NetFormer: An interpretable model for recovering identity and structure in neural population dynamics

Wuwei Zhang[*]
Princeton University

Ziyu Lu[*]
University of Washington

Trung Le
University of Washington

Hao Wang
Rutgers University

Uygar Sümbül
Allen Institute for Brain Science

Eric Shea-Brown[†]
University of Washington

Lu Mi[†]
Georgia Institute of Technology

Abstract

Neuronal dynamics are highly nonlinear and nonstationary. Traditional methods for extracting the underlying network structure from activity recordings mainly concentrate on modeling static connectivity, without accounting for key nonstationary aspects of biological neural systems, such as ongoing synaptic plasticity and neuronal modulation. To bridge this gap, we introduce the NetFormer model, an interpretable approach applicable to such systems. In our model, activity of each neuron across a series of historical time steps is defined as a token. These tokens are then linearly mapped through a query and key mechanism to generate a state- (and hence time-) dependent attention matrix that directly encodes nonstationary connectivity structures. We analyzed our formulation from the perspective of nonstationary and nonlinear networked dynamical systems. We then applied NetFormer to a large-scale, multi-modal dataset of neural activity patterns across populations of neurons in mouse visual cortex. By comparing against an allied dataset containing ground-truth baselines for connectivity between cell types, we demonstrated the effectiveness of NetFormer in predicting neural dynamics and recovering the underlying structural information about the molecular identity.

1 Introduction

Inferring the underlying connectivity of a network from observations of the activity of its units is a long-standing challenge. In the brain, this challenge is exacerbated by (i) different nonlinear dynamics present in individual neurons, (ii) experimental difficulty in sampling the full neuronal population simultaneously, and (iii) dynamic reconfiguration of effective connectivity, mediated by both synaptic plasticity and neuromodulation. This last issue carries significant practical importance in studying behavioral dynamics, learning and memory [1, 2, 3, 4, 5]. As such, it poses a (harder) generalization of the classical problem where the connectivity should no longer be considered as a static unknown, rather as a dynamical variable that needs to be inferred and tracked over time.

A surrogate, but not sufficient, measure of success in unsupervised inference of connectivity is the inferred network's success in fitting the observed dynamics (Appendix A.1). While traditional linear

[*]Equally contributing first authors.
[†]Equally contributing senior authors.
Correspondence to: wz1411@princeton.edu, luziyu@uw.edu, lmi7@gatech.edu, etsb@uw.edu.

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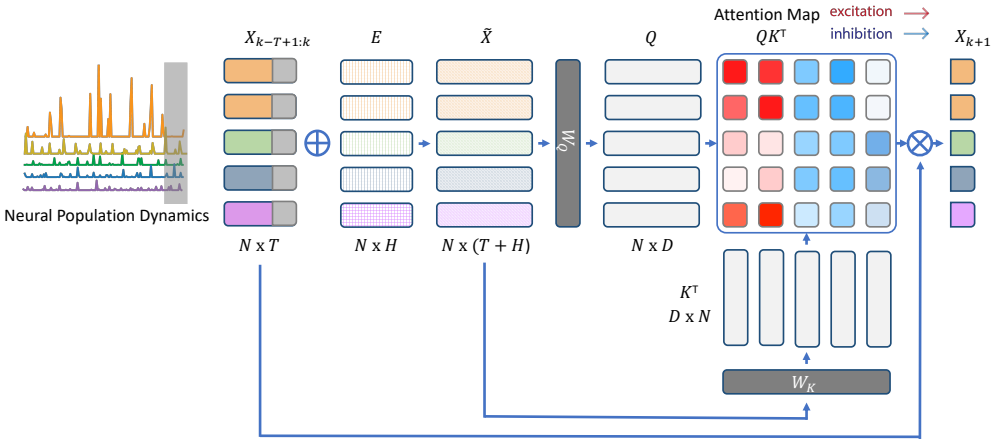

Figure 1: Overview of NetFormer. NetFormer learns to predict neural dynamics and infer connectivity through a linearized attention mechanism. It takes in as input activity of N neurons across T timesteps ($X_{k-T+1:k}$), and predicts their next-step activity (X_{k+1}). Queries Q and keys K are linearly mapped from $\tilde{X}$ ($X_{k-T+1:k}$ concatenated with positional embedding E), using W_Q and W_K. Linearized attention matrix is computed as $QK^\top$, which learns the neuron-level connectivity implicitly. Red and blue in the attention map indicate excitatory and inhibitory interactions, respectively.

dynamical models struggle to capture the essential nonlinear mechanisms of leaky integration and firing in biological neurons [6], more sophisticated nonlinear models typically suffer from a lack of interpretability, making it difficult to identify the underlying connectivity [7, 8, 9]. Moreover, traditional approaches often adopt a static perspective on connectivity [10, 11], failing to account for the nonstationary interactions, such as those produced by plasticity and modulation at synapses.

Here we propose an interpretable nonlinear and nonstationary dynamical model to represent interactions between neurons (Figure 1), based on the fast weight programming nature of the attention mechanism [12]. Prior research has suggested that the attention mechanism can reveal information about the underlying structure of a system [13, 14]. We further removed the softmax activation funtion in the attention mechanism, as the constraint of attention weights summing up to one is not biologically meaningful because neither the in-degrees nor the out-degrees of neuronal connectivity (nor their counterparts incorporating synaptic strength) are invariant across neurons [15]. We first demonstrated with both mathematical analysis and simulation study that even without the softmax activation, the core part of the attention mechanism – the dot-product between queries and keys – is capable of capturing nonstationary and nonlinear structural information. We then evaluated this novel approach on publicly available datasets of neuronal activity recordings, showing its potential for recovering meaningful identity and structural information. Our main contributions are as follows: (i) We formulated a transformer-inspired network model, the NetFormer, for which the core of the attention mechanism – the dot-product between queries and keys – directly encodes nonstationary and nonlinear structure of networks; (ii) We applied the NetFormer model to population activity recorded from mouse visual cortex, and showed that it can recover experimentally measured synaptic connectivity, while benchmarking it with standard recurrent models and other common statistical metrics; (iii) We provided a mathematical analysis on how the NetFormer can capture nonstationary interactions likely to exist in the brain, providing a hypothesis for the improved performance of the NetFormer on real neural data.

2 Model: Mathematical analysis on simulated systems

We consider an N-dimensional dynamical system

$$\frac{d}{dt}\boldsymbol{x}(t) = f\big(\boldsymbol{W}(t)\boldsymbol{x}(t)\big) \tag{2.1}$$

where $\boldsymbol{x}(t) \in \mathbb{R}^N$, $f : \mathbb{R}^N \to \mathbb{R}^N$, and $\boldsymbol{W}(t)$ is an $N \times N$ matrix whose entries may vary across time. $W_{i,j}(t)$ prescribes how the i-th variable $\boldsymbol{x}^{(i)}$ is driven by the j-th variable $\boldsymbol{x}^{(j)}$ at time t.

