Cross-Quality Few-Shot Transfer for Alloy Yield Strength Prediction: A New Material Science Benchmark and An Integrated Optimization Framework

Abstract

Discovering high-entropy alloys (HEAs) with high yield strength is an important yet challenging task in material science. However, the yield strength can only be accurately measured by very expensive and time-consuming real-world experiments, hence cannot be acquired at scale. Learning-based methods could facilitate the discovery process, but the lack of a comprehensive dataset on HEA yield strength has created barriers. We present **X-Yield**, a large-scale material science benchmark with 240 experimentally measured ("high-quality") and over 100K simulated (imperfect or "low-quality") HEA yield strength annotations. Due to the scarcity of experimental annotations and the quality gap in imperfectly simulated data, existing transfer learning methods cannot generalize well on our dataset. We address this *cross-quality few-shot transfer* problem by leveraging model sparsification "twice" — as a noise-robust feature learning regularizer at the pre-training stage, and as a data-efficient learning regularizer at the few-shot transfer stage. We then propose a bi-level optimization framework termed **Bi-RPT** that jointly learns optimal masks and automatically allocates sparsity levels for both stages. The effectiveness of Bi-RPT is validated through extensive experiments on our new challenging X-Yield dataset, alongside other synthesized testbeds. Specifically, we achieve an 8.9-19.8% reduction in terms of the test MSE and 0.98-1.53% in terms of test accuracy, merely using 5-10% of the experimental data.

1 Introduction

Machine learning (ML) methods have recently demonstrated great promise in the important field of material science, and in this paper, we focus on ML-assisted high-entropy alloy (HEA) (Yeh et al., 2004) discovery and property prediction. HEAs own promising properties that traditional alloys do not hold, making them well-suited options for various material applications.

The yield strength, which characterizes the maximum stress a material can endure before starting to deform, is a critical parameter for customized HEA design. However, in order to accurately measure the yield strength of specific HEAs, expensive and time-consuming experiments have to be conducted, which can take two to four weeks even for a domain expert team. Therefore, it is challenging to acquire yield strength measurements from those "high-quality" experiments at scale. Recent efforts try to mitigate the scarcity of real-world measurements using ML-based predictors by predicting the yield strengths (Bhandari et al., 2021a). While they can be trained with rich simulated data, they are often compromised by the domain gap between the simulated and the "ground-truth" experimental data, due to many simplifications in simulation modeling. The lack of public datasets in this field also renders it difficult to gauge the process of ML models.

In this paper, we curate a large-scale benchmark, called **X-Yield**, that combines existing experimental data with new simulation data to address the problem of predicting yield strength in HEAs. The former were carefully screened and curated from an open-source material database (Borg et al., 2020) by domain experts while the latter were predicted by an theoretical yield strength model (Maresca & Curtin, 2020). While using experimental data is always preferred since they are *"high-quality"* ground truths, it is impractical to generate high quantities of them, especially for capturing yield strength at elevated temperatures. Thus, simulation data can be acquired by massive quantities to fill the gap, despite their relatively *"low quality"* due to inherent model misspecifi-

cation or simplification. To our best knowledge, this is the first multi-fidelity dataset in the public domain that combines real experimental measurements and large quantities (over 100K) of simulation data for mechanical property prediction in HEAs. This specialized dataset should be able to predict high-temperature yield strength across a broad range of HEAs.

Since learning from such a multi-fidelity dataset is highly non-trivial, we conceptualize a **cross-quality few-shot transfer workflow**: first pre-training the prediction model on the source domain (simulated data), and then fine-tuning the model towards the target domain (experimental data). However, this vanilla workflow is challenged by two issues: a significant quality gap between source and target domains, and an extreme data scarcity of target data. Inspired by the recent success of sparsity regularizers, we propose to incorporate sparsity to regularize both stages: sparsifying pre-training to improve the robustness and cross-domain transferability of learned features (Chen et al., 2022; Sehwag et al., 2020), and sparsifying fine-tuning to overcome data shortfalls (Liu et al., 2020; Chen et al., 2021; Tao et al., 2022). Proof-of-concept experiments show that even a simple magnitude-based pruning could play effective regularization roles in our workflow. Moreover, to avoid the ad-hoc two-step pruning as well as trial-and-error sparsity ratio selection at either stage, we propose a novel integrated optimization framework termed *Bi-Level Regularized Pre-training and Transfer* (**Bi-RPT**), that jointly learns optimal sparse masks and allocates sparsity levels for both stages. Extensive experiments show that Bi-RPT can boost performance on the *X-Yield* benchmark alongside other synthesized testbeds. In particular, for the regression/classification task, we achieve a reduction of 8.9-19.8%/0.98-1.53% in the test MSE/accuracy, merely using 5-10% of the available experimental data.

2 RELATED WORK

ML has been applied to solve a wide range of problems in materials science, with the typical purposes to predict materials properties and accelerate simulations (Pilania, 2021). Deep learning has been successfully applied to problems in the field of HEAs, in particular to predict phase formation (Lee et al., 2021b; Zhu et al., 2022). These approaches provide significant increases in speed compared to phase predictions with methods (Saunders & Miodownik, 1998; Parr, 1983; Shuichi, 1991) commonly used in materials science. When it comes specifically to the yield strength of HEAs, its prediction has also been previously explored with deep learning (Liu et al., 2023; Bhandari et al., 2021a). However, a majority of these efforts are restricted to specific alloys (Zheng et al., 2021; Bhandari et al., 2021b) or solely of transition metals (Wen et al., 2019), and many studies also only use a small experimental dataset for prediction (Wen et al., 2021). A generalized multi-fidelity ML model to predict yield HEA strength at scale remains absent yet highly demanded.

Sparsity or pruning was traditionally treated as a mainstream model compression approach in deep learning (Han et al., 2015), yet recently has been used to enhance deep model robustness to various noise, malicious attacks, and distribution shifts. Guo et al. (2018); Sehwag et al. (2019); Gui et al. (2019) studied the intrinsic relationship between pruning and adversarial robustness. Diffenderfer et al. (2021) comprehensively demonstrated the benefit of model sparsification to improve robustness to distributional shifts (Hendrycks & Dietterich, 2019; Bulusu et al., 2020). Sparse regularizers also exhibit promise in improving data efficiency: Zheng et al. (2019); Liu et al. (2020); Tian et al. (2020) used sparsity to improve few-shot performance. They have even found effective beyond few-shot image classification, *e.g.*, enhancing the data efficiency in image generation (Chen et al., 2021).

3 X-YIELD: A NEW BENCHMARK FOR HEA YIELD STRENGTH PREDICTION

We focuses on the sub-field of refractory HEAs (RHEAs) which have been shown to have excellent mechanical properties at high temperatures (Li et al., 2020). We develop **X-Yield**, a multi-fidelity dataset consisting of over 100K low-quality simulated points and 240 experimental data points to explore the RHEA design space. From X-Yield, a multi-fidelity ML model is expected to be trained to predict high-temperature yield strength for a broad palette of RHEAs. The combination of high-temperature yield strengths from the simulated dataset and experimental input can generate an ML model to accurately and efficiently predict high-temperature yield strengths of alloys not included in the training set. More details on X-Yield can be found in Sec. C.1.

