268 ± 0.005
	192	0.294 ± 0.004	0.376 ± 0.006	0.272 ± 0.014	0.379 ± 0.01	0.206 ± 0.01	0.311 ± 0.006	0.177 ± 0.001	0.263 ± 0.001
	336	0.308 ± 0.007	0.39 ± 0.002	0.261 ± 0.016	0.374 ± 0.016	0.217 ± 0.005	0.322 ± 0.0	0.18 ± 0.005	0.271 ± 0.006
	720	0.364 ± 0.018	0.44 ± 0.017	0.269 ± 0.012	0.372 ± 0.005	0.243 ± 0.021	0.342 ± 0.021	0.226 ± 0.003	0.316 ± 0.004
Weather	96	0.005 ± 0.001	0.048 ± 0.005	0.009 ± 0.002	0.078 ± 0.009	0.009 ± 0.004	0.073 ± 0.014	0.003 ± 0.001	0.044 ± 0.006
	192	0.004 ± 0.0	0.051 ± 0.001	0.009 ± 0.002	0.068 ± 0.001	0.007 ± 0.002	0.067 ± 0.008	0.004 ± 0.0	0.046 ± 0.003
	336	0.003 ± 0.001	0.043 ± 0.004	0.006 ± 0.001	0.058 ± 0.006	0.006 ± 0.001	0.062 ± 0.007	0.004 ± 0.001	0.048 ± 0.004
	720	0.004 ± 0.002	0.049 ± 0.007	0.007 ± 0.001	0.063 ± 0.004	0.006 ± 0.001	0.06 ± 0.007	0.004 ± 0.0	0.049 ± 0.003

		N-BEATS-G		TSAA	
		MSE	MAE	MSE	MAE
ETTm2	96	0.08 ± 0.005	0.21 ± 0.007	0.068 ± 0.001	0.192 ± 0.002
	192	0.11 ± 0.004	0.25 ± 0.005	0.096 ± 0.001	0.237 ± 0.004
	336	0.172 ± 0.007	0.32 ± 0.007	0.139 ± 0.005	0.29 ± 0.005
	720	0.201 ± 0.008	0.353 ± 0.008	0.187 ± 0.008	0.336 ± 0.001
Electricity	96	0.324 ± 0.005	0.397 ± 0.002	0.244 ± 0.006	0.354 ± 0.012
	192	0.363 ± 0.005	0.42 ± 0.003	0.277 ± 0.003	0.368 ± 0.003
	336	0.392 ± 0.002	0.443 ± 0.006	0.31 ± 0.006	0.394 ± 0.005
	720	0.489 ± 0.013	0.502 ± 0.005	0.378 ± 0.026	0.447 ± 0.012
Exchange	96	0.223 ± 0.046	0.351 ± 0.045	0.093 ± 0.008	0.236 ± 0.007
	192	0.783 ± 0.203	0.675 ± 0.085	0.215 ± 0.035	0.352 ± 0.017
	336	2.622 ± 1.07	1.266 ± 0.23	0.532 ± 0.045	0.572 ± 0.006
	720	2.588 ± 0.11	1.303 ± 0.019	0.527 ± 0.047	0.594 ± 0.019
Traffic	96	0.159 ± 0.001	0.24 ± 0.002	0.158 ± 0.001	0.239 ± 0.001
	192	0.181 ± 0.005	0.264 ± 0.001	0.16 ± 0.0	0.243 ± 0.001
	336	0.155 ± 0.001	0.239 ± 0.001	0.156 ± 0.004	0.244 ± 0.006
	720	0.212 ± 0.003	0.304 ± 0.003	0.189 ± 0.002	0.279 ± 0.003
Weather	96	0.003 ± 0.0	0.043 ± 0.002	0.001 ± 0.0	0.024 ± 0.0
	192	0.004 ± 0.001	0.047 ± 0.004	0.001 ± 0.0	0.027 ± 0.001
	336	0.005 ± 0.001	0.054 ± 0.004	0.002 ± 0.0	0.035 ± 0.004
	720	0.004 ± 0.0	0.048 ± 0.002	0.002 ± 0.0	0.034 ± 0.002