Let $\boldsymbol{x}_k$ be observations of the system at discrete timesteps t_k. For each k, we train the NetFormer model (Figure 1) to predict $\boldsymbol{x}_{k+1}$ based on $\boldsymbol{X}_k = [\boldsymbol{x}_{k-T+1} \quad \cdots \quad \boldsymbol{x}_k] \in \mathbb{R}^{N\times T}$, the recent T-step history of the system up to timestep k. To encode neuronal identities, a learnable positional

embedding matrix $\boldsymbol{E} \in \mathbb{R}^{N \times H}$ is concatenated to $\boldsymbol{X}_k$, giving $\tilde{\boldsymbol{X}}_k = [\boldsymbol{X}_k \quad \boldsymbol{E}] \in \mathbb{R}^{N \times (T+H)}$. The queries $\boldsymbol{Q}_k$ and keys $\boldsymbol{K}_k$ are obtained through linear transformations of $\tilde{\boldsymbol{X}}_k$, and their product gives the linearized attention matrix $\boldsymbol{A}_k$:

$$\boldsymbol{Q}_k = \tilde{\boldsymbol{X}}_k \boldsymbol{W}_Q \in \mathbb{R}^{N \times D}, \ \boldsymbol{K}_k = \tilde{\boldsymbol{X}}_k \boldsymbol{W}_K \in \mathbb{R}^{N \times D}, \ \boldsymbol{A}_k = \boldsymbol{Q}_k \boldsymbol{K}_k^\top \in \mathbb{R}^{N \times N}. \tag{2.2}$$

It follows that entry (i, j) of $\boldsymbol{A}_k$ is computed from the history of $\boldsymbol{x}^{(i)}$ and $\boldsymbol{x}^{(j)}$, and thus describes the relationship between the i-th and j-th variables. To predict $\boldsymbol{x}_{k+1}$, we take $\boldsymbol{x}_k$ to be the values $\boldsymbol{v}_k$ and employ the residual connection [16], obtaining prediction as

$$\hat{\boldsymbol{x}}_{k+1} = \boldsymbol{v}_k + \boldsymbol{A}_k \boldsymbol{v}_k = \boldsymbol{x}_k + \boldsymbol{A}_k \boldsymbol{x}_k, \tag{2.3}$$

which is similar to the update rule we would get if Equation 2.1 were simulated using the classical forward Euler method with step size δ

$$\boldsymbol{x}_{k+1} = \boldsymbol{x}_k + \delta f(\boldsymbol{W}_k \boldsymbol{x}_k). \tag{2.4}$$

Since neuronal connections can be either excitatory or inhibitory, but neither effect can be arbitrarily large, we choose f to be a sigmoidal function with

$$f(0) = 0, \ f(\bar{x}) = f(0) + f'(0)\bar{x} + O(\bar{x}^3) \text{ for } \bar{x} \text{ within some interval } (-\epsilon, \epsilon) \text{ around } 0^{1}$$

Equation 2.4 can thus be written as

$$\boldsymbol{x}_{k+1} = \boldsymbol{x}_k + \delta f(\boldsymbol{W}_k \boldsymbol{x}_k) = \boldsymbol{x}_k + \delta f'(0) \boldsymbol{W}_k \boldsymbol{x}_k + \delta O(\boldsymbol{x}_k^3). \tag{2.5}$$

Comparing equations 2.3 and 2.5, we deduce that the linearized attention matrix $\boldsymbol{A}_k$ learned by the NetFormer may capture the true interactions between different variables $\boldsymbol{W}_k$ by approximating $\delta f'(0)\boldsymbol{W}_k$, especially when $\epsilon < 1$ and the first order term plays the most significant role. It is not hard to see that this hypothesis also extends to systems in the form of

$$\frac{d}{dt}\boldsymbol{x}(t) = -\boldsymbol{x}(t) + f\big(\boldsymbol{W}(t)\boldsymbol{x}(t)\big), \tag{2.6}$$

which includes the decaying effect that is commonly present in neural dynamics [17] (Appendix A.2).

We first considered four simplified simulated systems, with variations in the inclusion of nonlinearity and nonstationarity:

$$\textbf{(a)} \ \frac{d\boldsymbol{x}}{dt} = \boldsymbol{W}\boldsymbol{x}, \ \textbf{(b)} \ \frac{d\boldsymbol{x}}{dt} = \tanh(\boldsymbol{W}\boldsymbol{x}), \ \textbf{(c)} \ \frac{d\boldsymbol{x}}{dt} = \boldsymbol{W}(\boldsymbol{x})\boldsymbol{x}, \ \textbf{(d)} \ \frac{d\boldsymbol{x}}{dt} = \tanh(\boldsymbol{W}(\boldsymbol{x})\boldsymbol{x}),$$

where $\boldsymbol{W}(\boldsymbol{x}) = \boldsymbol{W}_0 + \boldsymbol{x}\boldsymbol{\omega}^\top$. Simulation details are in Appendix A.3.1. All trained NetFormer models are able to make accurate one-step-ahead predictions ($R^2 = 1.000$, Figure 2a-d left). Visually, the average linearized attention matrix across timesteps, $\bar{\boldsymbol{A}} = \frac{1}{K}\sum_{k=1}^{K} \boldsymbol{A}_k$, provides a good characterization of the average ground-truth dynamical association matrix across timesteps, $\bar{\boldsymbol{W}} = \frac{1}{K}\sum_{k=1}^{K} \boldsymbol{W}(\boldsymbol{x}_k)$ (Figure 2a-d right). As a baseline, we consider $\boldsymbol{A}_{\text{OLS}}$ from the linear ordinary least squares regression $\hat{\boldsymbol{x}}_{k+1} = \boldsymbol{A}_{\text{OLS}}\boldsymbol{x}_k$. We used the Spearman's rank correlation coefficient (ρ) between the off-diagonal entries of $\bar{\boldsymbol{A}}$ or $\boldsymbol{A}_{\text{OLS}}$ and $\bar{\boldsymbol{W}}$ to quantify how faithfully the learned connectivities reflect the ground-truth. $\bar{\boldsymbol{A}}$ achieved comparable performance as $\boldsymbol{A}_{\text{OLS}}$ in systems **(a) (b)**, but significantly outperformed $\boldsymbol{A}_{\text{OLS}}$ in systems **(c) (d)**, both visually (Figure 2a-d right) and quantitively (Appendix A.3.2). Moreover, in the nonstationary systems **(c) (d)**, the linearized attention matrix is able to track the majority of changes in $\boldsymbol{W}(\boldsymbol{x})$ across timesteps (Figure 2e-f and Appendix A.3.3). This ability to capture nonstationarity also explains why NetFormer can outperform the linear regression model which only accounts for static connectivity.

