OFF-DYNAMICS REINFORCEMENT LEARNING: TRAINING FOR TRANSFER WITH DOMAIN CLASSIFIERS

ABSTRACT

We propose a simple, practical, and intuitive approach for domain adaptation in reinforcement learning. Our approach stems from the idea that the agent's experience in the source domain should look similar to its experience in the target domain. Building off of a probabilistic view of RL, we achieve this goal by compensating for the difference in dynamics by modifying the reward function. This modified reward function is simple to estimate by learning auxiliary classifiers that distinguish source-domain transitions from target-domain transitions. Intuitively, the agent is penalized for transitions that would indicate that the agent is interacting with the source domain, rather than the target domain. Formally, we prove that applying our method in the source domain is guaranteed to obtain a near-optimal policy for the target domain, provided that the source and target domains satisfy a lightweight assumption. Our approach is applicable to domains with continuous states and actions and does not require learning an explicit model of the dynamics. On discrete and continuous control tasks, we illustrate the mechanics of our approach and demonstrate its scalability to high-dimensional tasks.

1 INTRODUCTION

Reinforcement learning (RL) can automate the acquisition of complex behavioral policies through real-world trial-and-error experimentation. However, many domains where we would like to learn policies are not amenable to such trial-and-error learning, because the errors are too costly: from autonomous driving to flying airplanes to devising medical treatment plans, safety-critical RL problems necessitate some type of *transfer learning*, where a safer source domain, such as a simulator, is used to train a policy that can then function effectively in a target domain. In this paper, we examine a specific transfer learning scenario that we call domain adaptation, by analogy to domain adaptation problems in computer vision (Csurka, 2017), where the training process in a source domain can be modified so that the resulting policy is effective in a given target domain.

RL algorithms today require a large amount of experience in the *target domain*. However, for many tasks we may have access to a different but structurally similar *source domain*. While the source domain has different dynamics than the target domain, experience in the source domain is much cheaper to collect. However, transferring policies from one domain to another is challenging because strategies which are effective in the source domain may not be effective in the target domain. For example, aggressive driving may work well on a dry racetrack but fail catastrophically on an icy road. While prior work has studied the domain adaptation of *observations* in RL (Bousmalis et al., 2018; Ganin et al., 2016; Higgins et al., 2017), it ignores the domain adaptation of the *dynamics*.

This paper presents a simple approach for domain adaptation in RL, illustrated in Fig. 1. Our main idea is that the agent's experience in the source domain should look similar to its experience in the target domain. Building off of a probabilistic view of RL, we formally show that we can achieve this goal by *compensating for the difference in dynamics by modifying the reward function*. This modified reward function is simple to estimate by learning auxiliary classifiers that distinguish source-domain transitions from target-domain transitions. Be-

Figure 1: Our method acquires a policy for the target domain by practicing in the source domain using a (learned) modified reward function.

cause our method learns a classifier, rather than a dynamics model, we expect it to handle high-dimensional tasks better than model-based methods, a conjecture supported by experiments on the 111-dimensional Ant task. Unlike prior work based on similar intuition (Koos et al., 2012; Wulfmeier et al., 2017b), a key contribution of our work is a formal guarantee that our method yields a near-optimal policy for the target domain.

The main contribution of this work is an algorithm for domain adaptation to dynamics changes in RL, based on the idea of compensating for differences in dynamics by modifying the reward function. This algorithm does not need to estimate transition probabilities, but rather modifies the reward function using a pair of classifiers. We formally analyze the conditions under which our method produces near-optimal policies for the target domain. On a range of discrete and continuous control tasks, we both illustrate the mechanics of our approach and demonstrate its scalability to higher-dimensional tasks. broadly-applicable approach for learning from inaccurate models.

2 RELATED WORK

While our work will focus on domain adaptation applied to RL, we start by reviewing more general ideas in domain adaptation, and defer to Kouw & Loog (2019) for a recent review of the field. Two common approaches to domain adaptation are importance weighting and domain-agnostic features. *Importance-weighting methods* (e.g., (Zadrozny, 2004; Cortes & Mohri, 2014; Lipton et al., 2018)) estimate the likelihood ratio of examples under the target domain versus the source domain, and use this ratio to re-weight examples sampled from the source domain. Similar to prior work on importance weighting (Bickel et al., 2007; Sønderby et al., 2016; Mohamed & Lakshminarayanan, 2016; Uehara et al., 2016), our method will use a classifier to estimate a probability ratio. Since we will need to estimate the density ratio of conditional distributions (transition probabilities), we will learn two classifiers. Importantly, we will use the logarithm of the density ratio to modify the reward function instead of weighting samples by the density ratio, which is often numerically unstable (see, e.g., Schulman et al. (2017, §3)) and led to poor performance in our experiments.

Prior methods for applying domain adaptation to RL include approaches based on system identification, domain randomization, and observation adaptation. Perhaps the most established approach, system identification (Ljung, 1999), uses observed data to tune the parameters of a simulator (Feldbaum, 1960; Werbos, 1989; Wittenmark, 1995; Ross & Bagnell, 2012; Tan et al., 2016; Zhu et al., 2017b; Farchy et al., 2013) More recent work has successfully used this strategy to bridge the sim2real gap (Chebotar et al., 2019; Rajeswaran et al., 2016). Closely related is work on online system identification and meta-learning, which directly uses the inferred system parameters to update the policy (Yu et al., 2017; Clavera et al., 2018; Tanaskovic et al., 2013; Sastry & Isidori, 1989). However, these approaches typically require either a model of the environment or a manually-specified distribution over potential test-time dynamics, requirements that our method will lift. Another approach, *domain randomization*, randomly samples the parameters of the source domain and then finds the best policy for this randomized environment (Sadeghi & Levine, 2016; Tobin et al., 2017; Peng et al., 2018; Cutler et al., 2014). While often effective, this method is sensitive to the choice of which parameters are randomized, and the distributions from which these simulator parameters are sampled. A third approach, *observation adaptation*, modifies the observations of the source domain to appear similar to those in the target domain (Fernando et al., 2013; Hoffman et al., 2016; Wulfmeier et al., 2017a). While this approach has been successfully applied to video games (Gamrian & Goldberg, 2018) and robot manipulation (Bousmalis et al., 2018), it ignores the fact that the source and target domains may have differing dynamics.

Finally, our work is similar to prior work on transfer learning (Taylor & Stone, 2009) and meta-learning in RL, but makes less strict assumptions that most prior work. For example, most work on meta-RL Killian et al. (2017); Duan et al. (2016); Mishra et al. (2017); Rakelly et al. (2019) and some work on transfer learning (Perkins et al., 1999; Tanaka & Yamamura, 2003; Sunmola & Wyatt, 2006) assume that the agent has access to many source tasks, all drawn from the same distribution as the target task. Selfridge et al. (1985); Madden & Howley (2004) assume a manually-specified curriculum of tasks, Ravindran & Barto (2004) assume that the source and target domains have the same dynamics locally, and Sherstov & Stone (2005) assume that the set of actions that are useful in the source domain is the same as the set of actions that will be useful in the target domain. Our method does not require these assumptions, allowing it to successfully learn in settings

where these prior works would fail. For example, the assumption of Sherstov & Stone (2005) is violated in our experiments with broken robots: actions which move a joint are useful in the source domain (where the robot is fully-function) but not useful in the target domain (where that joint is disabled). Our method will significantly outperform an importance weighting baseline (Lazaric, 2008). Unlike Vemula et al. (2020), our method does not require learning a dynamics model and is applicable to stochastic environments and those with continuous states and actions. Our algorithm bears a resemblance to that in Wulfmeier et al. (2017b), but a crucial algorithmic difference allows us to prove that our method acquires a near-optimal policy in the target domain, and also leads to improved performance empirically.

The theoretical derivation of our method is inspired by prior work which formulates control as a problem of probabilistic inference (e.g., (Toussaint, 2009; Rawlik et al., 2013; Levine et al., 2018)). Algorithms for model-based RL (e.g., (Deisenroth & Rasmussen, 2011; Hafner et al., 2018; Janner et al., 2019)) and off-policy RL (e.g., (Munos et al., 2016; Fujimoto et al., 2018; Dann et al., 2014; Dudík et al., 2011) similarly aim to improve the sample efficiency of RL, but do use the source domain to accelerate learning. Our method is applicable to any maximum entropy RL algorithm, including on-policy (Song et al., 2019), off-policy (Abdolmaleki et al., 2018; Haarnoja et al., 2018), and model-based (Janner et al., 2019; Williams et al., 2015) algorithms. We will use the SAC (Haarnoja et al., 2018) in our experiments and compare against model-based baselines.

