Compositional Program Generation for Systematic Generalization

Anonymous Author(s)
Affiliation
Address
email

Abstract

Compositional generalization remains a difficult problem for neural models. There has been progress but the hardest benchmark problems remain intractable without additional task-specific semantic information. In this paper we describe a neuro-symbolic architecture Compositional Program Generator (CPG) which generalizes systematically and productively for sequence-to-sequence language tasks, given a context-free grammar of the input language and a dictionary mapping each input word to its interpretation in the output language. Our approach learns to generate type-specific symbolic semantic functions composed in an input-dependent way to produce the output sequence. In experiments on SCAN, CPG solves all splits and few-shot generalizes on the systematicity ("add jump") split. On COGS it generalizes perfectly.

1 Introduction

Although no satisfactory formal definition of compositional generalization has yet been given, it is usually taken to have two requirements: generalization to new (grammatical) combinations of parts of an input seen in training (systematicity); and generalization to longer sequences than seen in training (productivity). For example, having translated a command like “jump left twice” to (I_TURN_LEFT, I_JUMP, I_TURN_LEFT, I_JUMP) as in Figure 1; having seen the command “walk” in training; and knowing that “jump” and “walk” are both of the same type, the model should generalize systematically to translate “walk left twice” as (I_TURN_LEFT, I_WALK, I_TURN_LEFT, I_WALK) with no further training. This kind of generalization has proved challenging for standard neural models such as transformers [**?**].

2 Approach

One strategy for achieving compositional generalization is to learn a compositional function. These are often described informally as “meaning" functions where “the meaning of the whole is a function of the meaning of the parts." Usually attributed to Frege, this idea appears in some form as early as the sixth century BCE [1]. In [1] they give two formal definitions of compositional functions, one of which, the functional definition, we restate here with minor modifications. It assumes the input language L is defined over finite vocabulary V and is generated by a set of context-free grammar rules Σ (denoted α, β, γ, etc.) which map input types to an output type (or for primitive types, an input token to an output type).

A function μ from a source language $L \subset V^*$ to a target language L' is *compositional* if for every rule $\alpha \in \Sigma$ there is a function $r(\alpha)$ such that if α is defined, then $\mu(\alpha(u_1, u_2, \ldots, u_n)) = r(\alpha)(\mu(u_1), \mu(u_2), \ldots, \mu(u_n))$. Here V is a finite vocabulary and V^* denotes the set of all strings

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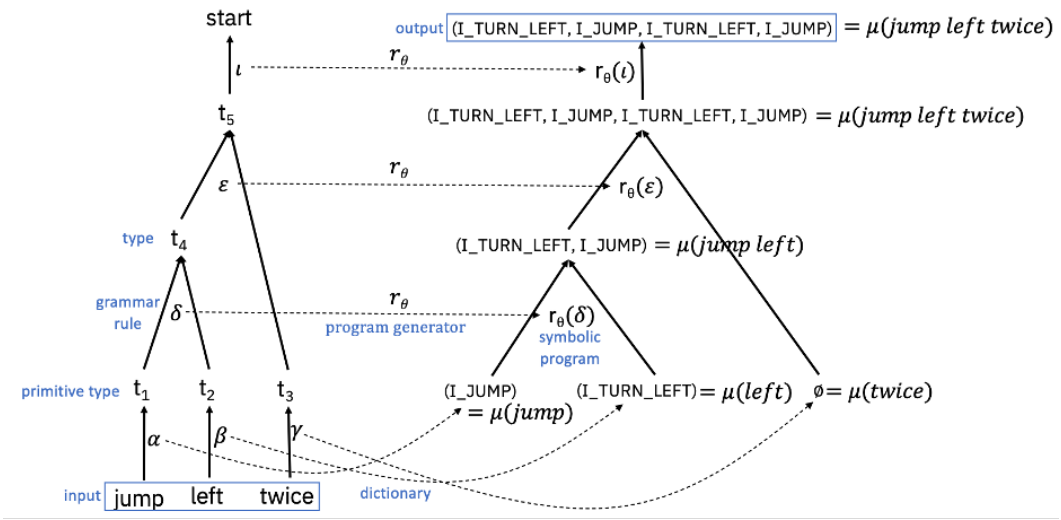

Figure 1: An example of compositional program generation on SCAN.

over that vocabulary. The function μ ("meaning") is defined recursively over a structure ("parts") determined by a parse of the input.

Compositional functions are a useful hypothesis class for learning models which compositionally generalize. First, they are defined recursively over an arbitrarily large input structure and hence productive by definition. Second, they offer a natural way to decompose the model by processing each rule α with a semantic module specific to that rule ($r(\alpha)$). Third, they allow the structure of the semantic computation to vary depending on the input. Finally, since r is not directly dependent on the input, a learner will generate the same semantic function for the same syntactic rule and the model will generate the same meaning for phrases with the same derivations in the grammar which is what is desired for systematic generalization.