3 Experiments on connectivity-constrained simulation and neural data

Neurons form synapses based, in part, on their cell types. The transmission of information through these synapses is stochastic, which is shaped by activity history [18]. We applied the NetFormer on a recent multi-modal dataset from [19], where both activity and cell type of neurons in the mouse primary visual cortex are available. After training the NetFormer to predict activity, we inferred the connectivity strength between cell types from its attention matrix, and compared it against

[1] see Appendix A.3.4 for more discussion on the radius of convergence of this series representation

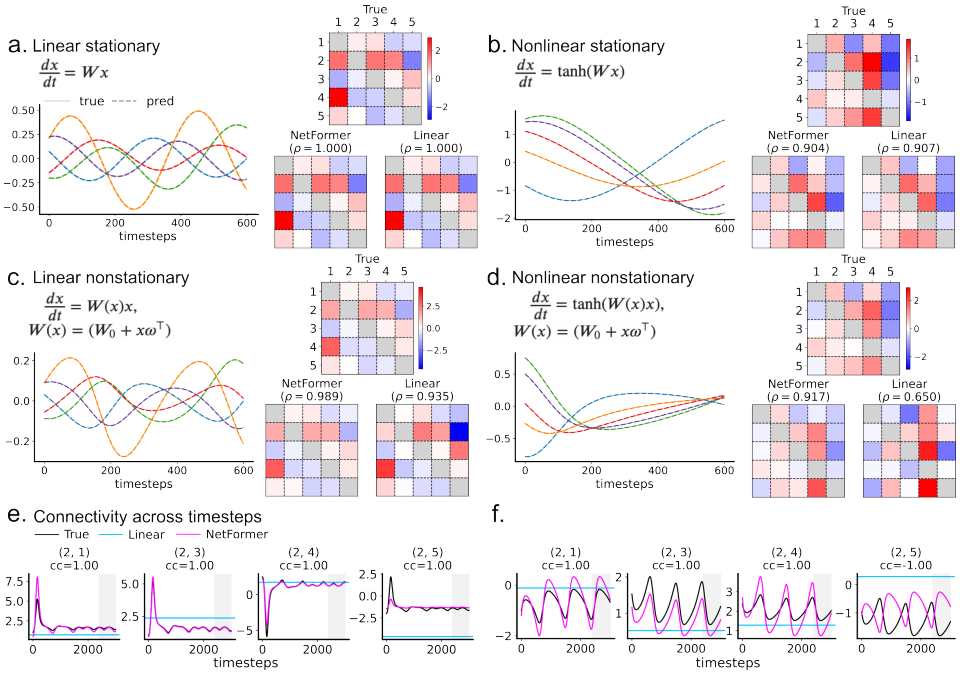

Figure 2: NetFormer provides accurate dynamics predictions, and recovers ground truth connectivity matrices. a-d Left: Test set predictions of NetFormer. Predicted trajectories were obtained by concatenating all one-step-ahead predictions. Predicted (dashed) trajectories overlap with the true (solid) trajectories. **a-d Right:** True and inferred connectivity from NetFormer's linearized attention matrix or linear regression weight matrix. For systems **c, d**, connectivity is averaged across test set timesteps for visualization. For NetFormer, the inferred connectivity shown is the one whose Spearman correlation ρ is closest to the average ρ across 10 random seeds. Colorbars: scale of off-diagonal entries. Diagonal entries are masked in grey. Inferred connectivity matrices were rescaled by the reciprocal of simulation stepsize for visualization. **e:** True and inferred temporal evolution of four example connections in the nonstationary system **c**. Timesteps used as test set are shaded in grey. **f:** True and inferred temporal evolution in system **d**.

the experimental ground truth: cell-type level postsynaptic potential (PSP) measured using patch-clamp experiments from [18], where stimuli were applied to each patched neuron and postsynaptic responses from other neurons were recorded. Additionally, following the experimental ground truth, we designed the connectivity of a synthetic neuronal population and simulated its activity. On this connectivity-constrained simulation dataset, we assessed the NetFormer's ability to infer both individual neuron-level and cell type-level connectivity. See below and Appendix A.4 for details about both datasets.

Multi-modal in-vivo neural recording: The dataset [19] includes spontaneous population activity recorded from the mouse primary visual cortex (V1) across layers 2 and 3 via two-photon calcium imaging. We trained NetFormer models on data from one animal (SB025), which includes recordings of 2481 neurons. The dataset also provides single-cell spatial transcriptomics data, enabling identification of excitatory and inhibitory neuron classes (Pvalb, Sst, and Vip).

Connectivity-constrained simulation: We generated activity of a synthetic neuron population with 200 neurons whose cell-type level connectivity is defined by results of patch clamp experiments [18], in which the probability and strength of connections between neurons are probed directly. Specifically, the population activity is generated following

$$\boldsymbol{x}_{k+1} = \tanh(\boldsymbol{W}\boldsymbol{x}_k + \boldsymbol{b}) + \boldsymbol{\epsilon}. \tag{3.1}$$

where ϵ is a Gaussian observation noise, b is a constant representing the baseline activity of each neuron, and W describes the neuronal connectivity. In our simulation, 76% of neurons are excitatory, with the remaining 24% being inhibitory. The inhibitory neurons are further subdivided into three cell types (Pvalb, Sst, and Vip) with equal size. To construct W, we first ensured that the connectivity proportion of each cell type pair aligns with the probabilities from [18]. For connected neurons, the connection strength is sampled from $\mathcal{N}(\mu, \sigma)$, where μ is the measured PSP from [18].

Neural dynamics prediction and connectivity inference: We benchmarked NetFormer against multiple methods and models. First, we compared it with linear recurrent model (referred as "linear

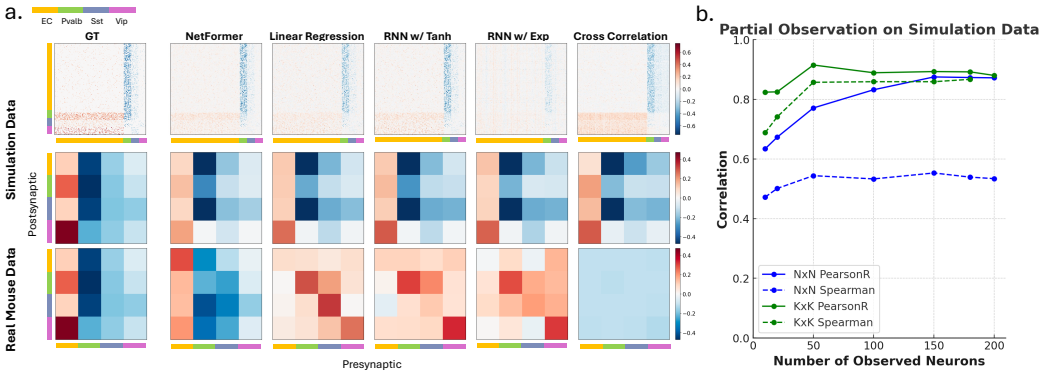

Figure 3: a. Visualization of ground truth and inferred connectivity matrices at both individual-neuron level and cell-type level. NetFormer is benchmarked with linear regression, RNNs with tanh and exponential nonlinearity, and standard statistics metrics in both simulation data and neural data. A positive linear transformation has been applied to standardize all matrices to the same range for better visualization. **b.** Experiment on partial observation with 200 neurons. Connectivity at both neuron-level and cell type-level are evaluated.

regression"): $\boldsymbol{x}_{k+1} = \boldsymbol{W}\boldsymbol{x}_k + \boldsymbol{b}$, where W represents neuronal coupling strengths and b accounts for baseline activity. Next, we compared it with two variants of nonlinear recurrent neural networks (referred as "RNNs"): (i) $\boldsymbol{x}_{k+1} = \tanh(\boldsymbol{W}\boldsymbol{x}_k + \boldsymbol{b})$, which closely matches our connectivity-constrained simulation and serves as an oracle approach to provide an upper bound on performance, (ii) $\boldsymbol{x}_{k+1} = \exp(\boldsymbol{W}\boldsymbol{x}_k + \boldsymbol{b})$, also known as the generalized linear model (GLM) [20], which models the case where the model nonlinearity does not match the one underlying the data. We also considered standard statistical metrics, including cross-correlation, covariance, mutual information, and transfer entropy (details in Appendix A.5), with results in Table 1.