Dataset Construction. The yield strength of the simulation data were predicted using the analytic and parameter-free mechanistic yield strength model developed by Maresca & Curtin (2020). This model describes body-centered cubic (BCC) multi-principal element alloy (MPEA) solid solution strengthening associated with edge dislocations, in terms of elemental atomic volumes and elastic moduli. The yield strength was predicted for all ternary (1% increments), quaternary (1% incre-

ments), quinary (5% increments), senary (5% increments), and septenary (5% increments) alloys from the Al-Cr-Fe-Hf-Mo-Nb-Ta-Ti-V-W-Zr element family at temperatures between 300K-2500K in increments of 100K. This resulted in over three billion data points of which approximately 100K were randomly selected for inclusion. Note that even this advanced simulation model suffers from notable oversimplification and data quality issues. For example, The phase stability and dislocation character were not used to filter alloys in the study and the model may overpredict the yield strength of alloys with non-BCC phases and underpredict the yield strength of alloys with different dislocation characters, *e.g.* screw.

The high-quality experimental data were carefully filtered and curated from the database generated by Borg et al. (2020) consisting of mechanical property information for MPEAs. We excluded alloys with crystal structures such as face-centered cubic (FCC) and hexagonal close-packed (HCP), and only considered data points with solely BCC phases, consisted of elements from the above element family, at temperature above 20 °C, and contained a yield strength value.

4 CROSS-QUALITY FEW-SHOT TRANSFER: A TWO-STAGE WORKFLOW AIDED BY SPARSITY (TWICE)

Basic Two-Stage Workflow: Pre-training then Fine-tuning. Let us denote the high-quality target domain (experimental data) by $\mathcal{D}_t$, and the low-quality source domain (simulated data) by $\mathcal{D}_s$. Our goal is to learn a generalizable predictor over $\mathcal{D}_t$ while leveraging $\mathcal{D}_s$. Due to the large domain gap between $\mathcal{D}_s$ and $\mathcal{D}_t$, as well as the sample scarcity in $\mathcal{D}_t$, simply combining the two data domains and jointly training a supervised model works poorly on $\mathcal{D}_t$. Instead, we propose to formulate our workflow as a two-stage pipeline: first pre-training a model on $\mathcal{D}_s$, and then fine-tuning over $\mathcal{D}_t$.

Incorporating Bi-Stage Sparsity: A Vanilla Approach. Inspired by the recent success of sparse regularizers in improving both robustness/transferability and data efficiency, we attempt to incorporate sparsity into both stages to address the two-fold challenges. We first prove our concepts by a vanilla approach called *Hand-Tune*. Starting from pre-training on $\mathcal{D}_s$, we perform the standard iterative magnitude pruning (IMP) (Frankle & Carbin, 2019). In particular, we alternate between (re-)training and pruning; each time, we prune the 20% smallest-magnitude weights from non-zero weights and continue (re-)training the remaining non-zero weights. We repeat such a procedure for N_s rounds to get the sparse mask $\boldsymbol{m}_s$ (1 denotes the element to be non-zero and 0 to be pruned) associated with the pretrained weights. Subsequently, we conduct IMP in fine-tuning for N_t rounds on the subset of current non-zero weights, yielding another sparse mask $\boldsymbol{m}_t$. The final model uses the joint sparse mask $\boldsymbol{m}_s \odot \boldsymbol{m}_t$ where $\odot$ represents the point-wise product. Such a simple pipeline suffices to achieve good performance with properly tuned N_s and N_t (see Sec. B.3).

Principled Bi-Stage Sparsity Integration with Bi-RPT. *Hand-Tune* has some apparent flaws: (1) it removes weights by merely using their magnitude, which is not explicitly task-driven; (2) $\boldsymbol{m}_s$ and $\boldsymbol{m}_t$ are decided in a sequential manner, so learning $\boldsymbol{m}_t$ will suffer from any artifact in learning $\boldsymbol{m}_s$; (3) the sparsity ratios assigned in both stages, as controlled by N_s and N_t, need to be manually tuned, without any obvious insight beyond exhaustive hyperparameter search.

We, therefore, devise a more principled framework that can jointly learn the optimal sparse masks as well as sparsity allocations for both stages, termed *Bi-Level Regularized Pre-training and Transfer* (**Bi-RPT**). The optimization problem is expressed as follows (γ is a coefficient):

$$\min_{\boldsymbol{\theta}, \boldsymbol{m}_s, \boldsymbol{m}_t} \mathbb{E}_{(\boldsymbol{x}_t, y_t) \sim \mathcal{D}_t} \left[\mathcal{L}_t((\boldsymbol{m}_s \odot \boldsymbol{m}_t) \odot \boldsymbol{\theta}, \boldsymbol{x}_t, y_t | \boldsymbol{\theta}^*, \boldsymbol{m}_s^*) \right] + \gamma \mathcal{R}(\boldsymbol{m}_s^* \odot \boldsymbol{m}_t) \tag{1}$$

$$\text{s.t. } \{\boldsymbol{\theta}^*, \boldsymbol{m}_s^*\} = \arg\min_{\boldsymbol{\theta}, \boldsymbol{m}_s} \mathbb{E}_{(\boldsymbol{x}_s, y_s) \sim \mathcal{D}_s} \mathcal{L}_s(\boldsymbol{m}_s \odot \boldsymbol{\theta}, \boldsymbol{x}_s, y_s), \tag{2}$$

where $\mathcal{L}_s/\mathcal{L}_t$ represents the objective functions for the two stages, respectively, $\boldsymbol{\theta}$ the models' parameters, and $\mathcal{R}$ the sparsity regularizer. Seemingly complicated at the first glance, the bi-level optimization formulation of Bi-RPT actually admits a clear physics "workflow" interpretation (refer to Sec. A.2). The lower- and upper-level problems in Bi-RPT are solved in an end-to-end manner, meaning that even the fine-tuning depends on $\boldsymbol{\theta}^*$ and $\boldsymbol{m}_s^*$, it can, in turn, provide feedbacks for adjusting the latter: hence a synergistic optimization is achieved between two stages. The sparse mask selection now directly hinges on the end task (target domain loss $\mathcal{L}_t$) rather than heuristics such as weight magnitudes. Lastly, the sparsity levels of $\boldsymbol{m}_s$ and $\boldsymbol{m}_t$ do not need to be separately designated nor manually controlled: we automatically learn the sparsity ratio allocation, under only the total sparsity regularizer $\mathcal{R}$. To practically solve the bi-level optimization of Bi-RPT, we derive algorithms whose details can be found in Appendix A. In general, for the lower-level optimization

problem, we update the models' parameters θ by gradients to minimize $\mathcal{L}_s$; for the upper-level optimization, we utilize the gradient unrolling to develop update rules for θ. We report the results of proof-of-concept experiments in Sec. B.2 to show the effectiveness of our methods.

5 MAIN EXPERIMENTS ON THE X-YIELD BENCHMARK

Task Definition, Architectures and Baselines. We apply Bi-RPT to solve the regression task (predicting the yield strength) and a surrogate classification task on X-Yield. The classification label is constructed based on the bin intervals where the ground-truth yields strength fall in. These intervals are: $[0, 0.5)$, $[0.5, 1)$, $[1, 1.5)$, $[1.5, 2)$, and $[2, \infty)$. The structure of the ML predictor we use is a convolutional neural network (refer to Sec. B.1). We compare our main proposal, Bi-RPT, with two baselines: *No Pretraining* and *Pretrain-and-transfer* (defined in Sec. B.2). The hyperparameters for training are reported in Sec. B.1. **Data Representations.** We featurize each HEA by mapping its composition and temperature into a "pseudoimage" (refer to Sec. B.4 and Fig. A1), which has two channels: the first is constructed from the alloys' composition using the randomized periodic table structure (Feng et al., 2021) and the second is $(T - 273.15)/2000$ where T is the temperature in Kelvin. **Data Splits.** We mainly explore two challenging *extreme few-shot* settings: we sample 5% (and 10%) of experimental data from each alloy type (ternary, quaternary, quinary and senary) as our training set. Results of cross-validation and uncertainty quantification are in Sec. B.6 and Sec. B.9.