We decompose the problem of learning a sequence-to-sequence model into sub-problems: specifying a context-free grammar for the input language L; programmatically generating a parser (we use Lark [1]); learning or providing the dictionary that maps input tokens to their output representation (if any); and learning to generate a type-specific semantic function for each type in the grammar. We will focus mainly on the problem of generating type-specific functions and leave it to future work to learn the grammar. We are able to learn a dictionary jointly with the semantic functions for SCAN since it's quite simple; learning the dictionary for COGS is more involved and we don't try it here. With these assumptions the model is able to solve SCAN in a productive and systematic way with interpretable semantic rules and with length-curricular training on sentences of commands of length ≤ 3 with few shot generalization on the "add jump" (systematicity) split. Using the same architecture and curricular training it also achieves perfect generalization on COGS, after 2 epochs of training.

Our approach to learning a compositional function is *compositional program generation* by which we mean both that the process of generating a (symbolic) program from an instance is compositional, generating each composition recursively, bottom-up over the structure of the parse, but also that the generated program is itself compositional with respect to that structure in the sense of [1], obeying the requirement that the meaning of the whole be a function of the meaning of it's parts.

The CPG model learns to generate parameters for two kinds of programs, *copy* programs, which produce an output sequence by copying elements of the input sequence (with filtering and repeats allowed), and *substitution* programs which substitute objects from one list into slots in an expression (denoted y in our examples) for use in COGS. Figure 2 gives the semantics for these operations.

[1] https://github.com/lark-parser/lark

$copy(x, x')$:
$|x| = |x'| = k$. α a grammar rule. θ trainable parameters
$P_\theta(\alpha)$ a probability distribution over $[0, \ldots, k-1]$
$s \leftarrow [j \sim P_\theta(\alpha)$ for i in $[0, \ldots, k-1]]$
x – source; x' – destination; s – indices to copy
$x'[i] \leftarrow x[s[i]]$ for i in s

(a) copy semantics

$subst(x, x')$:
$|x| = |x'| = k$. α a grammar rule. θ trainable parameters
$P'_\theta(\alpha)$ a probability distribution over $[0, \ldots, l]$
find target slots
$t \leftarrow$ find_slots(x')
$l \leftarrow |t|$
generated indices between 0 and the number of slots l.
index l indicates no substitution.
s $\leftarrow [j \sim P'_\theta$ for i in $[0, \ldots, l-1]]$
x – source; x' – destination; t – slot indices; s – source indices
$x'[t[i]] \leftarrow x[s[i]]$ if $s[i] \neq l$ else $x'[t[i]]$ for i in $[0, \ldots, l-1]$

(b) substitution semantics

Figure 2: (a) copy program (top); (b) substitution program (bottom)

Using the Lark parser generator we generate a parser for the input grammar and run it to produce a linear sequence of parse steps which produce the parse tree for that input. Each parse step applies a context-free grammar rule α to a contiguous span of the input and replaces it with the type specified as the output of α. Grammar rules with arity l for non-primitive types (see Figure 1) are of the form: $t_0 t_1 \ldots t_{l-1} \rightarrow t$ for input grammar types t_i, $0 \leq i \leq l-1$, and output grammar type t. For primitive types the rules are of the form $x \rightarrow t$ for x an input token and t a primitive type. Disjunctive rules are of the form $t_0 | t_1 | \ldots | t_{l-1} \rightarrow t$. Figure 1 shows an example of a parse tree constructed by successively applying the parse sequence rules to the input.

The parse rule sequence is the input to a recursive model, the compositional learner, which learns the function r_θ shown in Figure 1. To initialize the process it maps the input tokens individually to their output language interpretation using the dictionary as shown in the bottom of Figure 1. If a token does not have a corresponding output token it is mapped to the empty list, denoted ϕ. For COGS, where the output is a logical form, variables are required and we map each input token to a pair of sequences as shown in Figure 3, the first holding an expression representing the meaning of the input word (which may contain slots denoted y, e.g. $y.agent(y, y)$); and a separate sequence for objects (universal variables and constants) (e.g. $[0, Emma]$). Substitution relies on a function $find_slots(x)$ which returns the indices of the y variables (0-indexed). An example showing composition in COGS is shown in Figure 3. At each step the argument expression lists are concatenated to form the output expression and similarly with the object lists to form the output object list. After concatenation the generated substitution program is applied, to substitute objects from the concatenated object list for y variables in the output expression. Disjunctive rules are not associated with any substitution so the input object and expression lists are just concatenated into their output lists.

3 Experiments

All distributions for SCAN are implemented as linear layers (for COGS two-layer) followed by a Gumbel softmax estimator to sample. There are separate layers for each rule encouraging specialization. Training is curricular by input length and temperature is annealed for the Gumbel distributions in proportion to curriculum stage accuracy.