3 PRELIMINARIES

In this section, we introduce notation and formally define domain adaptation for RL. Our problem setting will consider two MDPs: $\mathcal{M}_{\text{source}}$ represents the source domain (e.g., a practice facility, simulator, or learned approximate model of the target domain) while $\mathcal{M}_{\text{target}}$ represents a the target domain. We assume that the two domains have the same state space $\mathcal{S}$, action space $\mathcal{A}$, reward function r, and initially state distribution $p_1(s_1)$; the only difference between the domains is the dynamics, $p_{\text{source}}(s_{t+1} \mid s_t, a_t)$ and $p_{\text{target}}(s_{t+1} \mid s_t, a_t)$. We will learn a Markovian policy $\pi_\theta(a \mid s)$, parametrized by θ. Our objective is to learn a policy π that maximizes the expected discounted sum of rewards on $\mathcal{M}_{\text{target}}$, $\mathbb{E}_{\pi, \mathcal{M}_{\text{target}}}[\sum_t \gamma^t r(s_t, a_t)]$. We now formally define our problem setting:

Definition 1. *Domain Adaptation for RL is the problem of using interactions in the source MDP $\mathcal{M}_{source}$ together with a small number of interactions in the target MDP $\mathcal{M}_{target}$ to acquire a policy that achieves high reward in the target MDP, $\mathcal{M}_{target}$.*

We will assume every transition with non-zero probability in the target domain will have non-zero probability in the source domain:

$$p_{\text{target}}(s_{t+1} \mid s_t, a_t) > 0 \implies p_{\text{source}}(s_{t+1} \mid s_t, a_t) > 0 \qquad \text{for all } s_t, s_{t+1} \in \mathcal{S}, a_t \in \mathcal{A}. \quad (1)$$

This assumption is common in work on importance sampling (Koller & Friedman, 2009, §12.2.2), and the converse need not hold: transitions that are possible in the source domain need not be possible in the target domain.

4 A VARIATIONAL PERSPECTIVE ON DOMAIN ADAPTATION IN RL

The probabilistic inference interpretation of RL (Kappen, 2005; Todorov, 2007; Toussaint, 2009; Ziebart, 2010; Rawlik et al., 2013; Levine, 2018) treats the reward function as defining a desired distribution over trajectories. The agent's task is to sample from this distribution by picking trajectories with probability proportional to their exponentiated reward. This section will reinterpret this model in the context of domain transfer, showing that domain adaptation of *dynamics* can be done by modifying the *rewards*. To apply this model to domain adaptation, define $p(\tau)$ as the desired distribution over trajectories in the target domain,

$$p(\tau) \propto p_1(s_1) \left(\prod_t p_{\text{target}}(s_{t+1} \mid s_t, a_t) \right) \exp \left(\sum_t r(s_t, a_t) \right),$$

and $q(\tau)$ as our agent's distribution over trajectories in the source domain,

$$q(\tau) = p_1(s_1) \prod_t p_{\text{source}}(s_{t+1} \mid s_t, a_t) \pi_\theta(a_t \mid s_t).$$

As noted in Section 3, we assume both trajectory distributions have the same initial state distribution. Our aim is to learn a policy whose behavior in the source domain both receives high reward and has high likelihood under the target domain dynamics. We codify this objective by minimizing the reverse KL divergence between these two distributions:

$$\min_{\pi(a|s)} D_{\mathrm{KL}}(q \| p) = -\mathbb{E}_{p_{\mathrm{source}}}\left[\sum_t r(s_t, a_t) + \mathcal{H}_\pi[a_t \mid s_t] + \Delta r(s_{t+1}, s_t, a_t) \right] + c, \quad (2)$$

where

$$\Delta r(s_{t+1}, s_t, a_t) \triangleq \log p(s_{t+1} \mid s_t, a_t) - \log q(s_{t+1} \mid s_t, a_t).$$

The constant c is the partition function of $p(\tau)$, which is independent of the policy and dynamics. While Δr is defined in terms of transition probabilities, in Sec. 5 we show how to estimate Δr without learning transition probabilities directly. Where the source and target dynamics are equal, the correction term Δr is zero and we recover maximum entropy RL (Ziebart, 2010; Todorov, 2007). The reward correction is different from prior work that adds $\log \beta(a \mid s)$ to the reward to regularize the policy to be close to the behavior policy β (e.g., Jaques et al. (2017); Abdolmaleki et al. (2018)).

In the case where the source dynamics are *not* equal to the true dynamics, this objective is not the same as maximum entropy RL on trajectories sampled from the source domain. Instead, this objective suggests a corrective term Δr that should be added to the reward function to account for the discrepancy between the source and target dynamics. The correction term, Δr, is quite intuitive. If a transition (s_t, a_t, s_{t+1}) has equal probability in the source and target domains, then $\Delta r(s_t, a_t) = 0$ so no correction is applied. For transitions that are likely in the source but are unlikely in the target domain, $\Delta r < 0$, so the agent is penalized for "exploiting" inaccuracies or discrepancies in the source domain by taking these transitions. For the example environment in Figure 1, transitions through the center of the environment are blocked in the target domain but not in the source domain. For these transitions, Δr would serve as a large penalty, discouraging the agent from taking these transitions and instead learning to navigate around the wall. Appendix A presents additional interpretations of Δr in terms of coding theory, mutual information, and a constraint on the discrepancy between the source and target dynamics. Appendix C discusses how prior work on domain agnostic feature learning can be viewed as a special case of our framework.

4.1 THEORETICAL GUARANTEES

We now analyze when maximizing the modified reward $r + \Delta r$ in the source domain yields a near-optimal policy for the target domain. Our proof relies on the following lightweight assumption:

Assumption 1. *Let $\pi^* = \arg\max_\pi \mathbb{E}_p\left[\sum r(s_t, a_t)\right]$ be the reward-maximizing policy in the target domain. Then the expected reward in the source and target domains differs by at most $2R_{max}\sqrt{\epsilon/2}$:*

$$\left| \mathbb{E}_{p_{source}}\left[\sum r(s_t, a_t) \right] - \mathbb{E}_{p_{target}}\left[\sum r(s_t, a_t) \right] \right| \leq 2R_{max}\sqrt{\epsilon/2}.$$

This assumption says that the optimal policy in the target domain is still a good policy for the source domain, and its expected reward is similar in both domains. We do not require that the opposite be true: the optimal policy in the source domain does not need to receive high reward in the target domain. If there are multiple optimal policies, we only require that this assumption hold for one of them. We now state our main result:

Theorem 4.1. *Let π^*_{DARC} be the policy that maximizes the modified (entropy-regularized) reward in the source domain, let π^* be the policy that maximizes the (unmodified, entropy-regularized) reward in the target domain, and assume that π^* satisfies Assumption 1. Then the following holds:*

$$\mathbb{E}_{p_{target}, \pi^*_{DARC}}\left[\sum r(s_t, a_t) + \mathcal{H}[a_t \mid s_t] \right] \geq \mathbb{E}_{p_{source}, \pi^*}\left[\sum r(s_t, a_t) + \mathcal{H}[a_t \mid s_t] \right] - 4R_{max}\sqrt{\epsilon/2}.$$

See Appendix B for the proof. This result that π^*_{DARC} attains near-optimal (entropy-regularized) reward on the target domain. Thus, we can expect that modifying the reward function should allow us to adapt to different dynamics. The next section will present a practical algorithm for acquiring π^*_{DARC} by estimating and effectively maximizing the modified reward in the source domain.

Algorithm 1 Domain Adaptation with Rewards from Classifiers [DARC]

1: **Input:** source MDP $\mathcal{M}_{\text{source}}$ and target $\mathcal{M}_{\text{target}}$; ratio r of experience from source vs. target.
2: **Initialize:** replay buffers for source and target transitions, $\mathcal{D}_{\text{source}}, \mathcal{D}_{\text{target}}$; policy π; parameters $\theta = (\theta_{\text{SAS}}, \theta_{\text{SA}})$ for classifiers $q_{\theta_{\text{SAS}}}(\text{target} \mid s_t, a_t, s_{t+1})$ and $q_{\theta_{\text{SAS}}}(\text{target} \mid s_t, a_t)$.
3: **for** $t = 1, \cdots,$ num iterations **do**
4:     $\mathcal{D}_{\text{source}} \leftarrow \mathcal{D}_{\text{source}} \cup \text{ROLLOUT}(\pi, \mathcal{M}_{\text{source}})$ ▷ Collect source data.
5:     **if** $t \mod r = 0$ **then**   ▷ Periodically, collect target data.
6:         $\mathcal{D}_{\text{target}} \leftarrow \mathcal{D}_{\text{target}} \cup \text{ROLLOUT}(\pi, \mathcal{M}_{\text{target}})$
7:     $\theta \leftarrow \theta - \eta \nabla_\theta \ell(\theta)$ ▷ Update both classifiers.
8:     $\tilde{r}(s_t, a_t, s_{t+1}) \leftarrow r(s_t, a_t) + \Delta r(s_t, a_t, s_{t+1})$ ▷ Δr is computed with Eq. 3.
9:     $\pi \leftarrow \text{MAXENT RL}(\pi, \mathcal{D}_{\text{source}}, \tilde{r})$
10: **return** π

---

5 DOMAIN ADAPTATION IN RL WITH A LEARNED REWARD

The variational perspective on model-based RL in the previous section suggests that we should modify the reward in the source domain by adding Δr. In this section we develop a practical algorithm for off-dynamics RL by showing how Δr can be estimated without learning an explicit dynamics model.