5.1 MAIN RESULTS

Classification and regression with extreme few-shot settings. We first apply Bi-RPT to solve the regression and classification tasks under the two extreme few-shot settings. Tab. 1 shows that: (1) pretraining on simulation data can benefit the ML predictor consistently on both the regression (over 10% reduction in MSE) and classification (over 11% improvement in accuracy) tasks, especially when the data are more scarce; (2) the integration of sparsity into the pretraining and transfer workflow can further strengthen the predictor's generalization, improving accuracy by 0.98% and reducing MSE by 8.91% using merely 10% training experiment data, and the improvement also becomes even more significant with 5% training data (1.53% increase and 19.75% reduction in terms of the accuracy and MSE, respectively).

Table 1: Test accuracy on the testing set of different splits of high-fidelity alloy data. The experiments are repeated 10 times, and we report both the mean and the 95% confidence interval.

Method	10% train samples		5% train samples	
	Test MSE	Test Accuracy	Test MSE	Test Accuracy
No Pretraining	0.114 ± 0.007	$54.84 \pm 1.59\%$	0.212 ± 0.041	$47.25 \pm 0.80\%$
Pretrain-and-transfer	0.101 ± 0.001	$65.85 \pm 0.88\%$	0.162 ± 0.002	$62.84 \pm 1.96\%$
Bi-RPT	$\mathbf{0.092 \pm 0.011}$	$\mathbf{66.83 \pm 1.41\%}$	$\mathbf{0.130 \pm 0.006}$	$\mathbf{64.37 \pm 1.10\%}$

Performance comparison on alloys at various temperatures. Based on the trained model with 10% experimental data, we predict the yield strength of two alloys, MoNbTaTiW and HfMoNbTaTiZr, at different temperatures. Tab. 2 shows the predicted yield stress on these alloys using Bi-RPT and baselines. On the quinary and senary alloy systems, Bi-RPT shows exceptional precision in predicting the experimental yield stress. More scrutiny of those predictions reveals several findings that neatly align with our material science expertise. For example, it is known that screw dislocations are more likely to be dominant than the edge in MoNbTi and NbTaTi ternaries (shown from the ternary comparison in the Citrine database (Borg et al., 2020)). Thus it makes sense that the model under-predicts the MoNbTaTiW case: our model seems to correctly pick up these differences and predicts a higher yield strength.

Table 2: Predicted yield stress under different temperatures. Only 10% of the experimental data are available during fine-tuning. We compare Bi-RPT with our "No Pretraining" (NP) and "Pretrain-and-transfer" (PT) baselines and the simulation. The numbers with the smallest error are in **bold**.

Alloys	Temperature (K)	Predicted Yield Stress (GPa)				Experimental (GPa)
		Bi-RPT	NP	PT	Simulation	
MoNbTaTiW	873.15	**0.677**	0.569	0.607	0.372	0.689
	1073.15	**0.618**	0.520	0.523	0.294	0.674
	1273.15	**0.536**	0.530	0.486	0.232	0.620
HfMoNbTaTiZr	873.15	**0.861**	0.556	0.685	1.178	0.973
	1073.15	**0.762**	0.536	0.612	0.516	0.791
	1273.15	**0.662**	0.563	0.573	0.421	0.753

6 CONCLUSIONS

To address the important yet challenging problem of HEA yield stress prediction, we curated and released X-Yield, the first large-scale, multi-fidelity benchmark. To effectively leverage this benchmark, we also designed a two-stage cross-quality few-shot transfer workflow and proposed to utilize sparsity to tackle both challenges of low data quality at pretraining and scarcity at transfer. Besides ad-hoc methods, we formulated a principled bi-level optimization framework to automatically learn the optimal sparse masks and sparsity allocation between two stages. Extensive experiments on both image data testbeds and X-Yield demonstrate the Bi-RPT showed a substantial improvement over existing baselines. Moving forward, we are now closely working with material scientists to validate our ML prediction results based on their domain expertise, and the team has already identified some alloy candidates that appear promising to be experimentally validated.

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A   MORE DETAILS ON METHODS

In this section, we present the technical details of our proposed method and framework ("Hand-Tune" and "Bi-RPT").

A.1   HAND-TUNE

Hand-Tune decides sparse masks for the two stages in an iterative way as explained in Algorithm 1.

Algorithm 1 Hand-Tune

Input: Initialization weights $\boldsymbol{\theta}_0$, low-quality pretraining dataset $\mathcal{D}_s$, high-quality fine-tuning dataset $\mathcal{D}_t$, number of IMP rounds N_s for the pretraining stage and N_t for the fine-tuning stage.
Output: the trained weights $\boldsymbol{\theta}^*$, the sparse mask $\boldsymbol{m}_s$ for the pretraining stage, and the sparse mask $\boldsymbol{m}_t$ for the fine-tuning stage.
Initialize the sparse masks $\boldsymbol{m}_s$ for the pretraining stage to be a all "1" mask.
Initialize the model's weight as $\boldsymbol{\theta}_0$ and train the weights on $\mathcal{D}_s$ to obtain $\boldsymbol{\theta}_s$.
for $i = 1, 2, \ldots, N_s$ **do**   ▷ IMP at the pre-training stage
    Prune 20% of the smallest-magnitude weights from the non-zero regions of $\boldsymbol{m}_s \odot \boldsymbol{\theta}_s$, by setting the values at corresponding positions to those weights in $\boldsymbol{m}_s$ to "0".
    (Re-)train the sparse weights $\boldsymbol{m}_s \odot \boldsymbol{\theta}_s$ on $\mathcal{D}_s$. Only $\boldsymbol{\theta}_s$ is updated.
end for
Initialize the sparse masks at the fine-tuning stage $\boldsymbol{m}_t$ to be all "1" masks and freeze $\boldsymbol{m}_s$.
Initialize model's weight as $\boldsymbol{m}_s \odot \boldsymbol{\theta}_s$, and train on $\mathcal{D}_t$ to obtain $\boldsymbol{m}_s \odot \boldsymbol{\theta}_t$.
for $i = 1, 2, \ldots, N_t$ **do**   ▷ IMP at the fine-tuning stage
    Prune 20% of the smallest-magnitude weights from the non-zero regions of weights $(\boldsymbol{m}_s \odot \boldsymbol{m}_t) \odot \boldsymbol{\theta}_s$, by setting the values at corresponding positions to those weights in $\boldsymbol{m}_t$ to "0".
    (Re-)train the sparse weights $(\boldsymbol{m}_s \odot \boldsymbol{m}_t) \odot \boldsymbol{\theta}_t$ on $\mathcal{D}_t$. Only $\boldsymbol{\theta}_t$ is updated.
end for
Obtain the final sparse weights $(\boldsymbol{m}_s \odot \boldsymbol{m}_t) \odot \boldsymbol{\theta}^*$ and return $\boldsymbol{\theta}^*$, $\boldsymbol{m}_s$ and $\boldsymbol{m}_t$.