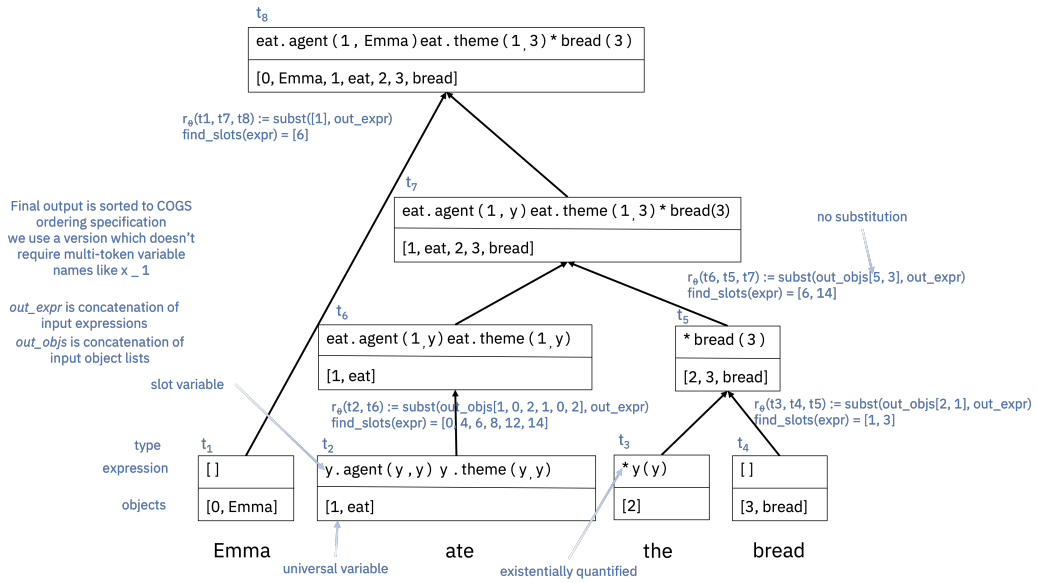

Figure 3: compositional generation on COGS

We've conducted experiments with both SCAN and COGS. For SCAN we modify the "add primitive" (systematicity) training data to have just a single example of the held-out word (one-shot). On SCAN the model generalizes perfectly on all splits after training on up to length 3 sentences, since all types have been seen in training by that point. The model also achieves perfect generalization on COGS after training on a subset of the training set containing sentences of length 12 or less in 2 epochs of training.

4 Related Work

Compositionality is an important characteristic of language understanding by humans. There has been a long-standing debate on whether connectionist architectures like neural networks are able to do compositional generalization [2]. Recently, with the ubiquity of neural networks, there has been a number of benchmarks proposed to study compositional generalization like SCAN [3, 4], COGS [5], CFQ [6] and others [7, 8]. Several of these works have shown that end-to-end neural networks are not able to compositionally generalize, especially in few-shot regimes. This in turn has led to neuro-symbolic architectures to tackle compositionality [9, 10]. However, these approaches suffer from being too specialized for a certain benchmark and require significant modifications to be adaptable to another benchmark. In contrast, our approach CPG learns to perfectly generalize compositionally in a task-agnostic manner, in one-shot learning scenarios.

In Liu et al. [9] they employ a similar bottom-up recursive approach (LANE), interleaving syntactic composition with the generation of symbolic programs and their evaluation. The key difference is that the syntactic composition does not produce types, as is done in parsing, it produces untyped variables, and the symbolic program generation is therefore not type-specific and modular. In their approach the generation is dependent on the current source expression and therefore is subject to over-fitting by the program generator. By contrast, we use *only* the rule input and output types to generate the program, forcing type-general solutions.

As in Herzig and Berant [11], we construct programs to solve the problem, bottom up recursively, however, we do not require gold programs to train and instead interleave program generation and evaluation with output supervision only. They infer semantic categories for each node but their semantic categories include just: (1) one type for each constant (like $Emma$ or fed) ; (2) a $join$ type that is used for all compositions; and (3) ϕ a category indicating not-important.

In an orthogonal direction, there are recent works that use pre-trained large language models using billions of parameters that are able to perform well on some compositional generalization benchmarks [12]. However, our objective is focusing on the architecture and learning algorithm and is orthogonal to pre-training, since we want to see if neuro-symbolic models, trained from scratch can outperform their purely neural counterparts.

5 Conclusion

We have presented a novel compositional architecture which decomposes the problem of sequence to sequence transduction into components which involve grammar specification, parsing, dictionary learning, and compositional function generator learning. We use these components to learn a compositional model which has three key attributes: This approach scales both productively and systematically for the SCAN and COGS dataset by learning to compose generated semantic copy and substitution operations, in a structure given by the parser. This class of semantic operations is quite general and should be applicable to other similar types of sequence manipulation tasks. For SCAN the dictionary is easy to learn; for COGS we haven't tried but believe that it could be learned as well. Grammar learning and parsing are also both possible to learn, as discussed in the related work section. We plan next to expand this work to learn those jointly.

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