We evaluated activity prediction using MSE, R^2, and Pearson correlation coefficient. We assessed the correlation between inferred and ground truth connectivity using Pearson and Spearman correlation coefficients, both at the $N \times N$ neuron level (N: number of recorded neurons) and the $K \times K$ cell type-level ($K = 4$ includes one excitatory and three inhibitory types: Pvalb, Sst, and Vip). Details on how to aggregate neuron-level connectivity to cell-level connectivity are provided in Appendix A.7.2. Qualitative comparison between the inferred connectivity and ground truth connectivity is shown in Figure 3**a**. All inferred connectivities have been linearly transformed for standardization and better visualization.

On the connectivity-constrained simulation, NetFormer, together with linear regression and cross correlation, performed comparably to the "oracle" model (RNN with tanh nonlinearity) in both neuron-wise and cell type-wise connectivity inference. RNN with exponential nonlinearity performed significantly worse, especially at individual neuron level, underscoring NetFormer's strength in not requiring prior knowledge of specific activation functions. Other statistical metrics such as covariance, mutual information, and transfer entropy all performed significantly worse than the NetFormer.

On the neural data, we only evaluated the inferred cell-type level connectivity, as we do not have access to ground truth connectivity at the level of individual neurons. Our NetFormer model consistently outperformed other methods in both inferring connectivity and predicting neural activity. Interestingly, linear regression and both variants of RNN failed to infer connectivity; we hypothesize that the reason is two-fold: the underlying connectivity is nonstationary rather than static as assumed by these models; the nonlinearity in the dynamics is different from the one used in these models. The statistical metrics were also unable to recover connectivity.

For most real neural systems, it is impossible to access activity of all neurons. To evaluate the robustness of the NetFormer model against such partial observation, in the simulated network, we randomly selected a subset of neurons and trained the NetFormer on their activity. In Figure 3**b**, we show that the performance in recovering the neuron-level connectivity does not significantly decrease with only half of the neurons observed. Moreover, cell-type level connectivity inference is less sensitive to partial observations, highlighting the potential of NetFormer to effectively derive cell-type level connectivity from real neural data.

			NetFormer	linear regression	RNN w/ tanh	RNN w/ exp	cross correlation	covariance	mutual information	transfer entropy
simulation	connectivity N × N	Pearson	**0.869**±0.002	0.817±0.002	0.905±0.000*	0.581±0.011	0.823	-0.029	0.539	0.600
		Spearman	**0.532**±0.001	0.507±0.001	0.546±0.000*	0.393±0.009	0.519	-0.015	0.262	0.339
	connectivity K × K	Pearson	0.879±0.001	0.885±0.001	0.908±0.000*	0.887±0.008	**0.888**	-0.438	0.371	0.419
		Spearman	**0.860**±0.002	0.852±0.005	0.866±0.002*	0.822±0.025	0.732	-0.334	0.018	0.353
in-vivo recording	connectivity K × K	Pearson	**0.777**±0.047	-0.395±0.020	-0.395±0.036	-0.407±0.006	-0.017	-0.162	-0.176	0.075
		Spearman	**0.847**±0.063	-0.409±0.051	-0.343±0.105	-0.191±0.300	-0.080	-0.190	-0.061	0.233
	activity prediction	MSE	**0.404**±0.004	0.443±0.001	0.560±0.001	0.476±0.003	–	–	–	–
		Pearson	**0.740**±0.003	0.720±0.001	0.639±0.000	0.699±0.002	–	–	–	–
		R^2	**0.548**±0.004	0.515±0.001	0.386±0.001	0.478±0.004	–	–	–	–

Table 1: Quantitative results from both connectivity-constrained simulation and in-vivo neural recording. An asterisk (*) indicates that RNN with tanh activation serves as the oracle model to provide an upper bound in the simulation data. The results of connectivity inference using mutual information and transfer entropy are assessed by comparing against the absolute values of the ground truth. Simulation data provides ground truth for neuron-level ($N \times N$) and cell type-level ($K \times K$) connectivity. Patch-clamp results serve as ground truth for real data cell-type connectivity. We assess performance using Spearman's and Pearson's coefficients. Next-step activity prediction on the test set is evaluated with mean squared error, Pearson's coefficient, and R^2.

4 Discussion and Conclusion

Experience and adaptation change the effective connectivity of the underlying neuronal network via mechanisms including synaptic plasticity and neuromodulation, at various time scales. This perspective poses connectivity as a dynamical variable that should be tracked, rather than inferred once. Here, we propose the NetFormer as a light-weighted model for dynamical connectivity inference. We began with a mathematical analysis that relates nonlinear and nonstationary dynamics to its linearized attention mechanism. We further demonstrated, on both simulated and in-vivo neural datasets, the strength of our model through comparison against various baselines.

Acknowledgments

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A Appendix

A.1 Related Work

Dynamical models of neuronal activity: Dynamical models have been a powerful tool for high-dimensional neural data analysis [21]. Generalized linear models (GLMs), known for both interpretability and desirable convexity properties [22], have been widely used to model neuronal population activity as well as inter-neuronal interactions [20]. Nevertheless, unless stacked with an explicit state switching mechanism [23], in GLMs the temporal filters describing interactions among neurons are typically stationary across time [24]. Recurrent neural networks (RNNs) have been a popular alternative [25, 26]; while the connectivity in (trained) RNNs is typically given by a static connectivity matrix "W", variants including long short-term memory networks (LSTMs) [27] and gated recurrent neural networks (GRUs) [28], do include nonstationarities at the level of individual neural units. While this can enhance the model's expressivity and performance in predictive tasks [29, 30], it also introduces challenges for interpretability [10]. Recently, transformer models [31] have been observed to outperform RNNs in various time series forecasting tasks [32, 33], but their deep layered structures and nonlinear attention mechanisms also raise challenges in interpretation with respect to underlying connectivity structures in the orignal data [34, 35], as discussed more below. A closely related approach to the present work is the switching linear dynamical systems [36, 37]. These models have nonstationary connectivity matrices which switch among a number of discrete values according to a Markov process. Nevertheless, in vivo experimental recordings have revealed that cortical activity is more likely to go through a continuum of states instead of discrete switching [38]. This motivates us to propose a model capable of capturing continuous changes in connectivity.

Predicting activity from connectivity: The reverse direction, predicting activity from connectivity, is an allied approach for studying the complexities relating functional and structural information. A prominent line of study have focused on the worm C. elegans as its synaptic connectome was the first available among all species [39]. Using this, generative models of activity have been proposed [40]. Nevertheless, decades of electrophysiological analyses have emphasized the strong additional role of neuromodulators in shaping activity [41, 3]. As a result, the synaptic connectome alone predicts only partial information about recorded population dynamics [1], which directly motivates our study of nonstationary, dynamical connectivity which aims to infer connectivity from functional activity.

Interpretability of the attention mechanism: Attention weights and positional embeddings provide opportunities to understand the inner working of the transformer models. However, the interpretability of these components is a subject of debate. Findings supporting a certain level of interpretability, such as correlation to linguistic features, are common in the literature, with specialized metrics developed to quantify their interpretability [42, 35]. However, caution should be taken when equating attention with explanation [34], considering the lack of identifiability [43] and the wide variety of underlying architectures and implementations [44]. In this work, we seek to avoid these confounding aspects by focusing on the linearized attention mechanism [12].