A.2   BI-RPT

We now build the techniques to solve the bi-level optimization problem formulated in Bi-RPT.

Formulation

$$\min_{\boldsymbol{\theta},\boldsymbol{m}_s,\boldsymbol{m}_t} \mathop{\mathbb{E}}_{(\boldsymbol{x}_t,y_t)\sim\mathcal{D}_t} \left[\mathcal{L}_t((\boldsymbol{m}_s \odot \boldsymbol{m}_t) \odot \boldsymbol{\theta}, \boldsymbol{x}_t, y_t | \boldsymbol{\theta}^*, \boldsymbol{m}_s^*)\right] + \gamma\mathcal{R}(\boldsymbol{m}_s^* \odot \boldsymbol{m}_t)$$

$$\text{s.t. } \{\boldsymbol{\theta}^*, \boldsymbol{m}_s^*\} = \mathop{\arg\min}_{\boldsymbol{\theta},\boldsymbol{m}_s} \mathop{\mathbb{E}}_{(\boldsymbol{x}_s,y_s)\sim\mathcal{D}_s} \mathcal{L}_s(\boldsymbol{m}_s \odot \boldsymbol{\theta}, \boldsymbol{x}_s, y_s).$$

Interpretation   Let us start from the *lower-level* problem (2) which instantiates the sparsity regularized pre-training stage over $\mathcal{D}_s$: its outputs include the pre-trained weight $\boldsymbol{\theta}^*$ and the corresponding sparse mask $\boldsymbol{m}_s$. Then, the *upper-level* problem (1) depicts the sparsity regularized fine-tuning over $\mathcal{D}_t$, which inherits both $\boldsymbol{\theta}^*$ and $\boldsymbol{m}_s^*$ as its starting point. It continues to modify the weight as well as to evolve another sparse mask $\boldsymbol{m}_t$. Eventually, a sparsity-promoting function $\mathcal{R}$ enforces the total sparsity over the joint mask $\boldsymbol{m}_s \odot \boldsymbol{m}_t$, and the final model weights could be represented as $(\boldsymbol{m}_s \odot \boldsymbol{m}_t) \odot \boldsymbol{\theta}$.

Lower-level problem   We solve the lower-level problem through a p-step SGD unrolling. Let $\boldsymbol{\theta}^{(k)}$ be the model weights, and $\boldsymbol{m}_s^{(k)}$ be the mask for the pretraining stage. The superscript (k) indicates they have been updated on the upper-level for k steps.

$\boldsymbol{\theta}^{(k)}$ and $\boldsymbol{m}_s^{(k)}$ will be the starting points for the lower-level optimization problem. $\boldsymbol{\theta}_l^{(t)}$ and $\boldsymbol{m}_{s,l}^{(t)}$ are the weights and mask, respectively, after being updated for t steps on the lower-level optimization

problem (implying $\boldsymbol{\theta}_l^{(0)} = \boldsymbol{\theta}^{(k)}$ and $\boldsymbol{m}_{s,l}^{(0)} = \boldsymbol{m}_s^{(k)}$). The update rules can be written as

$$\boldsymbol{\theta}_l^{(0)} = \boldsymbol{\theta}^{(k)}, \boldsymbol{\theta}_l^{(p)} = \boldsymbol{\theta}_l^{(p-1)} - \lambda_l \nabla_{\boldsymbol{\theta}} \mathcal{L}_s |_{\boldsymbol{\theta} = \boldsymbol{\theta}_l^{(p-1)}}, \tag{3}$$

$$\boldsymbol{m}_{s,l}^{(0)} = \boldsymbol{m}_s^{(k)}, \boldsymbol{m}_{s,l}^{(p)} = \boldsymbol{m}_{s,l}^{(p-1)} - \lambda_{m,l} \nabla_{\boldsymbol{m}} \mathcal{L}_s |_{\boldsymbol{m} = \boldsymbol{m}_{s,l}^{(p-1)}}, \tag{4}$$

where λ_l is the learning rate for the model weight $\boldsymbol{\theta}$, and $\lambda_{m,l}$ is the learning rate for the mask $\boldsymbol{m}_{s,l}^{(t)}$ at the lower-level optimization problem.

Upper-level problem and Sparse Regularization Loss   The upper-level problem is the sum of two losses: a normal training loss $\mathcal{L}_t$ and a sparse regularization loss $\mathcal{R}$ (γ is a coefficient).

We first develop update rules for the training loss $\mathcal{L}_t$. The weights $\boldsymbol{\theta}^*(:= \boldsymbol{\theta}_l^{(p)})$ and masks $\boldsymbol{m}_s^*(:= \boldsymbol{m}_{s,l}^{(p)})$ from the lower-level problem after p unroll steps will serve as the initialization of the upper-level problem. We update the model weight $\boldsymbol{\theta}$ and masks at the upper level by applying gradient-based methods (take SGD as an example):

$$\boldsymbol{\theta}^{(k+1)} = \boldsymbol{\theta}^* - \lambda_u \frac{\mathrm{d}\mathcal{L}_t}{\mathrm{d}\boldsymbol{\theta}^*} \tag{5}$$

$$= \boldsymbol{\theta}^* - \lambda_u (\frac{\partial \mathcal{L}_t}{\partial \boldsymbol{\theta}^*} + \frac{\partial \mathcal{L}_t}{\partial \boldsymbol{m}_s^*} \frac{\partial \boldsymbol{m}_s^*}{\partial \boldsymbol{\theta}^*}),$$

where λ_u is the learning rate for the weights for the upper-level optimization problem. The gradient on $\boldsymbol{m}_t$ is easy enough: $\frac{\partial \mathcal{L}_t}{\partial \boldsymbol{m}_t}$, while the gradient on $\boldsymbol{m}_s$ is slightly complicated:

$$\frac{\mathrm{d}\mathcal{L}_t}{\mathrm{d}\boldsymbol{m}_s^*} = \frac{\partial \mathcal{L}_t}{\partial \boldsymbol{m}_s^*} + \frac{\partial \mathcal{L}_t}{\partial \boldsymbol{\theta}^*} \frac{\partial \boldsymbol{\theta}^*}{\partial \boldsymbol{m}_s^*}. \tag{6}$$