To estimate Δr, we will use a pair of (learned) binary classifiers, which will infer whether transitions came from the source or target domain. The key idea is that the transition probabilities are related to the classifier probabilities via Bayes' rule:

Figure 2: Block diagram of DARC (Alg. 1)

$$p(\text{target} \mid s_t, a_t, s_{t+1}) = \underbrace{p(s_{t+1} \mid s_t, a_t, \text{target})}_{=p_{\text{target}}(s_{t+1} \mid s_t, a_t)} p(s_t, a_t \mid \text{target})p(\text{target})/p(s_t, a_t, s_{t+1}).$$

We estimate the term $p(s_t, a_t \mid \text{target})$ on the RHS via *another* classifier, $p(\text{target} \mid s_t, a_t)$:

$$p(s_t, a_t \mid \text{target}) = \frac{p(\text{target} \mid s_t, a_t)p(s_t, a_t)}{p(\text{target})}.$$

Substituting these expression into our definition for Δr and simplifying, we obtain an estimate for Δr that depends solely on the predictions of these two classifiers:

$$\Delta r(s_t, a_t, s_{t+1}) = \log p(\text{target} \mid s_t, a_t, s_{t+1}) - \log p(\text{target} \mid s_t, a_t)$$
$$- \log p(\text{source} \mid s_t, a_t, s_{t+1}) + \log p(\text{source} \mid s_t, a_t) \tag{3}$$

The orange terms are the difference in logits from the classifier conditioned on s_t, a_t, s_{t+1}, while the blue terms are the difference in logits from the classifier conditioned on just s_t, a_t. Intuitively, Δr answers the following question: for the task of predicting whether a transition came from the source or target domain, how much better can you perform after observing s_{t+1}? We make this connection precise in Appendix A.2 by relating Δr to mutual information. Ablation experiments (Fig. 10) confirm that both classifiers are important to the success of our method.

Algorithm Summary   Our algorithm modifies an existing MaxEnt RL algorithm to additionally learn two classifiers, $q_{\theta_{\text{SAS}}}(\text{target} \mid s_t, a_t, s_{t+1})$ and $q_{\theta_{\text{SAS}}}(\text{target} \mid s_t, a_t)$, parametrized by θ_{SAS} and θ_{SA} respectively, to minimize the standard cross-entropy loss.

$$\ell_{\text{SAS}}(\theta_{\text{SAS}}) \triangleq -\mathbb{E}_{\mathcal{D}_{\text{target}}}\left[\log q_{\theta_{\text{SAS}}}(\text{target} \mid s_t, a_t, s_{t+1})\right] - \mathbb{E}_{\mathcal{D}_{\text{source}}}\left[\log q_{\theta_{\text{SA}}}(\text{source} \mid s_t, a_t, s_{t+1})\right]$$

$$\ell_{\text{SA}}(\theta_{\text{SA}}) \triangleq -\mathbb{E}_{\mathcal{D}_{\text{target}}}\left[\log q_{\theta_{\text{SA}}}(\text{target} \mid s_t, a_t)\right] - \mathbb{E}_{\mathcal{D}_{\text{source}}}\left[\log q_{\theta_{\text{SA}}}(\text{source} \mid s_t, a_t)\right].$$

Our algorithm, Domain Adaptation with Rewards from Classifiers (DARC), is presented in Alg. 1 and illustrated in Fig. 2. To simplify notation, we define $\theta \triangleq (\theta_{SAS}, \theta_{SA})$ and $\ell(\theta) \triangleq \ell_{SAS}(\theta_{SAS}) + \ell_{SA}(\theta_{SA})$. At each iteration, we collect transitions from the source and (less frequently) target domain, storing the transitions in separate replay buffers. We then sample a batch of experience from both buffers to update the classifiers. We use the classifiers to modify the rewards from the *source* domain, and apply MaxEnt RL to this experience. We use SAC (Haarnoja et al., 2018) as our MaxEnt RL algorithm, but emphasize that DARC is applicable to any MaxEnt RL algorithm (e.g., on-policy, off-policy, and model-based). When training the classifiers, we add Gaussian input noise to prevent overfitting to the small number of target-domain transitions (see Fig. 10 for an ablation).

6 EXPERIMENTS

We start with a didactic experiment to build intuition for the mechanics of our method, and then evaluate on more complex tasks. Our experiments will show that DARC outperforms alternative approaches, such as directly applying RL to the target domain or learning importance weights. We will also show that our method can account for domain shift in the termination condition, and confirm the importance of learning two classifiers.

Illustrative example. We start with a simple gridworld example, shown on the right, where we can apply our method without function approximation. The goal is to navigate from the top left to the bottom left. The real environment contains an obstacle (shown in red), which is not present in the source domain. If we simply apply RL on the source domain, we obtain

Figure 3: **Tabular example of off-dynamics RL**

a policy that navigates directly to the goal (blue arrows), and will fail when used in the target domain. We then apply our method: we collect trajectories from the source domain and real world to fit the two tabular classifiers. These classifiers give us a modified reward, which we use to learn a policy in the source domain. The modified reward causes our learned policy to navigate around the obstacle, which succeeds in the target environment.

Visualizing the reward modification in stochastic domains. In our next experiment, we use an "archery" task to visualize how the modified reward accounts for differences in dynamics. The task, shown in Fig. 4, requires choosing an angle at which to shoot an arrow. The practice range (i.e., the source domain) is outdoors, with wind that usually blows from left to right. The competition range (i.e., the target domain) is indoors with no wind. The reward is the negative distance to the target. We

Figure 4: **Visualizing the modified reward**

plot the reward as a function of the angle in both domains in Fig. 4. The optimal strategy for the outdoor range is to compensate for the wind by shooting slightly to the left ($\theta = -0.8$), while the optimal strategy for the indoor range is to shoot straight ahead ($\theta = 0$). We estimate the modified reward function with DARC, and plot the modified reward in the windy outdoor range and indoor range. We aggregate across episodes using $J(\theta) = \log \mathbb{E}_{p(s'|\theta)}[\exp(r(s'))]$; see Appendix E.4 for details. We observe that maximizing the modified reward in the windy range does not yield high reward in the windy range, but does yield a policy that performs well in the indoor range.

Scaling to more complex tasks. We now apply DARC to the more complex tasks shown in Fig. 5. We define three tasks by crippling one of the joints of each robot in the target domain, but using the fully-functional robot in the source domain. We use three simulated robots taken from OpenAI Gym (Brockman et al., 2016): 7

Figure 5: **Environments**: broken reacher, broken half cheetah, broken ant, and half cheetah obstacle.

DOF reacher, half cheetah, and ant. The broken reacher is based on the task described by Vemula

Figure 6: **DARC compensates for crippled robots and obstacles**: We apply DARC to four continuous control tasks: three tasks (broken reacher, half cheetah, and ant) which are crippled in the target domain but not the source domain, and one task (half cheetah obstacle) where the source domain omits the obstacle from the target domain. Note that naïvely ignoring the shift in dynamics (green dashed line) performs quite poorly, while directly learning on the crippled robot requires an order of magnitude more experience than our method.

et al. (2020). We also include a task where the shift in dynamics is external to the robot, by modifying the cheetah task to reward the agent for running both forward and backwards. It is easier to learn to run backwards, an obstacle in the target domain prevents the agent from running backwards.

We compare our method to eight baselines. **RL on Source** and **RL on Target** directly perform RL on the source and target domains, respectively. The **Finetuning** baseline takes the result of running RL on the source domain, and further finetunes the agent on the target domain. The **Importance Weighting** baseline performs RL on importance-weighted samples from the source domain; the importance weights are $\exp(\Delta r)$. Since our method performs $10\times$ more gradient updates per environment step in the source domain, we trained a version of the RL on target baseline likewise takes $10\times$ gradient updates.. We compared against two recent model-based RL methods: **MBPO** (Janner et al., 2019) and **PETS** (Chua et al., 2018). Finally, we also compared against **MATL** (Wulfmeier et al., 2017b), which is similar in spirit to our method but uses a different modified reward.

We show the results of this experiment in Fig. 6, plotting the reward on the *target* domain as a function of the number of transitions in the *target* domain. On all tasks, the RL on source baseline (shown as a dashed line because it observes no target transitions) performs considerably worse than the optimal policy from RL on the target domain, suggesting that good policies for the source domain are suboptimal for the target domain. Nonetheless, on three of the four tasks our method matches (or even surpasses) the asymptotic performance of doing RL on the target domain, despite never doing RL on experience from the target domain, and despite observing 5 - 10x less experience from the target domain. On the broken reacher and broken half cheetah tasks, finetuning on the target domain performs on par with our method. On the simpler broken reacher task, just doing RL on the target domain with a large number of gradient steps works quite well (we did not tune this parameter for our method). While the model-based baselines (PETS and MBPO) also performed well on for low-dimensional tasks (broken reacher, broken half cheetah), the perform quite poorly on more challenging tasks like broken ant, supporting our intuition that classification is easier than learning a dynamics model in high dimensional tasks. Finally, DARC outperforms MARL on all tasks. We include additional ablation experiments in Appendix D.1.