A.2 Justification for linearized attention applied to "leaky" systems (Eqn 2.6)

Using the forward Euler method and step size δ, Equation 2.6 can be simulated as

$$\boldsymbol{x}_{k+1} = \boldsymbol{x}_k + \delta\Big(- \boldsymbol{x}_k + f(\boldsymbol{W}_k \boldsymbol{x}_k)\Big) = \boldsymbol{x}_k - \delta \boldsymbol{x}_k + \delta f(\boldsymbol{W}_k \boldsymbol{x}_k). \tag{A.1}$$

Following the same sigmoidal assumption on f, Equation A.1 can be written as

$$\boldsymbol{x}_{k+1} = \boldsymbol{x}_k + \delta(f'(0)\boldsymbol{W}_k - \boldsymbol{I})\boldsymbol{x}_k + \delta O(\boldsymbol{x}_k^3), \tag{A.2}$$

where $\boldsymbol{I}$ is the $N \times N$ identity matrix. Therefore, the linearized attention matrix $\boldsymbol{A}_k$ learned from Equation 2.3 may reflect the true interactions $\boldsymbol{W}_k$ by approximating $\delta(f'(0)\boldsymbol{W}_k - \boldsymbol{I})$, and can capture the interactions between different variables (off-diagonal entries of $\boldsymbol{W}_k$) up to a scaling factor $(\delta f'(0))$.

A.3 Additional details for nonlinear and nonstationary systems simulation (Sec ??)

A.3.1 Simulation details

In Figure 2**a,b**, ground-truth W were generated randomly, with real-part of each eigenvalue clipped at 0 to ensure stability of the system. W in **a,b** were also used as W_0 in **c,d**, respectively. ω in **c,d** were

picked randomly while maintaining stability of the system. In **a**, the system trajectory was simulated using the closed-form solution $x(t) = e^{Wt}\eta$. In **b-d**, trajectories were simulated using the forward Euler method: $x_{k+1} = x_k + \delta f(W_k x_k)$, where $W_k \equiv W$ for **b**, and $W_k = W_0 + x_k \omega^\top$ for **c, d**. All simulations consist of 3000 timesteps with stepsize $\delta = 0.01$, with the first 80% used as training set, and last 20% as test set. Time-averaged ground-truth across test set timesteps $\bar{W} = \sum_{k=2400}^{3000} W_k$ for **c, d**. Simulated trajectories are visualized in Figure 4. In all settings, the NetFormer model was trained to minimize the mean squared error on the trainining set for 1100 epochs using the Adam optimizer in Pytorch, with $T = 1, H = 5$, batch size = 80, initial learning rate = 0.01. In **b, d**, learning rate was decayed by a factor of 0.9 every 100 epochs. In **c**, learning rate was decayed by a factor of 0.8 every 100 epochs.

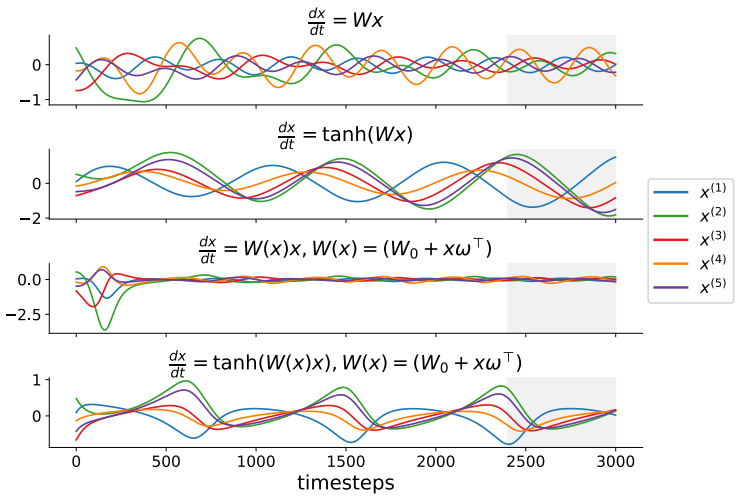

Figure 4: Simulated trajectories of toy models in Figure 2. Shaded regions represent timesteps used as test set.

A.3.2 Quantitive comparsion with linear regressoin model

For each toy system, we trained 10 NetFormer models with different random initializations, and computed the Spearman's rank correlation coefficient (ρ) and the Pearson correlation coefficient (r) between the off-diagonal entries of $\bar{A}$ and $\bar{W}$ for each trained model. In terms of ρ, $\bar{A}$ achieved comparable performance as A_{OLS} in systems **(a) (b)** ($p > 0.3$, two-sided one sample t test), but significantly outperformed A_{OLS} in systems **(c) (d)** ($p < 10^{-8}$) (figure5 left). Similar observations can be made with r (figure5 right). For each system, the attention matrix visualized in figure2 is the one whose ρ is the closet to the average ρ across 10 random initializations.

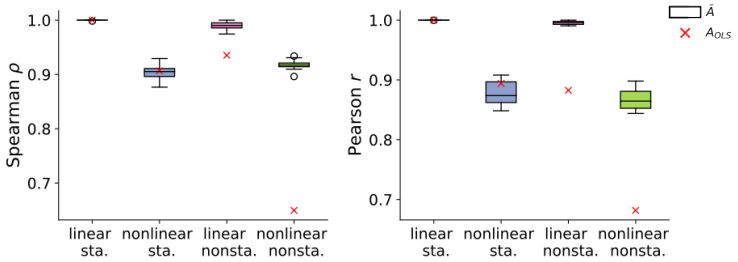

Figure 5: Comparison between A_{OLS} (red cross) and $\bar{A}$ from NetFormer models with 10 different random initializations (boxplots).

A.3.3 Nonstationarity connectivity tracking

On toy systems with nonstationary connectivity (Figure 2c, d), we evaluated how well linearized attention matrices across timesteps can track changes in the connectivity. For each pair (i, j), $i, j =$

$1, \ldots, 5, i \neq j$, we collected A_{ij} and W_{ij} across all test timesteps, resulting in two time-varying series $A_{ij}(t)$ and $W_{ij}(t)$, and computed the Pearson correlation coefficient between them. Results for 10 trained NetFormer models with different random seeds are shown in Figure 6. Distributions of the temporal correlation coefficients for all off-diagonal pairs (i, j) are shown as violin plots, where each violin corresponds to model trained with one random seed. The median of each distribution is marked with a black line. All medians are greater than 0.999.

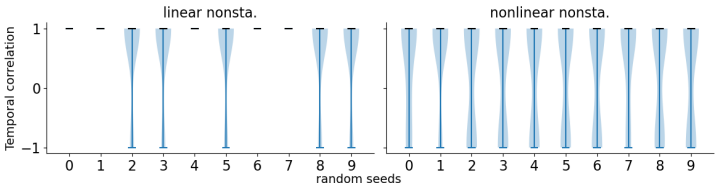

Figure 6: Distribution of test set temporal correlation between the linearized attention matrix and the true nonstationary connectivity. Each column shows result from NetFormer model with a different random seed. Median of each distribution is marked in black. All medians are greater than 0.999.