We expand the latter terms in Eqn. 5 and Eqn. 6 based on the first-order approximation (picking $p = 1$) on the lower-level problem:

$$\frac{\partial \boldsymbol{\theta}^*}{\partial \boldsymbol{m}_s^*} = \frac{\partial(\boldsymbol{\theta}_l^{(0)} - \lambda_l \nabla_{\boldsymbol{\theta}} \mathcal{L}_s)}{\partial(\boldsymbol{m}_{s,l}^{(0)} - \lambda_{m,l} \nabla_{\boldsymbol{m}_s} \mathcal{L}_s)} = \frac{\partial(\boldsymbol{\theta}_l^{(0)} - \lambda_l \nabla_{\boldsymbol{\theta}} \mathcal{L}_s)}{\partial \boldsymbol{\theta}_l^{(0)}} \frac{\partial \boldsymbol{\theta}_l^{(0)}}{\partial(\boldsymbol{m}_{s,l}^{(0)} - \lambda_{m,l} \nabla_{\boldsymbol{m}_s} \mathcal{L}_s)} + \tag{7}$$

$$\frac{\partial(\boldsymbol{\theta}_l^{(0)} - \lambda_l \nabla_{\boldsymbol{\theta}} \mathcal{L}_s)}{\partial \boldsymbol{m}_{s,l}^{(0)}} \frac{\partial \boldsymbol{m}_{s,l}^{(0)}}{\partial(\boldsymbol{m}_{s,l}^{(0)} - \lambda_{m,l} \nabla_{\boldsymbol{m}_s} \mathcal{L}_s)}$$

$$= (\mathrm{I} - \lambda_l \nabla_{\boldsymbol{\theta}}^2 \mathcal{L}_s)(-\lambda_{m,l} \nabla_{\boldsymbol{m}_s \boldsymbol{\theta}} \mathcal{L}_s)^{-1} +$$

$$(-\lambda_l \nabla_{\boldsymbol{m}_s \boldsymbol{\theta}} \mathcal{L}_s)(\mathrm{I} - \lambda_{m,l} \nabla_{\boldsymbol{m}_s}^2 \mathcal{L}_s)^{-1},$$

$$\frac{\partial \boldsymbol{m}_s^*}{\partial \boldsymbol{\theta}^*} = \frac{\partial(\boldsymbol{m}_{s,l}^{(0)} - \lambda_{m,l} \nabla_{\boldsymbol{m}_s} \mathcal{L}_s)}{\partial(\boldsymbol{\theta}_l^{(0)} - \lambda_l \nabla_{\boldsymbol{\theta}} \mathcal{L}_s)} = (\mathrm{I} - \lambda_l \nabla_{\boldsymbol{\theta}}^2 \mathcal{L}_s)^{-1}(-\lambda_{m,l} \nabla_{\boldsymbol{m}_s \boldsymbol{\theta}} \mathcal{L}_s) +$$

$$(-\lambda_l \nabla_{\boldsymbol{m}_s \boldsymbol{\theta}} \mathcal{L}_s)^{-1}(\mathrm{I} - \lambda_{m,l} \nabla_{\boldsymbol{m}_s}^2 \mathcal{L}_s). \tag{8}$$

Further approximations can be made to avoid the matrix inverse and save computation:

$$\frac{\partial \boldsymbol{\theta}^*}{\partial \boldsymbol{m}_s^*} \approx -\lambda_l \nabla_{\boldsymbol{m}_s \boldsymbol{\theta}} \mathcal{L}_s \quad, \frac{\partial \boldsymbol{m}_s^*}{\partial \boldsymbol{\theta}^*} \approx -\lambda_{m,l} \nabla_{\boldsymbol{m}_s \boldsymbol{\theta}} \mathcal{L}_s.$$

Based on the rules, $\boldsymbol{m}_s$ and $\boldsymbol{m}_t$ can be optimized by:

$$\hat{\boldsymbol{m}}_t^{(k+1)} = \boldsymbol{m}_t^{(k)} - \lambda_m \frac{\partial \mathcal{L}_t}{\partial \boldsymbol{m}_t} |_{\boldsymbol{m}_t = \boldsymbol{m}_t^{(k)}}, \quad \hat{\boldsymbol{m}}_s^{(k+1)} = \boldsymbol{m}_s^{(k)} - \lambda_m \frac{\partial \mathcal{L}_t}{\partial \boldsymbol{m}_s} + \lambda_m \lambda_l \frac{\partial \mathcal{L}_t}{\partial \boldsymbol{\theta}^*} \nabla_{\boldsymbol{m}_s \boldsymbol{\theta}} \mathcal{L}_s |_{\boldsymbol{m}_s = \boldsymbol{m}_s^{(k)}}, \tag{9}$$

where the superscript (k) means the steps updated.

We then focus on the latter term. We choose ℓ_0 loss (*i.e.* the number of non-zero elements) as the sparse regularizer $\mathcal{R}$, which is not differentiable and difficult to optimize. Therefore, we follow Guo et al. (2021) to use the smoothed ℓ_0 formulation to facilitate differentiable training. Specifically, a gate function $g_\epsilon(\boldsymbol{x}) := \frac{\boldsymbol{x}^2}{\boldsymbol{x}^2+\epsilon}$, where ϵ is a small positive number, is used to replace the binary masks, which are instead parameterized by $g_\epsilon(\boldsymbol{m}_s)$ and $g_\epsilon(\boldsymbol{m}_t)$. We decay the value of ϵ every epoch, and the gate function will gradually output only polarized numbers (*i.e.,* 0 and 1). We further apply the proximal-SGD (Nitanda, 2014) to minimize the ℓ_0 loss: after we update the $\boldsymbol{m}_s$ and $\boldsymbol{m}_t$ with respect to $\mathcal{L}_t$ by gradient descent-based methods (Eqn. 9), we use the proximal operator to alternatively update each mask. For $\boldsymbol{m}_s$, the formulation can be written as:

$$\text{prox}_{\lambda_m\gamma\mathcal{R}}(\boldsymbol{m}_s^{(k+1)}) = \arg\min_{\boldsymbol{m}_s} \frac{1}{2}\|\boldsymbol{m}_s^{(k+1)}\odot\hat{\boldsymbol{m}}_t^{(k+1)}-\hat{\boldsymbol{m}}_s^{(k+1)}\odot\hat{\boldsymbol{m}}_t^{(k+1)}\|_2^2+\lambda_m\gamma\|\boldsymbol{m}_s^{(k+1)}\odot\hat{\boldsymbol{m}}_t^{(k+1)}\|_0.$$

We follow (Guo et al., 2021) to solve it by relaxing it to the ℓ_1 norm problem, which has a closed form solution:

$$m_{s,i} = \begin{cases} \hat{m}_{s,i}^{(k+1)} - \frac{\gamma\lambda_m}{\hat{m}_{t,i}^{(k+1)}}, & \hat{m}_{s,i}^{(k+1)} \geq \frac{\gamma\lambda_m}{\hat{m}_{t,i}^{(k+1)}} \\ \hat{m}_{s,i}^{(k+1)} + \frac{\gamma\lambda_m}{\hat{m}_{t,i}^{(k+1)}}, & \hat{m}_{s,i}^{(k+1)} \leq -\frac{\gamma\lambda_m}{\hat{m}_{t,i}^{(k+1)}} \\ 0, & -\frac{\gamma\lambda_m}{\hat{m}_{t,i}^{(k+1)}} < \hat{m}_{s,i}^{(k+1)} < \frac{\gamma\lambda_m}{\hat{m}_{t,i}^{(k+1)}} \end{cases}, \tag{10}$$

where $m_{s,i}$ is the i-th element in $\boldsymbol{m}_s$ (the same for $m_{t,i}$).

Similarly, we derive the update for $\boldsymbol{m}_t$:

$$m_{t,i}^{(k+1)} = \begin{cases} \hat{m}_{t,i}^{(k+1)} - \frac{\gamma\lambda_m}{\hat{m}_{s,i}^{(k+1)}}, & \hat{m}_{t,i}^{(k+1)} \geq \frac{\gamma\lambda_m}{\hat{m}_{t,i}^{(k+1)}} \\ \hat{m}_{t,i}^{(k+1)} + \frac{\gamma\lambda_m}{\hat{m}_{s,i}^{(k+1)}}, & \hat{m}_{t,i}^{(k+1)} \leq -\frac{\gamma\lambda_m}{\hat{m}_{t,i}^{(k+1)}} \\ 0, & -\frac{\gamma\lambda_m}{\hat{m}_{s,i}^{(k+1)}} < \hat{m}_{t,i}^{(k+1)} < \frac{\gamma\lambda_m}{\hat{m}_{s,i}^{(k+1)}} \end{cases}. \tag{11}$$

Finally, we combine all these components into Algorithm 2.