To gain more intuition for our method, we recorded the reward correction Δr throughout training on the broken reacher environment. In this experiment, we ran RL on the source domain for 100k steps before switching to our method. Said another way, we ignored Δr for the first 100k steps of training. As shown in Fig. 7, Δr steadily decreases during these first 100k steps, suggesting that the agent is learning a strategy that takes transitions where the source domain and target domain have different dynamics: the agent is making use of its broken joint. After 100k steps, when we maximize the combination of task reward and Δr, we observe that Δr increases, so the agent's transitions in the source domain are increasingly consistent

Figure 7: Without the reward correction, the agent takes transitions where the source domain and target domains are dissimilar; after adding the reward correction, the agent's transitions in the source domain are increasingly likely under the target domain.

with target domain dynamics. After around 1e6 training steps Δr is zero: the agent has learned a strategy that uses transitions that are indistinguishable between the source and target domains.

Safety emerges from domain adaptation to the termination condition. In many safety-critical applications, the real-world and simulator have different safegaurds, which kick in to stop the agent and terminate the episode. For an agent to effectively transfer from the simulator to the real world, it cannot rely on safeguards which are present in one domain but not the other. Since this termination condition is part of the dynamics (White, 2017), we can readily apply DARC to this setting.

Figure 8: Our method accounts for domain shift in the termination condition, causing the agent to avoid transitions that cause termination in the target domain.

We use the humanoid shown in Fig. 8 for this experiment and set the task reward to 0. In the source domain episodes have a fixed length of 300 steps; in the target domain the episode terminates when the robot falls. The scenario mimics the real-world setting where robots have freedom to practice in a safe, cushioned, practice facility, but are preemptively stopped when they try to take unsafe actions in the real world. Our aim is for the agent to learn to avoid unsafe transitions in the source domain that would result in episode termination in the target domain. As shown in Fig. 8, our method learns to remain standing for nearly the entire episode. As expected, baselines that maximize the zero reward on the source and target domains fall immediately. While DARC was not designed as a method for safe RL (Tamar et al., 2013; Achiam et al., 2017; Eysenbach et al., 2017; Berkenkamp et al., 2017), this experiment suggests that safety may emerge automatically from DARC, without any manual reward function design.

Comparison with Prior Transfer Learning Methods We are not the first work that modifies the reward function to perform transfer in RL (Koos et al., 2012), nor the first work to *learn* how to modify the reward function (Wulfmeier et al., 2017a). However, these prior works lack theoretical justification. In contrast, our approach maximizes a well-defined variational objective and our analysis guarantees that agents learned with our method will achieve similar rewards in the source and target domains. Our formal guarantees (Sec. 4)

Figure 9: Comparison with MATL

do not apply to MATL (Wulfmeier et al., 2017b) because their classifier is not conditioned on the action. Indeed, our results on the four tasks in Fig. 6 indicate that DARC ourperforms MATL on all tasks. To highlight this difference, we compared DARC and MATL on a gridworld (right), where the source and target domains differed by assigning opposite effects to the "up" and "down" in the purple state in the source and target domains. We collected data from a uniform random policy, so the *marginal* distribution $p(s_{t+1} \mid s_t)$ was the same in the source and target domains, even though the dynamics $p(s_{t+1} \mid s_t, a_t)$ where different. In this domain, MATL fails to recognize that the source and target domains are different. DARC succeeds in this task for 80% of trials while MATL succeeds for 0% of trials. We conclude the conditioning on the action, as suggested by our analysis, is especially important when using experience collected from stochastic policies.

7 DISCUSSION

In this paper, we proposed a simple, practical, and intuitive approach for domain adaptation to changing dynamics in RL. We motivate this method from a novel variational perspective on domain adaptation in RL, which suggests that we can compensate for differences in dynamics via the reward function. Moreover, we formally prove that, subject to a lightweight assumption, our method is guaranteed to yield a near-optimal policy for the target domain. Experiments on a range of control tasks show that our method can leverage the source domain to learn policies that will work well in the target domain, despite observing only a handful of transitions from the target domain.

REFERENCES

Abbas Abdolmaleki, Jost Tobias Springenberg, Yuval Tassa, Remi Munos, Nicolas Heess, and Martin Riedmiller. Maximum a posteriori policy optimisation. *arXiv preprint arXiv:1806.06920*, 2018.

Joshua Achiam, David Held, Aviv Tamar, and Pieter Abbeel. Constrained policy optimization. In *Proceedings of the 34th International Conference on Machine Learning-Volume 70*, pp. 22–31. JMLR. org, 2017.

Felix Berkenkamp, Matteo Turchetta, Angela Schoellig, and Andreas Krause. Safe model-based reinforcement learning with stability guarantees. In *Advances in neural information processing systems*, pp. 908–918, 2017.

Steffen Bickel, Michael Brückner, and Tobias Scheffer. Discriminative learning for differing training and test distributions. In *Proceedings of the 24th international conference on Machine learning*, pp. 81–88, 2007.

Konstantinos Bousmalis, Alex Irpan, Paul Wohlhart, Yunfei Bai, Matthew Kelcey, Mrinal Kalakrishnan, Laura Downs, Julian Ibarz, Peter Pastor, Kurt Konolige, et al. Using simulation and domain adaptation to improve efficiency of deep robotic grasping. In *2018 IEEE International Conference on Robotics and Automation (ICRA)*, pp. 4243–4250. IEEE, 2018.

Greg Brockman, Vicki Cheung, Ludwig Pettersson, Jonas Schneider, John Schulman, Jie Tang, and Wojciech Zaremba. Openai gym. *arXiv preprint arXiv:1606.01540*, 2016.

Yevgen Chebotar, Ankur Handa, Viktor Makoviychuk, Miles Macklin, Jan Issac, Nathan Ratliff, and Dieter Fox. Closing the sim-to-real loop: Adapting simulation randomization with real world experience. In *2019 International Conference on Robotics and Automation (ICRA)*, pp. 8973–8979. IEEE, 2019.

Kurtland Chua, Roberto Calandra, Rowan McAllister, and Sergey Levine. Deep reinforcement learning in a handful of trials using probabilistic dynamics models. In *Advances in Neural Information Processing Systems*, pp. 4754–4765, 2018.

Ignasi Clavera, Anusha Nagabandi, Ronald S Fearing, Pieter Abbeel, Sergey Levine, and Chelsea Finn. Learning to adapt: Meta-learning for model-based control. *arXiv preprint arXiv:1803.11347*, 3, 2018.

Corinna Cortes and Mehryar Mohri. Domain adaptation and sample bias correction theory and algorithm for regression. *Theoretical Computer Science*, 519:103–126, 2014.

Gabriela Csurka. Domain adaptation for visual applications: A comprehensive survey. *arXiv preprint arXiv:1702.05374*, 2017.

Mark Cutler, Thomas J Walsh, and Jonathan P How. Reinforcement learning with multi-fidelity simulators. In *2014 IEEE International Conference on Robotics and Automation (ICRA)*, pp. 3888–3895. IEEE, 2014.

Christoph Dann, Gerhard Neumann, Jan Peters, et al. Policy evaluation with temporal differences: A survey and comparison. *Journal of Machine Learning Research*, 15:809–883, 2014.

Marc Deisenroth and Carl E Rasmussen. Pilco: A model-based and data-efficient approach to policy search. In *Proceedings of the 28th International Conference on machine learning (ICML-11)*, pp. 465–472, 2011.

Yan Duan, John Schulman, Xi Chen, Peter L Bartlett, Ilya Sutskever, and Pieter Abbeel. Rl^2: Fast reinforcement learning via slow reinforcement learning. *arXiv preprint arXiv:1611.02779*, 2016.

Miroslav Dudík, John Langford, and Lihong Li. Doubly robust policy evaluation and learning. *arXiv preprint arXiv:1103.4601*, 2011.

Benjamin Eysenbach, Shixiang Gu, Julian Ibarz, and Sergey Levine. Leave no trace: Learning to reset for safe and autonomous reinforcement learning. *arXiv preprint arXiv:1711.06782*, 2017.

Alon Farchy, Samuel Barrett, Patrick MacAlpine, and Peter Stone. Humanoid robots learning to walk faster: From the real world to simulation and back. In *Proceedings of the 2013 international conference on Autonomous agents and multi-agent systems*, pp. 39–46, 2013.

AA Feldbaum. Dual control theory. i. *Avtomatika i Telemekhanika*, 21(9):1240–1249, 1960.