A.3.4 Further discussion on nonlinear dynamical systems

In section 2, we showed that when f is sigmoidal, A can reflect W through Taylor series approximation of $f(Wx_k)$. Take $f = \tanh$ as an example. When $|\vec{w}_i^\top x^k| < \frac{\pi}{2}\ \forall i = 1, \ldots, N$,

$$\tanh(Wx) = \tanh(0) + \tanh'(0)Wx + O(x^3).$$

As $\tanh(0) = 0$, the forward Euler method is

$$x_{k+1} = x_k + \delta \tanh(Wx_k) = x_k + \delta \tanh'(0)Wx_k + \delta O(x_k^3).$$

This analysis also applies to other sigmoidal functions f, such as $\arctan$, with

$$f(0) = 0, f(x) = f'(0)x + O(x^3) \text{ for } x \text{ within some interval around } 0.$$

Therefore, we hypothesize that A can capture W through learning $\delta f'(0)W$ for sigmoidal f. It is also clear that learning W becomes more challenging when $\vec{w}_i^\top x$ does not always stay within the radius of convergence of the Maclaurin series. Nonetheless, we note that if some $\vec{w}_i^\top x$ is constantly outside the convergence region, $f(\vec{w}_i^\top x)$ will be constantly positive or negative, and the system will either blow up or decay to zero. Therefore, for the systems of interest here, which are those with interesting persistent dynamics, from time to time $\vec{w}_i^\top x$ must fall within the convergence region where the Maclaurin series representation is valid. That being said, while A may still be able to capture some aspect of W, it could become less accurate, and may require more observations of the system to gather sufficient timestamps within the convergence region.

In the example nonlinear dynamical system shown in figure 2**b**, $\vec{w}_i^\top x^k$ stays within the radius of convergence of $\tanh$ for all i and k, which makes the Maclaurin series approximation valid for all timesteps. In figure 7, we provide another toy model example showing that the attention from NetFormer still bears considerable similarity to the ground-truth W even when $\vec{w}_i^\top x^k$ falls out of the convergence region for some i and k.

A.4 Connectivity-constrained simulation and neural data: Datasets and preprocessing

A.4.1 Connectivity-constrained simulation

We used the following procedure to construct the ground-truth connectivity matrix. For each cell-type pair and for every pair of neurons, we first drew a random sample from the uniform distribution between 0 and 1. Then, we used the connectivity probability from patch-clamp experiments [18] as a cutoff threshold to determine if two neurons are connected. For connected neurons, we sampled their connection strength from a normal distribuion $\mathcal{N}(\mu, 0.1)$, where μ is the measured post-synaptic potential from patch-clamp experiments. We simulated $30,000$ steps for 200 neurons, using the first 80% timesteps for training and the last 20% for testing.

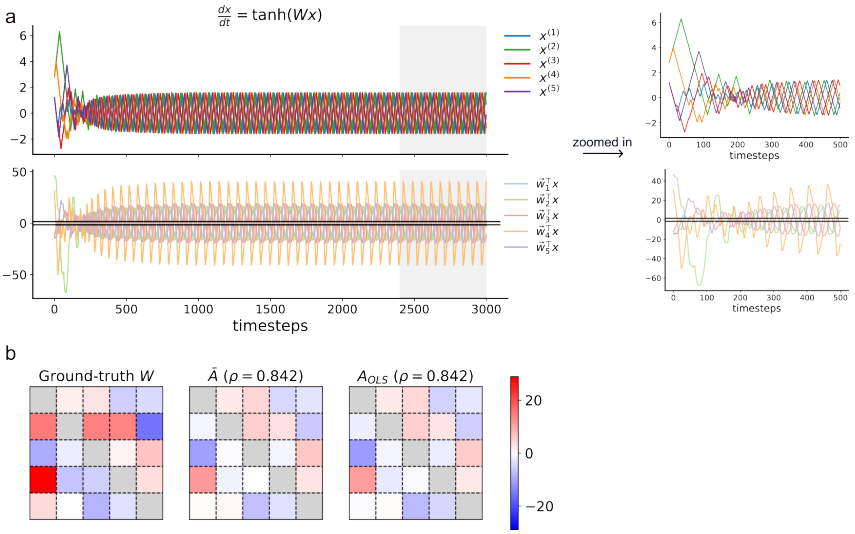

Figure 7: Demonstration of NetFormer on a nonlinear system $\frac{dx}{dt} = \tanh(Wx)$ where $\vec{w}_i^\top x^k$ does not always stay within the convergence region of the Maclaurin series of $\tanh$. **a. Top row:** Trajectories of the simulated system. Simulation was done using the forward Euler method with stepsize $\delta = 0.1$. Shaded regions represent timesteps used as test set. **Bottom row:** Visualization of $\vec{w}_i^\top x$ across simulated timesteps. Boundaries of the convergence region, $\pm\frac{\pi}{2}$, were marked with black horizontal lines. The right column provides a zoomed-in view of the first 500 simulation timesteps. **b. Left to right** Ground-truth W, average linearized attention matrix across test timesteps from NetFormer ($\bar{A}$), A_{OLS} fitted through least-squares regression. Colorbars indicate the scale of the off-diagonal entries, and the diagonal entries are masked in grey. $\bar{A}$, A_{OLS} were rescaled for visualization. Spearman's rank correlation coefficients (ρ) were computed between the off-diagonal entries of $\bar{A}$ or A_{OLS} and W. We trained 10 NetFormer models with different random initializations ($\rho = 0.841 \pm 0.02$, mean $\pm$ std), and $\bar{A}$ shown is the one whose ρ is the closet to the average ρ across 10 random initializations. NetFormer models achieved similar performance as A_{OLS} ($p = 0.9$, two-sided one sample t test). All NetFormer models were trained to minimize the mean squared error on the trainining set for 600 epochs using the Adam optimizer in Pytorch, with $T = 1, H = 5$, batch size = 80. Learning rate was initialized to 0.01, and was decayed by a factor of 0.9 every 100 epochs.

A.4.2 Patch-clamp dataset

The dataset released in [18] contains experimental results of connectivity probability and connectivity strength (Postsynaptic Potential (PSP)) at the cell-type level measured using patch-clamp. In each experiment, up to eight neurons were simultaneously subjected to whole-cell patch-clamp recording, mainly under current-clamp conditions, with some stimuli also tested under voltage-clamp conditions. Stimuli were applied to each patched neuron while recording the other neurons for postsynaptic responses. We mainly focus on the experimental results for layers 2/3 in mouse primary visual cortext (V1), to match the neurons recorded in the multimodal mouse datatset [19].

A.4.3 Multimodal mouse data

For functional activity recordings from neuronal populations, we used a recent, public multimodal dataset provided by [19]. This dataset includes spontaneous population activity recordings from the mouse primary visual cortex (V1) across layers 2/3 via 2-photon calcium imaging at a temporal sampling frequency of 4.3Hz across six 20-minute sessions, recording approximately 500 neurons per session. Spatial coordinates of the recorded neurons are also provided. We trained our models on data from one experimental subject (SB025), which includes recordings of 2481 neurons, with some neurons repeating across six sessions. The dataset also includes single-cell spatial transcriptomics, profiling mRNA expression for 72 selected genes to identify excitatory and inhibitory class labels of neurons. 51% of neurons in the inhibotiry class can further be identified to be one of Lamp5, Pvalb, Vip, Sncg, and Sst.

A.4.4 Data preprocessing

In the connectivity-constrained simulation, when using RNN with an exponential activation, we rescaled the data to ensure that all neuronal activities are nonnegative, as exponential activation produces only nonnegative outputs.

For the experimental neural recording, which is nonnegative, we normalized it using the mean and standard deviation calculated across all sessions and neurons involved in training. When using the RNN model with exponential activation, we normalized the data by dividing by the standard deviation only, without first subtracting the mean.