Algorithm 2 Solving Bi-RPT

Input: Initialization weights $\boldsymbol{\theta}_0$, training loss functions for two stages $\mathcal{L}_s$ and $\mathcal{L}_t$, low-quality pretraining dataset $\mathcal{D}_s$, high-quality fine-tuning dataset $\mathcal{D}_t$, number of steps for gradient unroll p.
Output: Trained model weights $\boldsymbol{\theta}$, sparse masks $\boldsymbol{m}_s$ and $\boldsymbol{m}_t$.
Train $\boldsymbol{\theta}_0$ on $\mathcal{D}_s$ to get weights $\boldsymbol{\theta}$.
while not converged **do**
    Given the fixed $\boldsymbol{m}_s$, update the weights $\boldsymbol{\theta}$ on $\mathcal{D}_s$ by gradient unrolling (Eqn. 3)
    Update the weights $\boldsymbol{\theta}$ by Eqn. 5
    Update the masks $\boldsymbol{m}_s$ and $\boldsymbol{m}_t$ by Eqn. 9.
    Update the masks $\boldsymbol{m}_s$ and $\boldsymbol{m}_t$ by Eqn. 10 and Eqn. 11.
end while

B MORE EXPERIMENTS DETAILS AND RESULTS

B.1 BASELINES, HYPERPARAMETERS AND ARCHITECTURES.

We list the hyper-parameters we used for all the baselines in this section. **General Settings.** When pre-training the models on $\mathcal{D}_s$ (ImageNet and ImageNet-C), we use the SGD optimizer and a learning rate is 4×10^{-1}. We linearly warm-up the learning rate within 5 epochs, and then decay it by 10 for every 30 epochs. Models are pretrained for 95 epochs on $\mathcal{D}_s$, with a batch size of 1024. On $\mathcal{D}_t$, *i.e.*, CUB-200 and CUB-200 (10-shot), we set the initial learning rate as 1×10^{-3}. The learning rate is decayed by 10 every 30 epochs, and the model is trained for 90 epochs with a batch size of 64.

For Hand-Tune, we train the models with 95 epochs from scratch on $\mathcal{D}_s$ to get a *densely* pretrained models. The number of training epochs is reduced to 45 after the pretrained model is derived. After

the pretraining stage ends, we continue to transfer the model on $\mathcal{D}_t$ following the above hyper-parameters. The number of epochs is also reduced to 45 after we prune the weights.

For No-Pretraining, we train the model using an initial learning rate of 1×10^{-2} and a batch size of 64. For Mix-Training, as the number of classes is different for ImageNet and CUB-200, we use two fully-connected layers on top the normal ResNet-18 backbone, and train them simultaneously. We sample batches from the two domains ($\mathcal{D}_s$ and $\mathcal{D}_t$) using the same batch size of 64. The initial learning rate for these methods are 1×10^{-2}, and it is decayed by 10 every 30 epochs.

For Bi-RPT, we follow the same learning rate settings despite some additional hyper-parameters are newly introduced. The learning rate for the lower-level problem (λ_l) is 1×10^{-3}, the same as the learning rate for upper-level problem (λ_u). The value of γ is set to 1×10^{-4}, which are determined through ablation studies in Table A10. The value of λ_m are set to 3.5, which are also determined through ablation studies in Table A11.

For experiments on X-Yield, We pretrain the ML predictor on the simulation data for 10 epochs. During the pretraining, we use the Adam optimizer (Kingma & Ba, 2014) with an initial learning rate of 1×10^{-4} and a cosine annealing schedule (Loshchilov & Hutter, 2016). For the transfer stage, we fine-tune the pretrained model on the experimental data for 90 epochs. The optimizer we use is the SGD optimizer with an initial learning rate of 1×10^{-3}. We also decay the learning rate by 10 for every 30 epoch. The batch sizes for pretraining and fine-tuning are 16 and 4, respectively.

The ML predictor we use is a convolutional neural network. It consists of 3 convolutional layers, each of which has a kernel size of 3, followed by Batch Normalization (Ioffe & Szegedy, 2015) and ReLU (Glorot et al., 2011) activation. A multi-layer perceptron is appended after the convolutional neural network to generate the final prediction.

B.2 PROOF-OF-CONCEPT EXPERIMENTS.

For proof-of-concept, we conduct experiments on a synthesized testbed of image classification, to compare Hand-Tune and Bi-RPT. We adopt two source-domain dataset options: ImageNet (Deng et al., 2009) and ImageNet-C (Hendrycks & Dietterich, 2019), the latter more noisy and corrupted. Two target-domain options are also accompanied: CUB-200 (Wah et al., 2011) and *CUB-200 (10-shot)*, the latter designed to be rigorously "few-shot" where each class has only 10 training samples. Different combinations of $\mathcal{D}_s/\mathcal{D}_t$ allow us to conduct controlled experiments for stretch-testing various algorithm options' noise robustness as well as data efficiency.

Several baselines are compared to *Hand-Tune* and *Bi-RPT*: (1) *Pretrain-and-transfer*: the basic workflow of pre-training on $\mathcal{D}_s$ followed by finetuning on $\mathcal{D}_t$, with no sparsity involved; (2) *Pretrain sparsity only /transfer sparsity only*: following our proposed pretrain-and-transfer workflow, but conducting IMP to only the pre-training/finetuning stage; (3) *No Pretraining*: directly training on $\mathcal{D}_t$ without using $\mathcal{D}_s$; (4) *Mix Training*: training one model on $\mathcal{D}_s$ and $\mathcal{D}_t$ combined. For those methods with IMP involved, we hand-select the sparsity ratio(s) for either or both stages that yield the highest generalization performance on $\mathcal{D}_t$, i.e., from hyperparameter grid search via cross-validation.

Table A3 reports the accuracies of all methods over various source/target combinations, on the same testing set of CUB-200 in Table A3. All methods use the same ResNet-18 backbone. We high-light several key observations: (1) incorporating $\mathcal{D}_s$ in general helps both CUB-200 and CUB-200 (10-shot), and the improvement margin is much more substantial for the few-shot case; (2) models trained by *Mix Training* fail to generalize on $\mathcal{D}_t$ - in fact even worse than *No Pretraining*, showcasing the negative influence of the quality gap; (3) in the same regime of pre-training then fine-tuning, adding appropriate sparsity helps, and two-stage sparsity can help more; (4) *Bi-RPT* stably outperforms *Hand-Tune* (especially, very notably in few-shot cases), despite the best efforts in tuning the latter's hyperparameters. More observations and analysis can be found in Appendix B (Tables A4 - A7, and Figure A3): including but unlimited to the backfiring effect of "over-sparsification", and the compound influence of per-stage IMP sparsity allocation in *Hand-Tune*.

B.3 PERFORMANCE OF HAND-TUNE UNDER DIFFERENT LEVELS OF SPARSITY.