Basura Fernando, Amaury Habrard, Marc Sebban, and Tinne Tuytelaars. Unsupervised visual domain adaptation using subspace alignment. In *Proceedings of the IEEE international conference on computer vision*, pp. 2960–2967, 2013.

Scott Fujimoto, David Meger, and Doina Precup. Off-policy deep reinforcement learning without exploration. *arXiv preprint arXiv:1812.02900*, 2018.

Shani Gamrian and Yoav Goldberg. Transfer learning for related reinforcement learning tasks via image-to-image translation. *arXiv preprint arXiv:1806.07377*, 2018.

Yaroslav Ganin, Evgeniya Ustinova, Hana Ajakan, Pascal Germain, Hugo Larochelle, François Laviolette, Mario Marchand, and Victor Lempitsky. Domain-adversarial training of neural networks. *The Journal of Machine Learning Research*, 17(1):2096–2030, 2016.

Sergio Guadarrama, Anoop Korattikara, Oscar Ramirez, Pablo Castro, Ethan Holly, Sam Fishman, Ke Wang, Ekaterina Gonina, Chris Harris, Vincent Vanhoucke, et al. Tf-agents: A library for reinforcement learning in tensorflow, 2018.

Tuomas Haarnoja, Aurick Zhou, Pieter Abbeel, and Sergey Levine. Soft actor-critic: Off-policy maximum entropy deep reinforcement learning with a stochastic actor. *arXiv preprint arXiv:1801.01290*, 2018.

Danijar Hafner, Timothy Lillicrap, Ian Fischer, Ruben Villegas, David Ha, Honglak Lee, and James Davidson. Learning latent dynamics for planning from pixels. *arXiv preprint arXiv:1811.04551*, 2018.

Irina Higgins, Arka Pal, Andrei Rusu, Loic Matthey, Christopher Burgess, Alexander Pritzel, Matthew Botvinick, Charles Blundell, and Alexander Lerchner. Darla: Improving zero-shot transfer in reinforcement learning. In *Proceedings of the 34th International Conference on Machine Learning-Volume 70*, pp. 1480–1490. JMLR. org, 2017.

Judy Hoffman, Dequan Wang, Fisher Yu, and Trevor Darrell. Fcns in the wild: Pixel-level adversarial and constraint-based adaptation. *arXiv preprint arXiv:1612.02649*, 2016.

Michael Janner, Justin Fu, Marvin Zhang, and Sergey Levine. When to trust your model: Model-based policy optimization. In *Advances in Neural Information Processing Systems*, pp. 12498–12509, 2019.

Natasha Jaques, Shixiang Gu, Dzmitry Bahdanau, José Miguel Hernández-Lobato, Richard E Turner, and Douglas Eck. Sequence tutor: Conservative fine-tuning of sequence generation models with kl-control. In *Proceedings of the 34th International Conference on Machine Learning-Volume 70*, pp. 1645–1654. JMLR. org, 2017.

Hilbert J Kappen. Path integrals and symmetry breaking for optimal control theory. *Journal of statistical mechanics: theory and experiment*, 2005(11):P11011, 2005.

Taylor W Killian, Samuel Daulton, George Konidaris, and Finale Doshi-Velez. Robust and efficient transfer learning with hidden parameter markov decision processes. In *Advances in neural information processing systems*, pp. 6250–6261, 2017.

Diederik P Kingma and Jimmy Ba. Adam: A method for stochastic optimization. *arXiv preprint arXiv:1412.6980*, 2014.

Daphne Koller and Nir Friedman. *Probabilistic graphical models: principles and techniques*. MIT press, 2009.

Sylvain Koos, Jean-Baptiste Mouret, and Stéphane Doncieux. The transferability approach: Crossing the reality gap in evolutionary robotics. *IEEE Transactions on Evolutionary Computation*, 17 (1):122–145, 2012.

Wouter Marco Kouw and Marco Loog. A review of domain adaptation without target labels. *IEEE transactions on pattern analysis and machine intelligence*, 2019.

Alessandro Lazaric. *Knowledge transfer in reinforcement learning*. PhD thesis, PhD thesis, Politecnico di Milano, 2008.

Sergey Levine. Reinforcement learning and control as probabilistic inference: Tutorial and review. *arXiv preprint arXiv:1805.00909*, 2018.

Sergey Levine, Peter Pastor, Alex Krizhevsky, Julian Ibarz, and Deirdre Quillen. Learning hand-eye coordination for robotic grasping with deep learning and large-scale data collection. *The International Journal of Robotics Research*, 37(4-5):421–436, 2018.

Zachary C Lipton, Yu-Xiang Wang, and Alex Smola. Detecting and correcting for label shift with black box predictors. *arXiv preprint arXiv:1802.03916*, 2018.

Lennart Ljung. System identification. *Wiley encyclopedia of electrical and electronics engineering*, pp. 1–19, 1999.

Michael G Madden and Tom Howley. Transfer of experience between reinforcement learning environments with progressive difficulty. *Artificial Intelligence Review*, 21(3-4):375–398, 2004.

Oliver Mihatsch and Ralph Neuneier. Risk-sensitive reinforcement learning. *Machine learning*, 49 (2-3):267–290, 2002.

Nikhil Mishra, Mostafa Rohaninejad, Xi Chen, and Pieter Abbeel. A simple neural attentive meta-learner. *arXiv preprint arXiv:1707.03141*, 2017.

Shakir Mohamed and Balaji Lakshminarayanan. Learning in implicit generative models. *arXiv preprint arXiv:1610.03483*, 2016.

Rémi Munos, Tom Stepleton, Anna Harutyunyan, and Marc Bellemare. Safe and efficient off-policy reinforcement learning. In *Advances in Neural Information Processing Systems*, pp. 1054–1062, 2016.

Xue Bin Peng, Marcin Andrychowicz, Wojciech Zaremba, and Pieter Abbeel. Sim-to-real transfer of robotic control with dynamics randomization. In *2018 IEEE international conference on robotics and automation (ICRA)*, pp. 1–8. IEEE, 2018.

Theodore J Perkins, Doina Precup, et al. Using options for knowledge transfer in reinforcement learning. *University of Massachusetts, Amherst, MA, USA, Tech. Rep*, 1999.

Aravind Rajeswaran, Sarvjeet Ghotra, Balaraman Ravindran, and Sergey Levine. Epopt: Learning robust neural network policies using model ensembles. *arXiv preprint arXiv:1610.01283*, 2016.

Kate Rakelly, Aurick Zhou, Chelsea Finn, Sergey Levine, and Deirdre Quillen. Efficient off-policy meta-reinforcement learning via probabilistic context variables. In *International conference on machine learning*, pp. 5331–5340, 2019.

Balaraman Ravindran and Andrew G Barto. *An algebraic approach to abstraction in reinforcement learning*. PhD thesis, University of Massachusetts at Amherst, 2004.

Konrad Rawlik, Marc Toussaint, and Sethu Vijayakumar. On stochastic optimal control and reinforcement learning by approximate inference. In *Twenty-Third International Joint Conference on Artificial Intelligence*, 2013.

Stephane Ross and J Andrew Bagnell. Agnostic system identification for model-based reinforcement learning. *arXiv preprint arXiv:1203.1007*, 2012.

Fereshteh Sadeghi and Sergey Levine. Cad2rl: Real single-image flight without a single real image. *arXiv preprint arXiv:1611.04201*, 2016.

Sosale Shankara Sastry and Alberto Isidori. Adaptive control of linearizable systems. *IEEE Transactions on Automatic Control*, 34(11):1123–1131, 1989.

John Schulman, Filip Wolski, Prafulla Dhariwal, Alec Radford, and Oleg Klimov. Proximal policy optimization algorithms. *arXiv preprint arXiv:1707.06347*, 2017.

Oliver G Selfridge, Richard S Sutton, and Andrew G Barto. Training and tracking in robotics. In *IJCAI*, pp. 670–672, 1985.

Alexander A Sherstov and Peter Stone. Improving action selection in mdp's via knowledge transfer. In *AAAI*, volume 5, pp. 1024–1029, 2005.

Casper Kaae Sønderby, Jose Caballero, Lucas Theis, Wenzhe Shi, and Ferenc Huszár. Amortised map inference for image super-resolution. *arXiv preprint arXiv:1610.04490*, 2016.

H Francis Song, Abbas Abdolmaleki, Jost Tobias Springenberg, Aidan Clark, Hubert Soyer, Jack W Rae, Seb Noury, Arun Ahuja, Siqi Liu, Dhruva Tirumala, et al. V-mpo: On-policy maximum a posteriori policy optimization for discrete and continuous control. *arXiv preprint arXiv:1909.12238*, 2019.

Funlade T Sunmola and Jeremy L Wyatt. Model transfer for markov decision tasks via parameter matching. In *Proceedings of the 25th Workshop of the UK Planning and Scheduling Special Interest Group (PlanSIG 2006)*, pp. 246–252, 2006.

Aviv Tamar, Huan Xu, and Shie Mannor. Scaling up robust mdps by reinforcement learning. *arXiv preprint arXiv:1306.6189*, 2013.