A.5 Baselines

Linear Regression: We denote neural activity data as $X \in \mathbb{R}^{N \times T}$ recorded from N neurons and T time steps. Let $x_{k+1} \in \mathbb{R}^N$ denote the neuronal activity at the $(k+1)$th time step. Given previous 1 time step, x_k, linear regression predicts current time step activity as

$$\hat{x}_{k+1} = W x_k + b$$

Recurrent Neural Network (RNN) with tanh activation: Given neuronal activity across previous p time steps, $x_k, x_{k-1}, \ldots, x_{k-p+1}$, a RNN with predefined Tanh activation function predicts current time step activity as

$$\hat{x}_{k+1} = \sigma\left(W^{(0)} x_k + W^{(1)} x_{k-1} + \cdots + W^{(p-1)} x_{k-p+1} + b\right), \sigma = \tanh$$

where $W^{(l)}, l \in \{0, 1, \ldots, p-1\}$, represent how the previous l-th step affects the current step activity and each element $W_{ij}^{(l)}$ represents how the j-th neuron at the previous l-th time step influences the ith neuron in current step. The RNN is trained by minimizing mean squared errors (MSE) of the current time step activity prediction given previous time steps. $p = 1$ is commonly used for RNN. For modeling both simulation data and real mouse data, we chose $p = 1$, because the simulation data has exactly one timestep dependency. Using larger p did not improve performance in real data either.

Recurrent Neural Network (RNN) with exponential activation: Next, we change the predefined activation function of RNN to exponential function for modeling both simulation data and real mouse data.

$$\hat{x}_{k+1} = \sigma\left(W^{(0)} x_k + W^{(1)} x_{k-1} + \cdots + W^{(p-1)} x_{k-p+1} + b\right), \sigma = \exp$$

Cross correlation: Recall that $X_k = [x_{k-T+1} \quad \cdots \quad x_k] \in \mathbb{R}^{N \times T}$ denotes activity of N neurons across T time steps. Let $x^{(i)}, x^{(j)} \in \mathbb{R}^T$ denote the i-th and j-th neurons' activity across T time steps. For simplicity, let $a = x^{(i)}[\tau :], b = x^{(j)}[: -\tau]$. Cross correlation with time delay τ reflects connectivity as

$$r^{i \leftarrow j} = \frac{a^\top b}{\|a - \bar{a}\| \|b - \bar{b}\|}$$

We choose $\tau = 1$ for inferring connectivity in both simulation and read data.

Covariance: Similar to above, let $x^{(i)}, x^{(j)} \in \mathbb{R}^T$ denote the i-th and j-th neurons' activity across T time steps. Covariance indicates the level to which two variables vary together. Covariance matrix is symmetric, which assumes that the influence from neuron i to neuron j is the same as influence from neuron j to neuron i. Covariance between neuron i and j is defined as

$$c^{i \leftarrow j} = c^{j \leftarrow i} = \frac{1}{T-1} \Sigma_{k=1}^{T} x_k^{(i)} x_k^{(j)}$$

Mutual information: Mutual information quantifies the amount of information that one random variable contains about another, which is also symmetric. When calculating the mutual information between activity history of two neurons, the computation involves estimating the entropy of each neuron's activity individually and the joint entropy of both neurons together. We used the Python package PyInform.mutualinfo to compute the mutual information. Let $x^{(i)}, x^{(j)} \in \mathbb{R}^T$ as defined above, then

$$I^{i \leftarrow j} = I^{j \leftarrow i} = I(x^{(i)}; x^{(j)}) = H(x^{(i)}) + H(x^{(j)}) - H(x^{(i)}, x^{(j)}),$$

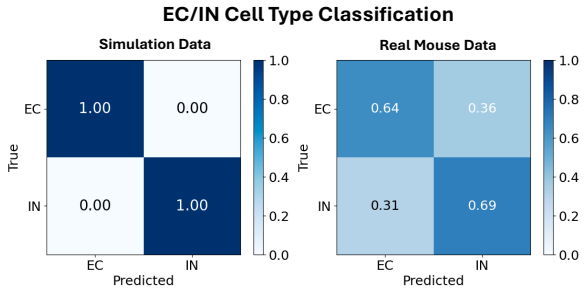

Figure 8: Confusion matrices of Excitatory/Inhibitory cell type classification using the learnable neuronal embedding from NetFormer on both connectivity-constrained simulation and real mouse data. The classifier is logistic regression. For real data, all neurons in one session are classified to be Excitatory or Inhibitory neurons.

where $H(x^{(i)})$ is the entropy of neuron i's activity, calculated as $H(x^{(i)}) = -\sum_{z \in x^{(i)}} p(z) \log p(z)$. $H(x^{(j)})$ is the entropy of neuron j's activity. $H(x^{(i)}, x^{(j)})$ is the joint entropy of neurons i and j, calculated as $H(x^{(i)}, x^{(j)}) = -\sum_{z \in x^{(i)}, \xi \in x^{(j)}} p(z, \xi) \log p(z, \xi)$.

Transfer entropy: Transfer entropy quantifies the amount of directed information transferred between systems, or in our case, between two neurons. We use python package PyInform.transferentropy to compute the transfer entropy, which is defined as

$$T^{i \leftarrow j} = \sum p\left(x_{k+1}^{(i)}, x_{(k+1-p):k}^{(i)}, x_{(k+1-l):k}^{(j)}\right) \log \left(\frac{p\left(x_{k+1}^{(i)} \mid x_{(k+1-p):k}^{(i)}, x_{(k+1-l):k}^{(j)}\right)}{p\left(x_{k+1}^{(i)} \mid x_{(k+1-p):k}^{(i)}\right)} \right),$$

where $x_{k+1}^{(i)}$ is the future activity of neuron i. $x_{(k+1-p):k}^{(i)}$ represents the past p activities of neuron i up to time k. $x_{(k+1-l):k}^{(j)}$ denotes the past l activities of neuron j up to time k. $p(\cdot)$ denotes the probability distributions calculated from the joint and conditional activities as observed in the data.

A.6 Neuronal identity information

We demonstrate the learned positional embeddings E for each neuron, as in [45]. We train a logistic regression for binary classification using embeddings as features for neurons in the training set. We classify unseen neurons in the test set as excitatory/inhibitory neurons, with 100% top-1 accuracy in simulation data, 71.21% top-1 accuracy and AUROC score of 0.700 in real mouse data (confusion matrixes in Figure 8). This shows that excitatory and inhibitory cell types are learned in a linearly separable way using the positional embeddings in the NetFormer.

A.7 Implementaion Details

A.7.1 Model framework for fitting connectivity-constrained simulation and real mouse data

Following Section 2, we train the NetFormer to predict x_{k+1} based on $X_k = [x_{k-T+1} \quad \cdots \quad x_k] \in \mathbb{R}^{N \times T}$. To encode neuron identities, a learnable positional embedding matrix $E \in \mathbb{R}^{N \times H}$ is concatenated to X, giving $\tilde{X}_k = [X_k \quad E] \in \mathbb{R}^{N \times (T+H)}$. The queries Q_k and keys K_k are obtained through linear transformations of $\tilde{X}_k$, $Q_k = \tilde{X}_k W_Q \in \mathbb{R}^{N \times D}$, and $K_k = \tilde{X}_k W_K \in \mathbb{R}^{N \times D}$. NetFormer model is trained to predict the next time-step activity x_{k+1}, defined as

$$\hat{x}_{k+1} = A_k x_k + x_k = \phi(\frac{Q_k K_k^T}{\sqrt{D}}) x_k + x_k = \frac{1}{\sqrt{D}} (\tilde{X}_k W_Q)(W_K^\top \tilde{X}_k^\top) x_k + x_k,$$

where A_k is the self-attention that we want to use for inferring connectivity, ϕ is the attention activation. In the standard Transformer model [31], softmax is used as the attention activation function, but here we set ϕ equal to identity for better interpretability. In fact, we experimented with different activation functions and empirically found that the identity activation yields the best results on recordings from the mouse cortex.