We report the performance of the Hand-Tune method under different levels of sparsity. We conduct experiments with $N_s = \{0, 1, 2, 3, 4, 5\}$ and $N_t = \{0, 1, 2, 3, 4\}$, resulting sparsity levels

Table A3: Experiments on image data: testing accuracy of fine-tuned ResNet-18 on CUB-200 / CUB-200 (10-shot) as $\mathcal{D}_t$, after pretraining on ImageNet and ImageNet-C as $\mathcal{D}_s$, respectively.

$\mathcal{D}_t$	Methods	Two-stage	m_s	m_t	$\mathcal{D}_s$	
					ImageNet	ImageNet-C
CUB-200 / CUB-200 (10-shot)	No Pretraining	✗	✗	✗	44.27% / 7.98%	
	Mix Training	✗	✗	✗	30.88% / 6.72%	27.32%/6.89%
	Pretrain-and-transfer	✓	✗	✗	74.16% / 38.66%	71.59% / 32.14%
	Pretrain sparsity only	✓	✓	✗	76.01% / 40.73%	73.70% / 38.76%
	Transfer sparsity only	✓	✗	✓	74.16% / 38.90%	71.83% / 32.53%
	Hand-Tune	✓	✓	✓	76.01% / 40.78%	74.01% / 39.94%
	Bi-RPT	✓	✓	✓	**78.60% / 51.55%**	**76.29% / 47.01%**

at pre-training stage of $\{0.00\%, 20.00\%, 36.00\%, 48.80\%, 59.04\%, 67.23\%\}$ and sparsity levels at transfer stage of $\{0.00\%, 20.00\%, 36.00\%, 48.80\%, 59.04\%\}$. We conduct experiments over all the combinations of pretraining and transfer pruning rounds. More specifically, we first perform IMP on $\mathcal{D}_s$ for N_s rounds, and continue to perform IMP on $\mathcal{D}_t$ for another N_t rounds. The experiment results over various source and target combinations are shown in Table A4 to Table A7. Note that all the models are evaluated on the testing samples in $\mathcal{D}_t$.

From this series of tables we observe that: (1) sparsity at pretraining helps improve the model's performance on $\mathcal{D}_t$ after fine-tuning, and the performance gain is larger when $\mathcal{D}_s$ contains more noise and has larger domain shifts; (2) sparsity at transfer is also beneficial to the performance after fine-tuning, and the improvement is more significant when the $\mathcal{D}_t$ is more "data-scarce"; (3) the optimal sparse levels for the two stages vary for different combinations of pretrain and transfer domains, highlighting the importance of choosing the correct pruning rounds for both stages.

Table A4: Test accuracy of fine-tuned ResNet-18 on CUB-200 after pretrained on ImageNet, under different levels of sparsity at pretraining and sparsity at transfer.

Sparsity At Transfer	Sparsity At Pretraining					
	0.00%	20.00%	36.00%	48.80%	59.04%	67.23%
0.00%	74.16%	**76.01%**	75.77%	75.87%	74.99%	74.35%
20.00%	74.15%	75.54%	75.82%	75.98%	74.73%	74.46%
36.00%	74.13%	75.08%	75.56%	75.73%	74.06%	73.94%
48.80%	73.84%	74.01%	74.56%	74.46%	72.37%	72.16%
59.04%	73.61%	73.77%	73.61%	72.89%	70.66%	70.56%

Table A5: Test accuracy of fine-tuned ResNet-18 on CUB-200 after pretrained on ImageNet-C, under different levels of sparsity at pretraining and sparsity at transfer.

Sparsity At Transfer	Sparsity At Pretraining					
	0.00%	20.00%	36.00%	48.80%	59.04%	67.23%
0.00%	71.59%	71.89%	73.44%	73.70%	73.63%	73.52%
20.00%	71.83%	72.44%	73.97%	**74.01%**	73.52%	73.39%
36.00%	71.68%	72.80%	73.46%	73.47%	72.95%	72.70%
48.80%	71.13%	71.87%	72.14%	72.40%	71.87%	71.28%
59.04%	69.26%	70.31%	70.61%	70.73%	70.11%	69.38%

B.4 HEA DATA REPRESENTATIONS

The raw inputs for our ML predictor are the alloy's composition and the temperature where the experiment is conducted; therefore, they are 11-dimensional vectors. We map these vectors into 2D images following the pipeline shown in Figure A1. Given a formulation of an alloy, the periodic

Table A6: Test accuracy of fine-tuned ResNet-18 on CUB-200 (10-shot) after pretrained on ImageNet, under different levels of sparsity at pretraining and sparsity at transfer.

Sparsity At Transfer	Sparsity At Pretraining					
	0.00%	20.00%	36.00%	48.80%	59.04%	67.23%
0.00%	38.66%	35.88%	38.30%	39.23%	40.73%	39.14%
20.00%	38.90%	36.56%	38.66%	40.14%	**40.78%**	39.33%
36.00%	38.42%	36.31%	38.95%	40.14%	40.32%	38.97%
48.80%	38.13%	35.23%	37.80%	38.02%	38.37%	35.69%
59.04%	37.02%	33.21%	35.83%	35.54%	35.55%	32.78%

Table A7: Test accuracy of fine-tuned ResNet-18 on CUB-200 (10-shot) after pretrained on ImageNet-C, under different levels of sparsity at pretraining and sparsity at transfer.

Sparsity At Transfer	Sparsity At Pretraining					
	0.00%	20.00%	36.00%	48.80%	59.04%	67.23%
0.00%	32.14%	34.29%	38.07%	36.12%	38.21%	36.85%
20.00%	32.53%	35.99%	39.63%	37.92%	**39.94%**	37.66%
36.00%	32.52%	36.07%	38.99%	38.56%	39.07%	36.95%
48.80%	31.69%	34.85%	37.59%	36.45%	36.69%	34.79%
59.04%	30.64%	32.55%	34.79%	33.31%	33.72%	32.64%

table representation (PTR) sets the percentage of each element into a specific position according to its position in the periodic table; and the randomized periodic table representation (RPTR) sets the percentage of each element with a pre-defined shuffled periodic table. In our experiments, we use the RPTR to map values in a more balanced way.

B.5 PERFORMANCE AT HIGH TEMPERATURES.

One of the important tasks in the alloy design community is to find alloys that are capable of withstanding stress at high temperatures. To verify if Bi-RPT can provide reliable recommendations to help the community achieve this goal, we look deeper into the predictive performance in high-temperature regimes. We train our model with 10% data, predict the yield stress for the rest 90%, and compare the predictive quality of models at high temperatures in Figure A2. We can see that Bi-RPT significantly outperforms other baselines, especially at temperatures greater than 1400K. These results suggest Bi-RPT could serve as a strong tool for designing HEAs with superior yield stress at elevated temperatures.

B.6 CLASSIFICATION AND REGRESSION WITH 10-FOLD CROSS-VALIDATION.

On the slightly "data-rich" 10-fold cross-validation setting, we have observed a similar trend: the bi-stage regime of pretraining and transfer out-performs the single-stage training pipeline, and incorporating sparsity can consistently provide remarkable improvement to the ML predictor, particularly in the regression performance.

Table A8: Classification and regression performance under the ten-folded cross-validation settings.

	Classification	Regression
No Pretraining	$67.50 \pm 5.16\%$	0.226 ± 0.027
Pretrain-and-transfer	$82.09 \pm 3.86\%$	0.206 ± 0.026
Bi-RPT	$\mathbf{82.50 \pm 2.93\%}$	$\mathbf{0.068 \pm 0.009}$

Figure A1: The pipeline for converting a raw input into a pseudoimage. The temperature is embedded as the value of the second channel.