Jie Tan, Zhaoming Xie, Byron Boots, and C Karen Liu. Simulation-based design of dynamic controllers for humanoid balancing. In *2016 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS)*, pp. 2729–2736. IEEE, 2016.

Fumihide Tanaka and Masayuki Yamamura. Multitask reinforcement learning on the distribution of mdps. In *Proceedings 2003 IEEE International Symposium on Computational Intelligence in Robotics and Automation. Computational Intelligence in Robotics and Automation for the New Millennium (Cat. No. 03EX694)*, volume 3, pp. 1108–1113. IEEE, 2003.

Marko Tanaskovic, Lorenzo Fagiano, Roy Smith, Paul Goulart, and Manfred Morari. Adaptive model predictive control for constrained linear systems. In *2013 European Control Conference (ECC)*, pp. 382–387. IEEE, 2013.

Matthew E Taylor and Peter Stone. Transfer learning for reinforcement learning domains: A survey. *Journal of Machine Learning Research*, 10(7), 2009.

Louis C Tiao, Edwin V Bonilla, and Fabio Ramos. Cycle-consistent adversarial learning as approximate bayesian inference. *arXiv preprint arXiv:1806.01771*, 2018.

Josh Tobin, Rachel Fong, Alex Ray, Jonas Schneider, Wojciech Zaremba, and Pieter Abbeel. Domain randomization for transferring deep neural networks from simulation to the real world. In *2017 IEEE/RSJ international conference on intelligent robots and systems (IROS)*, pp. 23–30. IEEE, 2017.

Emanuel Todorov. Linearly-solvable markov decision problems. In *Advances in neural information processing systems*, pp. 1369–1376, 2007.

Marc Toussaint. Robot trajectory optimization using approximate inference. In *Proceedings of the 26th annual international conference on machine learning*, pp. 1049–1056, 2009.

Masatoshi Uehara, Issei Sato, Masahiro Suzuki, Kotaro Nakayama, and Yutaka Matsuo. Generative adversarial nets from a density ratio estimation perspective. *arXiv preprint arXiv:1610.02920*, 2016.

Anirudh Vemula, Yash Oza, J Andrew Bagnell, and Maxim Likhachev. Planning and execution using inaccurate models with provable guarantees. *arXiv preprint arXiv:2003.04394*, 2020.

Paul J Werbos. Neural networks for control and system identification. In *Proceedings of the 28th IEEE Conference on Decision and Control,*, pp. 260–265. IEEE, 1989.

Martha White. Unifying task specification in reinforcement learning. In *Proceedings of the 34th International Conference on Machine Learning-Volume 70*, pp. 3742–3750. JMLR. org, 2017.

Grady Williams, Andrew Aldrich, and Evangelos Theodorou. Model predictive path integral control using covariance variable importance sampling. *arXiv preprint arXiv:1509.01149*, 2015.

Björn Wittenmark. Adaptive dual control methods: An overview. In *Adaptive Systems in Control and Signal Processing 1995*, pp. 67–72. Elsevier, 1995.

Markus Wulfmeier, Alex Bewley, and Ingmar Posner. Addressing appearance change in outdoor robotics with adversarial domain adaptation. In *2017 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS)*, pp. 1551–1558. IEEE, 2017a.

Markus Wulfmeier, Ingmar Posner, and Pieter Abbeel. Mutual alignment transfer learning. *arXiv preprint arXiv:1707.07907*, 2017b.

Wenhao Yu, Jie Tan, C Karen Liu, and Greg Turk. Preparing for the unknown: Learning a universal policy with online system identification. *arXiv preprint arXiv:1702.02453*, 2017.

Bianca Zadrozny. Learning and evaluating classifiers under sample selection bias. In *Proceedings of the twenty-first international conference on Machine learning*, pp. 114, 2004.

Jun-Yan Zhu, Taesung Park, Phillip Isola, and Alexei A Efros. Unpaired image-to-image translation using cycle-consistent adversarial networks. In *Proceedings of the IEEE international conference on computer vision*, pp. 2223–2232, 2017a.

Shaojun Zhu, Andrew Kimmel, Kostas E Bekris, and Abdeslam Boularias. Fast model identification via physics engines for data-efficient policy search. *arXiv preprint arXiv:1710.08893*, 2017b.

Brian D. Ziebart. *Modeling Purposeful Adaptive Behavior with the Principle of Maximum Causal Entropy*. PhD thesis, Carnegie Mellon University, 2010.

A ADDITIONAL INTERPRETATIONS OF THE REWARD CORRECTION

This section presents four additional interpretations of the reward correction, Δr.

A.1 CODING THEORY

The reward correction Δr can also be understood from the perspective of coding theory. Suppose that we use a data-efficient replay buffer that exploits that fact that the next state s_{t+1} is highly redundant with the current state and action, s_t, a_t. If we assume that the replay buffer compression has been optimized to store transitions from the target environment, (negative) Δr is the number of additional bits (per transition) needed for our source replay buffer, as compared with our target replay buffer. Thus, an agent which maximizes Δr will seek those transitions that can be encoded most efficiently, minimizing the size of the source replay buffer.

A.2 MUTUAL INFORMATION

We can gain more intuition in the modified reward by writing the expected value of Δr from Eq. 3 in terms of mutual information:

$$\mathbb{E}[\Delta r(s_t, a_t, s_{t+1})] = I(s_{t+1}; \text{target} \mid s_t, a_t) - I(s_{t+1}; \text{source} \mid s_t, a_t).$$

The mutual information $I(s_{t+1}; \text{target} \mid s_t, a_t)$ reflects how much better you can predict the next state if you know that you are interacting with the target domain, instead of the source domain. Our approach does exactly this, rewarding the agent for taking transitions that provide information about the target domain while penalizing transitions that hint to the agent that it is interacting with a source domain rather than the target domain: we don't want our are agent to find bugs in the Matrix.[1]

A.3 LOWER BOUND ON THE RISK-SENSITIVE REWARD OBJECTIVE.

While we derived DARC by minimizing a reverse KL divergence (Eq. 2), we can also show that DARC maximizes a lower bound on a risk-sensitive reward objective (Mihatsch & Neuneier, 2002):

$$\log \mathbb{E}_{\substack{s' \sim p_{\text{target}}(s'|s,a), \\ a \sim \pi(a|s)}} \left[\exp\left(\sum_t r(s_t, a_t) \right) \right]$$

$$= \log \mathbb{E}_{\substack{s' \sim p_{\text{source}}(s'|s,a), \\ a \sim \pi(a|s)}} \left[\left(\prod_t \frac{p_{\text{target}}(s_{t+1} \mid s_t, a_t)}{p_{\text{source}}(s_{t+1} \mid s_t, a_t)} \right) \exp\left(\sum_t r(s_t, a_t) \right) \right]$$

$$= \log \mathbb{E}_{\substack{s' \sim p_{\text{source}}(s'|s,a), \\ a \sim \pi(a|s)}} \left[\exp\left(\sum_t r(s_t, a_t) + \underbrace{\log p_{\text{target}}(s_{t+1} \mid s_t, a_t) - \log p_{\text{source}}(s_{t+1} \mid s_t, a_t)}_{\Delta r(s_t, a_t, s_{t+1})} \right) \right] \tag{4}$$

$$\geq \mathbb{E}_{\substack{s' \sim p_{\text{source}}(s'|s,a), \\ a \sim \pi(a|s)}} \left[\sum_t r(s_t, a_t) + \Delta r(s_t, a_t, s_{t+1}) \right]. \tag{5}$$

The inequality on the last line is an application of Jensen's inequality. One interesting question is when it would be preferable to maximize Eq. 4 rather than Eq. 5. While Eq. 5 provides a loser bound on the risk sensitive objective, empirically it may avoid the risk-seeking behavior that can be induced by risk-sensitive objectives. We leave the investigation of this trade-off as future work.

A.4 A CONSTRAINT ON DYNAMICS DISCREPANCY

Our method regularizes the policy to visit states where the transition dynamics are similar between the source domain and target domain:

$$\max_\pi \mathbb{E}_{\substack{a \sim \pi(a|s) \\ s' \sim p(s'|s,a)}} \left[\sum_t r(s_t, a_t) + \underbrace{\log p_{\text{target}}(s_{t+1} \mid s_t, a_t) - \log p_{\text{source}}(s_{t+1} \mid s_t, a_t)}_{-D_{\text{KL}}(p_{\text{source}} \,\|\, p_{\text{target}})} + \mathcal{H}_\pi[a_t \mid s_t] \right].$$

---

[1] The CMU compute cluster where we ran our experiments is also named Matrix.