Although not used in the current experiments, it is possible to use an additional linear transformation on X_k to accommodate neuronal dynamics that can depend on multiple previous timesteps, that is,

$$\hat{x}_{k+1} = A_k(X_k w_{out}) + X_k w_{out}, w_{out} \in \mathbb{R}^{T\times 1}.$$

A.7.2 NetFormer training and evaluation

We first assign each unique neuron in all sessions an ID, which is later used to track positional embedding for each unique neuron, because same neuron can be recorded in more than one session. Then, within each session, we construct samples with window size 200 in simulation and 60 in real data, and we make sure samples in one batch should come from the same session so that the dimensions can match.

We use the first 80% time-steps in all sessions for training and the last 20% time-steps for validation. The model is trained using MSE as the loss function, comparing the predicted activity for the next time step with the ground-truth activity. We employ early stopping criteria, ceasing training if there are 20 epochs without improvement, with a hard limit of 100 epochs maximum.

After training is complete, we calculate the attention for each sample in the dataset. For each session, we aggregate the attentions from all samples to compute a single averaged attention. Averaged attentions from all sessions are then transformed into a final cell-type level attention. We achieve this by aggregating attention values according to their corresponding presynaptic and postsynaptic cell types and dividing by the total count of such pairings.

We also extract positional embeddings from the model and utilize each neuron's unique ID to determine the neuronal embedding for every unique neuron. These embeddings are then used as features for logistic regression to classify neurons as either excitatory or inhibitory.

For evaluation, we assess the inferred cell-type level connectivity against the Postsynaptic Potential (PSP) resting state amplitude obtained from patch-clamp experiments, which serves as the experimental ground-truth. Additionally, we evaluate the accuracy of the binary cell-type classification using experimental data from single-cell spatial transcriptomics, which provides a classification of neurons into excitatory and inhibitory types across all sessions.

A.7.3 Evaluation Metircs

We use python libraries and built-in functions for computing evaluation metrics.

For connectivity inference, we flatten the inferred 2-dimensional $N \times N$ or $K \times K$ connectivity matrix and grond-truth matrix.
Pearson correlation: scipy.stats.pearsonr()
Spearman rank correlation: scipy.stats.spearmanr().

For activity prediction, given the input matrix $\in \mathbb{R}^{B\times N\times T}$ for NetFormer and input matrix $\in \mathbb{R}^{B\times N}$ for RNN, where B is the batch size, NetFormer outputs $\in \mathbb{R}^{B\times N\times 1}$ and RNN outputs $\in \mathbb{R}^{B\times N}$. We flatten the predicted activity and the grond-truth.
MSE: torch.nn.functional.mse_loss()
Pearson correlation: scipy.stats.pearsonr()
$\mathbf{R^2}$ **:** sklearn.metrics.r2_score()

For binary classification, classifier predicts the probability for all neurons.
Top-1 accuracy: sklearn.metrics.accuracy_score()
Area Under the Receiver Operating Characteristic (AUROC): sklearn.metrics.roc_auc_score()

A.7.4 Hyperparameters

In connectivity-constrained simulation data, for training NerFormer, we use window size 100, embedding size 200, hidden dimension of query and key matrices is 300, learning rate 10^{-3}, and batch size 32. For training RNN, we use $p = 1$, batch size 32, and learning rate 10^{-3}.

In real data, for training NetFormer, we use window size 60, embedding size 30, hidden dimension of query and key matrices 90, learning rate 10^{-3}, and batch size 32. For training RNN, we use $p = 1$, batch size 32, and learning rate 10^{-4}.

We use PyTorch [46] and PyTorch Lightning [47] for model development and training, and Adam as the optimizer.

A.7.5 Pseudo Code

We train NetFormer and extract attentions and positional embeddings for connectivity inference and binary cell-type classification. The pseudo code for model training , connectivity inference and cell-type classification is provided as follows:

```
NetFormer(x, neuron_ids):
    if constraint == True:
        cell_type_level_mean = parameters(num_cell_type, num_cell_type)
        cell_type_level_var = parameters(num_cell_type, num_cell_type)

    embeddings = embedding_table(neuron_ids)
    input = layer_norm(concat(x, embeddings))
    x, embeddings = input[:, :, :T], input[:, :, T:]

    dim_x, dim_e = x.shape[-1], embeddings.shape[-1]
    scale = (dim_x + dim_e) ** -0.5

    logits = input @ W_Q_W_KT @ input.T
    logits = logits * scale

    if activation == softmax:
            attention = softmax(logits)
        elif activation == sigmoid:
            attention = sigmoid(logits)
        elif activation == tanh:
            attention = tanh(logits)
        elif activation == none:
            attention = logits

    output = layer_norm(attention @ x + x)

    if out_layer == True:
        # linear_out is a lienar transformation from dimension T to 1
        output = linear_out(output)
        return output, attention
    else:
        # Use the last column as prediction
        return output[:, :, -1], attention


NetFormer_Training(all_samples):
    all_inputs, all_neuron_ids, all_GT_targets = all_samples
    model = NetFormer()
    optimizer = Adam(model, learning_rate)

    all_predictions, all_attentions = model(all_inputs, all_neuron_ids)

    prediction_loss = MSE(all_predictions, all_GT_targets)
    loss = prediction_loss

    optimizer.zero_grad()
    loss.backward()
    optimizer.step()


Connectivity_Inference(all_samples, trained_NetFormer, GT_connectivity):
```

```
    all_inputs, all_neuron_ids, all_GT_targets = all_samples
    all_predictions, all_attentions = trained_NetFormer(all_inputs, all_neuron_ids)

    avg_attention = mean(all_attentions, axis=0)

    pearson_corr = pearsonr(GT_connectivity, avg_attention)
    spearman_corr = spearmanr(GT_connectivity, avg_attention)


Cell_Type_Classification(trained_NetFormer, neuron_ids, cell_types):
    embeddings = trained_NetFormer.embedding_table(neuron_ids)

    X_train = embeddings[TRAIN_idx]
    y_train = cell_types[TRAIN_idx]
    X_test = embeddings[TEST_idx]
    y_test = cell_types[TEST_idx]

    # Train classifier
    classifier = LogisticRegression.fit(X_train, y_train)
    # Test on test set
    y_pred = classifier.predict(X_test)
```

A.8 Compute Resources

Model training on simulated systems in 2 was done on a MacBook Pro with Apple M1 chip. Using the NVIDIA A100 GPU, NetFormer model trained on connectivity-constrained simulation data took about 10min. NetFormer model trained on one mouse (SB025) in real mouse data took about 20min, which requires at least 60 GB of RAM and 16 GB of GPU memory.

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