B.7 ABLATIONS ON IMAGE DATA

Effects of sparsity at two stages. We conduct a set of ablation experiments to study the effects of two sparse masks in the Bi-RPT formulation on ResNet-18 (pretrained by ImageNet-C, fine-tuned on CUB-200). We compare against three baselines: fixing m_s, fixing m_t, and fixing both of them. The performance comparison is shown in Table A9, where we can see that learning masks at both stage yields the highest performance.

Effects of γ We conduct a set of ablation experiments to study the effects of different γ again on ResNet-18 (pretrained by ImageNet-C, fine-tuned on CUB-200).We vary γ with in *i.e.,* $\{0.5, 1, 2, 3\} \times 10^{-4}$, and we present the results in Table A10. We show that 1×10^{-4} yields the highest performance among all the choices.

Figure A2: Prediction MSE under different temperatures. We compare the results of three methods: No Pretraining (NP), Pretrain-and-transfer (PT), and Bi-RPT.

Effects of learning rates. We conduct a set of ablation experiments on ResNet-18 (pretrained by ImageNet-C, fine-tuned on CUB-200) to study the effects of different learning rate on m_s and m_t. The learning rates we study in this ablation experiments are $\{2.5, 3.0, 3.5, 4.0, 4.5, 5.0\}$. We present the test accuracies in Table A11, and we observe that Bi-RPT can stably outperform baselines (74.01%) within a wide range of λ_m.

Table A9: Ablation study on different sparse masks on image data. "Fixed" means the value of h unchanged. We study the combination of pretraining on ImageNet-C and transferring to Birds.

Mask Type	Test Accuracy
Fixed m_s and m_t	71.58%
Fixed m_s	72.09%
Fixed m_t	75.53%
Ours (Bi-RPT)	76.29%

Table A10: Ablation study on the effects of different γ on the image data. Test accuracy of fine-tuned ResNet-18 on CUB-200 after pretrained on ImageNet-C is reported.

γ	Test Accuracy
0.5×10^{-4}	72.32%
1×10^{-4}	76.29%
2×10^{-4}	65.42%
3×10^{-4}	52.59%

Table A11: Ablation study on the effects of different learning rate on m_s and m_t on image data. Test accuracy of fine-tuned ResNet-18 on CUB-200 after pretrained on ImageNet-C is reported.

λ_m	Test Accuracy
2.5	72.88%
3.0	75.73%
3.5	76.29%
4.0	75.94%
4.5	73.69%
5.0	73.34%

B.8 VISUALIZATION

We visualize the sparsity pattern learned by Bi-RPT at two stages in Figure A3.

B.9 UNCERTAINTY QUANTIFICATION

We provide additional analysis of uncertain quantification. We ensemble ten models trained with Bi-RPT and pretrain-and-transfer (PT) methods by averaging their predictions (Lakshminarayanan et al., 2017), and calculate the standard deviation of the predictions as the uncertainty. The results after ensemble are shown in Table A12.

We show that an ensemble of sparse models provides more reliable results compared to the pretrain-and-transfer baseline. Compared with the ensemble of dense models (PT), the ensemble of sparse models also exhibits strong correlation between the uncertainty and the prediction error.

Figure A3: Layerwise sparsity learned by Bi-RPT on CUB-200 and Birds-S with ImageNet and ImageNet-C pretraining. We report the sparsity level of the two masks, as well as their combined sparsity (note that Bi-RPT allows for the two masks to partially overlap).

Table A12: Uncertainty estimation calculated by ensembling independently trained models. We study two methods: pretrain-and-transfer (PT) and Bi-RPT. The results after ensemble are reported as PT-Ensemble and Bi-RPT-Ensemble, respectively. The estimated uncertainty is reported in brackets.

Alloys	Temperature (K)	Predicted Yield Stress (GPa)				Experimental (GPa)
		Bi-RPT	Bi-RPT-Ensemble	PT	PT-Ensemble	
MoNbTaTiW	873.15	**0.677**	0.798 (0.102)	0.607	0.624 (0.022)	0.689
	1073.15	0.618	**0.681 (0.111)**	0.523	0.528 (0.013)	0.674
	1273.15	0.536	**0.567 (0.124)**	0.486	0.496 (0.017)	0.620
HfMoNbTaTiZr	873.15	0.861	**0.864 (0.098)**	0.685	0.698 (0.017)	0.973
	1073.15	**0.762**	0.747 (0.105)	0.612	0.624 (0.022)	0.791
	1273.15	**0.662**	0.646 (0.134)	0.573	0.587 (0.022)	0.753

C MORE DETAILS ON DATASET

C.1 DATASET CHARACTERISTICS AND "QUALITY GAP"

As depicted in Figure A4, the simulation and experimental yield stress have different distributions. In the low-quality simulation data, a considerable portion of yield stress annotations is greater than 2, while the experimental data hardly contains yield stress points beyond 2 (with one datapoint exception) due to the experimental condition constraints. The distribution of the simulated yield stress is also significantly more skewed than the experimental ones. Pairwise visualization of the yield stress on the 240 high-quality experimental samples suggests a substantial deviation between the simulation and experimental results. The distributions of the processing temperatures are also heterogeneous, *i.e.*, the simulation data presents a uniform pattern while the temperatures in the conducted experiments are in a bimodal shape. These observations showcase the domain shifts or "quality gap" between simulations and experiments.

We visualize the distribution of the yield strength and the temperature of the simulation and experimental data, and also the pairwise visualization (experimentally measured versus theoretically calculated) of the yield strength on the 240 high-quality samples in Figure A4.

Figure A4: Left: the distribution of the yield stress; Middle: the distribution of the temperature; Right: pairwise visualization of the yield stress.

C.2 DATASET COMPARISON

We have provided a comparison between different relevant datasets in Table A13. We elaborate more on the differences:

1. Maresca & Curtin (2020) have only sparse data from the Mo-Nb-Ta-V-W element family.

2. Lee et al. (2021a) has released a database of the predicted yield strength of 10 million alloys from the Al-Cr-Mo-Nb-Ta-V-W-Hf-Ti-Zr family at 1300 K. Our dataset contains alloys from Al-Cr-**Fe**-Mo-Nb-Ta-V-W-Hf-Ti-Zr family at temperatures from **300 K** to **2500 K**. Our simulation data are significantly larger (over 3 billion samples). The whole simulation data will be available, while only 100K are included for training the ML models in this study.

3. Borg et al. (2020) compiles experimental data from published material science articles since 2004. The dataset contains 630 samples with different crystal structures. While our experimental dataset also compiles existing experimental data, we have also sub-selected the data points using material science domain knowledge. Specifically, we only focus on alloys with BCC structures in contrast to Borg et al. (2020).

Table A13: Comparison between different datasets.

Dataset	Alloy Family	Number of data points	Temperature
Maresca & Curtin (2020)	Mo-Nb-Ta-V-W	Sparse	N/A
Lee et al. (2021a)	Al-Cr-Mo-Nb-Ta-V-W-Hf-Ti-Zr	10 million	1300 K
Borg et al. (2020)	N/A	630	N/A
X-Yield (Ours)	Al-Cr-Fe-Mo-Nb-Ta-V-W-Hf-Ti-Zr	3 billion	300 K - 2500 K