This objective can equivalently be expressed as applying MaxEnt RL to only those policies which avoid exploiting the dynamics discrepancy. More precisely, the KKT conditions guarantee that there exists a positive constant $\epsilon > 0$ such that our objective is equivalent to the following constrained objective:

$$\max_{\pi \in \Pi_{\text{DARC}}} \mathbb{E}_{\substack{a \sim \pi(a|s) \\ s' \sim p(s'|s,a)}} \left[\sum_t r(s_t, a_t) + \mathcal{H}_\pi[a_t \mid s_t] \right],$$

where Π_{DARC} denotes the set of policies that do not exploit the dynamics discrepancy:

$$\Pi_{\text{DARC}} \triangleq \left\{ \pi \middle| \mathbb{E}_{\substack{a \sim \pi(a|s) \\ s' \sim p(s'|s,a)}} \left[\sum_t D_{\text{KL}}(p_{\text{source}}(s_{t+1} \mid s_t, a_t) \| p_{\text{target}}(s_{t+1} \mid s_t, a_t)) \right] \leq \epsilon \right\}. \quad (6)$$

One potential benefit of considering our method as the unconstrained objective is that it provides a principled method for increasing or decreasing the weight on the Δr term, depending on how much the policy is currently exploiting the dynamics discrepancy. We leave this investigation as future work.

B   PROOFS OF THEORETICAL GUARANTEES

In this section we present our analysis showing that maximizing the modified reward $r + \Delta r$ in the source domain yields a near-optimal policy for the target domain, subject to Assumption 1. To start, we show that maximizing the modified reward in the source domain is equivalent to maximizing the unmodified reward, subject to the constraint that the policy not exploit the dynamics:

Lemma B.1. *Let a reward function $r(s,a)$, source dynamics $p_{source}(s' \mid s, a)$, and target dynamics $p_{target}(s' \mid s, a)$ be given. Then there exists $\epsilon > 0$ such the optimization problem in Eq. 2 is equivalent to*

$$\max_{\pi \in \Pi_{no\ exploit}} \mathbb{E}_{p_{source}, \pi} \left[\sum r(s_t, a_t) + \mathcal{H}_\pi[a_t \mid s_t] \right],$$

where $\Pi_{no\ exploit}$ denotes the set of policies that do not exploit the dynamics:

$$\Pi_{no\ exploit} \triangleq \left\{ \mathbb{E}_{\substack{a \sim \pi(a|s) \\ s' \sim p(s'|s,a)}} \left[\sum_t D_{\text{KL}}(p_{source}(s_{t+1} \mid s_t, a_t) \| p_{target}(s_{t+1} \mid s_t, a_t)) \right] \leq \epsilon \right\}.$$

The proof is a straightforward application of the KKT conditions. This lemma says that maximizing the modified reward can be equivalently viewed as restricting the set of policies to those that do not exploit the dynamics. Next, we will show that policies that do not exploit the dynamics have an expected (entropy-regularized) reward that is similar in the source and target domains:

Lemma B.2. *Let policy $\pi \in \Pi_{no\ exploit}$ be given, and let R_{max} be the maximum (entropy-regularized) return of any trajectory. Then the following inequality holds:*

$$\left| \mathbb{E}_{p_{source}} \left[\sum r(s_t, a_t) + \mathcal{H}_\pi[a_t \mid s_t] \right] - \mathbb{E}_{p_{source}} \left[\sum r(s_t, a_t) + \mathcal{H}_\pi[a_t \mid s_t] \right] \right| \leq 2R_{max}\sqrt{\epsilon/2}.$$

Proof. To simplify notation, define $\tilde{r}(s,a) = r(s,a) - \log \pi(a \mid s)$. We then apply Holder's inequality and Pinsker's inequality to obtain the desired result:

$$\mathbb{E}_q \left[\sum \tilde{r}(s_t, a_t) \right] - \mathbb{E}_p \left[\sum \tilde{r}(s_t, a_t) \right] = \sum_\tau (p_{\text{source}}(\tau) - p_{\text{target}}(\tau)) \left(\sum \tilde{r}(s_t, a_t) \right)$$

$$\leq \| \sum \tilde{r}(s_t, a_t) \|_\infty \cdot \| q(\tau) - p(\tau) \|_1$$

$$\leq \left(\max_\tau \sum r(s_t, a_t) \right) \cdot 2\sqrt{\frac{1}{2} D_{\text{KL}}(p_{\text{source}}(\tau) \| p_{\text{target}}(\tau))}$$

$$\leq 2R_{\max}\sqrt{\epsilon/2}.$$

$\square$

We restate our main result:

Theorem B.3. *Let π^*_{DARC} be the policy that maximizes the modified (entropy-regularized) reward in the source domain, let π^* be the policy that maximizes the (unmodified, entropy-regularized) reward in the target domain, and assume that π^* satisfies Assumption 1. Then π^*_{DARC} receives near-optimal (entropy-regularized) reward on the target domain:*

$$\mathbb{E}_{p_{target},\pi^*_{DARC}}\left[\sum r(s_t,a_t) + \mathcal{H}[a_t \mid s_t]\right] \geq \mathbb{E}_{p_{target},\pi^*}\left[\sum r(s_t,a_t) + \mathcal{H}[a_t \mid s_t]\right] - 4R_{max}\sqrt{\epsilon/2}.$$

Proof. Assumption 1 guarantees that the optimal policy for the target domain, π^*, lies within $\Pi_{\text{no exploit}}$. Among all policies in $\Pi_{\text{no exploit}}$, π^*_{DARC} is (by definition) the one that receives highest reward on the source dynamics, so

$$\mathbb{E}_{p_{\text{source}},\pi^*_{\text{DARC}}}\left[\sum r(s_t,a_t) + \mathcal{H}[a_t \mid s_t]\right] \geq \mathbb{E}_{p_{\text{source}},\pi^*}\left[\sum r(s_t,a_t) + \mathcal{H}[a_t \mid s_t]\right].$$

Since the both π^*_{DARC} and π^* lie inside the constraint set, Lemma B.2 dictates that their rewards on the target domain differ by at most $2R_{\max}\sqrt{\epsilon/2}$ from their source domain rewards. In the worst case, the reward for π^*_{DARC} decreases by this amount and the reward for π^* increases by this amount:

$$\mathbb{E}_{p_{\text{source}},\pi^*_{\text{DARC}}}\left[\sum r(s_t,a_t) + \mathcal{H}[a_t \mid s_t]\right] \leq \mathbb{E}_{p_{\text{target}},\pi^*_{\text{DARC}}}\left[\sum r(s_t,a_t) + \mathcal{H}[a_t \mid s_t]\right] + 2R_{\max}\sqrt{\epsilon/2}$$

$$\mathbb{E}_{p_{\text{source}},\pi^*}\left[\sum r(s_t,a_t) + \mathcal{H}[a_t \mid s_t]\right] \geq \mathbb{E}_{p_{\text{target}},\pi^*}\left[\sum r(s_t,a_t) + \mathcal{H}[a_t \mid s_t]\right] - 2R_{\max}\sqrt{\epsilon/2}$$

Substituting these inequalities on the LHS and RHS of Eq. B and rearranging terms, we obtain the desired result. $\qquad\square$

C   THE SPECIAL CASE OF AN OBSERVATION MODEL

To highlight the relationship between domain adaptation of dynamics versus observations, we now consider a special case. In this subsection, we will assume that the state $s_t \triangleq (z_t, o_t)$ is a combination of the system latent state z_t (e.g., the poses of all objects in a scene) and an observation o_t (e.g., a camera observation). We will define $q(o_t \mid z_t)$ and $p(o_t \mid z_t)$ as the *observation models* for the source and target domains. In this special case, we can decompose the KL objective (Eq. 2) into three terms:

$$D_{\text{KL}}(q \parallel p) = -\mathbb{E}_q\left[\sum_t \underbrace{r(s_t,a_t) + \mathcal{H}_\pi[a_t \mid s_t]}_{\text{MaxEnt RL objective}} + \underbrace{\log p_{\text{target}}(o_t \mid z_t) - \log p_{\text{source}}(o_t \mid z_t)}_{\text{Observation Adaptation}}\right.$$

$$\left. + \underbrace{\log p_{\text{target}}(z_{t+1} \mid z_t, a_t) - \log p_{\text{source}}(z_{t+1} \mid z_t, a_t)}_{\text{Dynamics Adaptation}}\right].$$

Prior methods that perform observation adaptation (Bousmalis et al., 2018; Gamrian & Goldberg, 2018) effectively minimize the observation adaptation term,[2] but ignore the effect of dynamics. In contrast, the Δr reward correction in our method provides one method to address both dynamics and observations. These approaches could be combined; we leave this as future work.

D   ADDITIONAL EXPERIMENTS

D.1   ABLATION EXPERIMENTS.

Our next experiment examines the importance of using two classifiers to estimate Δr. We compared our method to an ablation that does not learn the SA classifier, effectively ignoring the blue terms in Eq. 3. As shown in Fig. 10 (left), this ablation performs considerably worse than our method. Intuitively, this makes sense: we might predict that a transition came from the source domain not

---

[2]Tiao et al. (2018) show that observation adaptation using CycleGan (Zhu et al., 2017a) minimizes a Jensen-Shannon divergence. Assuming sufficiently expressive models, the Jensen-Shannon divergence and the reverse KL divergence above have the same optimum.

Figure 10: **Ablation experiments** *(Left)* DARC performs worse when only one classifier is used. *(Right)* Using input noise to regularize the classifiers boosts performance. Both plots show results for broken reacher; see Appendix D.1 for results on all environments.

Figure 11: **Importance of using two classifiers**: Results of the ablation experiment from Fig. 10 (left) on all environments.

because the next state had higher likelihood under the source dynamics, but rather because the state or action was visited more frequently in the source domain. The second classifier used in our method corrects for this distribution shift.

Finally, we examine the importance of input noise regularization in classifiers. As we observe only a handful of transitions from the target domain, we hypothesized that regularization would be important to prevent overfitting. We test this hypothesis in Fig. 10 (right) by training our method on the broken reacher environment with varying amounts of input noise. With no noise or little noise our method performs poorly (likely due to overfitting); too much noise also performs poorly (likely due to underfitting). We used a value of 1 in all our experiments, and did not tune this value. See Appendix D.1 for more plots of both ablation experiments.

E EXPERIMENT DETAILS AND HYPERPARAMETERS

Our implementation of DARC is built on top of the implementation of SAC from Guadarrama et al. (2018). Unless otherwise specified, all hyperparameters are taken from Guadarrama et al. (2018). All neural networks (actor, critics, and classifiers) have two hidden layers with 256-units each and ReLU activations. Since we ultimately will use the *difference* in the predictions of the two classifiers, we use a residual parametrization for the SAS classifier $q(\text{target} \mid s_t, a_t, s_{t+1})$. Using $f_{\text{SAS}}(s_t, a_t, s_{t+1}), f_{\text{SA}}(s_t, a_t) \in \mathbb{R}^2$ to denote the outputs of the two classifier networks, we compute the classifier predictions as follows:

$$q_{\theta_{\text{SA}}}(\cdot \mid s_t, a_t) = \text{SOFTMAX}(f_{\text{SA}}(s_t, a_t))$$
$$q_{\theta_{\text{SAS}}}(\cdot \mid s_t, a_t, s_{t+1}) = \text{SOFTMAX}(f_{\text{SAS}}(s_t, a_t, s_{t+1}) + f_{\text{SA}}(s_t, a_t))$$

For the SAS classifier we propagate gradients back through both networks parameters, θ_{SAS} and θ_{SA}. Both classifiers use Gaussian input noise with $\sigma = 1$. Optimization of all networks is done with Adam (Kingma & Ba, 2014) with a learning rate of 3e-4 and batch size of 128. Most experiments with DARC collected 1 step in the target domain every 10 steps in the source domain (i.e., $r = 10$). The one exception is the half cheetah obstacle domain, where we tried increasing r beyond 10 to 30, 100, 300, and 1000. We found a large benefit from increasing r to 30 and 100, but did not run the other experiments long enough to draw any conclusions. Fig. 6 uses $r = 30$ for half cheetah obstacle. We did not tune this parameter, and expect that tuning it would result in significant improvements in sample efficiency.

Figure 12: **Importance of regularizing the classifiers**: Results of the ablation experiment from Fig. 10 (right) on all environments.

We found that DARC was slightly more stable if we warm-started the method by applying RL on the source task *without* Δr for the first t_{warmup} iterations. We used $t_{\text{warmup}} = 1e5$ for all tasks except the broken reacher, where we used $t_{\text{warmup}} = 2e5$. This discrepancy was caused by a typo in an experiment, and subsequent experiments found that DARC is relatively robust to different values of t_{warmup}; we did not tune this parameter.

E.1 BASELINES

The **RL on Source** and **RL on Target** baselines are implemented identically to our method, with the exception that Δr is not added to the reward function. The **RL on Target (10x)** is identical to RL on Target, with the exception that we take 10 gradient steps per environment interaction (instead of 1). The **Importance Weighting** baseline estimates the importance weights as $p_{\text{target}}(s_{t+1} \mid s_t, a_t)/p_{\text{source}}(s_{t+1} \mid s_t, a_t) \approx \exp(\Delta r)$. The importance weight is used to weight transitions in the SAC actor and critic losses.

PETS (Chua et al., 2018) The **PETS** baseline is implemented using the default configurations used by (Chua et al., 2018) for the environments evaluated. The `broken-half-cheetah` environment uses the hyperparameters as used by the `half-cheetah` environment in (Chua et al., 2018). The `broken-ant` environment uses the same set of hyperparameters, namely: task horizon = 1000, number of training iterations = 300, number of planning (real) steps per iteration = 30, number of particles to be used in particle propagation methods = 20. The PETS codebase can be found at `https://github.com/kchua/handful-of-trials`.

MBPO (Janner et al., 2019) We used the authors implementation with the default hyperparameters: `https://github.com/JannerM/mbpo`. We kept the environment configurations the same as their default unmodified MuJoCo environments, except for the domain and task name. We added our custom environment xmls in `mbpo/env/assets/` folder, and their corresponding environment python files in the `mbpo/env/ folder`. Their static files were added under `mbpo/static/`. These environments can be registered as gym environments in the init file under `mbpo_odrl/mbpo/env/` or can be initialized directly in `softlearning/environments/adapters/gym adapter.py`. We set the time limit to `max_episode_steps=1000` for the Broken Half Cheetah, Broken Ant and Half Cheetah Obstacle environments and to 100 for the Broken Reacher environment.

E.2 ENVIRONMENTS

Broken Reacher This environment uses the 7DOF robot arm from the Pusher environment in OpenAI Gym. The observation space is the position and velocities of all joints and the goal. The reward function is

$$r(s, a) = -\frac{1}{2}\|s_{\text{end effector}} - s_{\text{goal}}\|_2 - \frac{1}{10}\|a\|_2^2,$$

and episodes are 100 steps long. In the target domain the 2nd joint (0-indexed) is broken: zero torque is applied to this joint, regardless of the commanded torque.

Broken Half Cheetah This environment is based on the HalfCheetah environment in OpenAI Gym. Episodes are 1000 steps long. In the target domain the 0th joint (0-indexed) is broken: zero torque is applied to this joint, regardless of the commanded torque.

Broken Ant   This environment is based on the Ant environment in OpenAI Gym. We use the standard termination condition and cap the maximum episode length at 1000 steps. In the target domain the 3rd joint (0-indexed) is broken: zero torque is applied to this joint, regardless of the commanded torque.

In all the broken joint environments, we choose which joint to break to computing which joint caused the "RL on Source" baseline to perform worst on the target domain, as compared with the "RL on Target" baseline.

Half Cheetah Obstacle   This environment is based on the HalfCheetah environment in OpenAI Gym. Episodes are 1000 steps long. We modified the standard reward function to use the absolute value in place of the velocity, resulting the following reward function:

$$r(s, a) = s_{\text{x vel}} \cdot \Delta t - \|a\|_2^2,$$

where $s_{\text{x vel}}$ is the velocity of the agent along the forward-aft axis and $\Delta t = 0.01$ is the time step of the simulator. In the target domain, we added a wall at $x = -3m$, roughly 3 meters behind the agent.

Humanoid   Used for the experiment in Fig. 8, we used a modified version of Humanoid from OpenAI Gym. The source domain modified this environment to ignore the default termination condition and instead terminate after exactly 300 time steps. The target domain uses the unmodified environment, which terminates when the agent falls.

E.3   FIGURES

Unless otherwise noted, all experiments were run with three random seeds. Figures showing learning curves (Figures 6, 10, 7, 11, and 12) plot the *mean* over the three random seeds, and also plot the results for each individual random seed with semi-transparent lines.

E.4   ARCHERY EXPERIMENT

We used a simple physics model for the archery experiment. The target was located 70m North of the agent, and wind was applied along the East-West axis. The system dynamics:

$$s_{t+1} = 70 \sin(\theta) + f/\cos(\theta)^2 \qquad \begin{cases} f \sim \mathcal{N}(\mu = 1, \sigma = 1) & \text{in the source domain} \\ f \sim \mathcal{N}(\mu = 0, \sigma = 0.3) & \text{in the target domain} \end{cases}$$

We trained the classifier by sampling $\theta \sim \mathcal{U}[-2, 2]$ (measured in degrees) for 10k episodes in the source domain and 10k episodes in the target domain. The classifier was a neural network with 1 hidden layer with 32 hidden units and ReLU activation. We optimized the classifier using the Adam optimizer with a learning rate of 3e-3 and a batch size of 1024. We trained until the validation loss increased for 3 consecutive epochs, which took 16 epochs in our experiment. We generated Fig. 4 by sampling 10k episodes for each value of θ and aggregating the rewards using $J(\theta) = \log \mathbb{E}_{p(s'|\theta)}[\exp(r(s'))]$. We found that aggregating rewards by taking the mean did not yield meaningful results, perhaps because the mean corresponds to a (possibly loose) lower bound on J (see Appendix A.3).