Fast Fourier Convolutions in Self-Supervised Neural Networks for Image Denoising

Abstract

Recently, denoising convolutional neural networks (CNN) have started to outperform classical denoising algorithms. However, CNNs performance could be constrained by the limited receptive field of regular convolution. To mitigate this problem, a new modification for CNNs was proposed: Fast Fourier Convolution (FFC). Here, a global receptive field is achieved by using Fourier Transform and convolving spectral representation. The global perception field can help CNNs to better capture dependencies in image regions that are far apart. In this work, we design multiple approaches for incorporating FFC into self-supervised neural networks for image denoising. We evaluate these approaches on three benchmark datasets and compare them with supervised and self-supervised methods. We empirically show that an FFC-enhanced denoising network achieves the state-of-the- art results on the character dataset and shows a comparable level of performance for both grayscale and color natural images.

1 Introduction

Chi et al. (2020) proposed Fast Fourier Convolution (FFC) with non-local receptive field. Unlike a regular convolution operating locally, FFCs can capture essential details of the image far apart in the spectral domain. FFC blocks can be seamlessly imputed in place of vanilla convolutions.

An FFC block is divided into two branches with local and global receptive fields. The input tensor is split channel-wise between the two paths (usually in halfs). The local branch works as a normal convolutional layer. The global branch operates in the spectral domain and carries out global updates to the input.

Multiple state-of-the-art neural networks could benefit from the use of FFC for image recognition, super-resolution (Zhang et al., 2022), segmentation (Farshad et al., 2022), large image inpainting (Suvorov et al., 2022), etc. In this work, we integrate FFCs in a self-supervised denoising framework, Noise2Same (Xie et al., 2020). We conduct an ablation study for the optimal FFC position in the U-Net (Ronneberger et al., 2015) backbone and empirically find suitable data domains for FFC application.

2 Architecture

We follow Xie et al. (2020) for the baseline U-Net implementation and explore different strategies to replace normal convolutions with FFC. We aim to keep our implementations similar to the baseline in terms of the number of parameters and overall U-shape for comparability.

FFC blocks are only reasonable to use if at least three of them are in a row (the first and last blocks are used for splitting/merging local and global channels, and middle blocks perform spectral convolutions). This conflicts with the original U-Net design with two convolutional blocks per level. We explore three different FFC U-Net designs that solve this problem.

In **Vanilla** design, we switch U-Net's down- and upsampling convolutions also with FFC blocks to provide us with three FFC blocks for each level. In **Extra Layer** design we keep the regular down- and upsampling

convolutions but add an extra convolutional layer to each level. In **Twin Pass** design, local and global channels are not merged together at the end of every level. Both spatial and spectral information flow through the network in parallel and so we do not need to worry about the number of convolutional blocks in a level. All designs are summarized in Figure 4 and can be used in U-Net's encoder/decoder (or both).

3 EXPERIMENTS

Figure 1: Visualization of testing results on HànZì dataset. We compare our best model (extra layer design with FFC encoder and decoder) against vanilla Noise2Same baseline. We see that in our model, the character is "diffusing" less to the background.

Table 1: Comparisons among denoising methods on different datasets, in terms of Peak Signal-to-Noise Ratio (PSNR). Best metrics are highlighted in bold. The extended table is in appendix.

	Methods	**Datasets**		
		ImageNet	HànZì	BSD68
	Input	9.69	6.45	20.19
Self-Supervised	Noise2Self-Donut Batson & Royer (2019)	8.62	13.29	**28.20**
	Noise2Same Xie et al. (2020)	22.26	14.38	27.95
	Noise2Same (our implementation)	**22.84**	14.83	28.14
	Extra Layer (FFC encoder & decoder)	22.65	**15.72**	28.13
	Twin Pass (FFC encoder)	22.34	15.28	28.16

We tested these designs on two natural image datasets, BSD68 (Martin et al., 2001) and ImageNet (Deng et al., 2009), and also on the Chinese character dataset HànZì (C.-L. Liu, 2011). The image denoising setup used is based on the setup used in Noise2Same paper (Xie et al., 2020).

We compare our best models with other methods in Table 1 and summarize our own results in Table 2. Denoising examples for each dataset are shown in Figures 1, 2 and 3. On BSD68, FFC models match baseline results or slightly exceed them. On ImageNet our model's performance slightly declines compared to the baseline. We compare our best-performing models to other denoising models in Table 1. We see that on HànZì our models beat current state-of-the-art models including supervised models (Table 3).

4 CONCLUSION

We tested three different FFC neural network designs for image denoising on three datasets. We observed state-of-the-art results on HànZì and comparable level of performance on natural image datasets. Among our model designs, no design was superior in all experiments. Our results suggest that FFC can improve denoising performance in some cases, and this topic is worth exploring further.

URM STATEMENT

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REFERENCES

Joshua Batson and Loic Royer. Noise2self: Blind denoising by self-supervision. In *International Conference on Machine Learning*, pp. 524–533. PMLR, 2019.

Antoni Buades, Bartomeu Coll, and Jean-Michel Morel. Non-local means denoising. *Image Processing On Line*, 1:208–212, 2011.

D.-H. Wang Q.-F. Wang C.-L. Liu, F. Yin. Casia online and offline chinese handwriting databases, proc. 11th international conference on document analysis and recognition (icdar), 2011.

Lu Chi, Borui Jiang, and Yadong Mu. Fast fourier convolution. *Advances in Neural Information Processing Systems*, 33:4479–4488, 2020.

Kostadin Dabov, Alessandro Foi, Vladimir Katkovnik, and Karen Egiazarian. Image denoising by sparse 3-d transform-domain collaborative filtering. *IEEE Transactions on image processing*, 16(8):2080–2095, 2007.

Jia Deng, Wei Dong, Richard Socher, Li-Jia Li, Kai Li, and Li Fei-Fei. Imagenet: A large-scale hierarchical image database. In *2009 IEEE conference on computer vision and pattern recognition*, pp. 248–255. Ieee, 2009.

Azade Farshad, Yousef Yeganeh, Peter Gehlbach, and Nassir Navab. Y-net: A spatiospectral dual-encoder network for medical image segmentation. In *Medical Image Computing and Computer Assisted Intervention–MICCAI 2022: 25th International Conference, Singapore, September 18–22, 2022, Proceedings, Part II*, pp. 582–592. Springer, 2022.

Diederik P Kingma and Jimmy Ba. Adam: A method for stochastic optimization. *arXiv preprint arXiv:1412.6980*, 2014.

Alexander Krull, Tim-Oliver Buchholz, and Florian Jug. Noise2void-learning denoising from single noisy images. In *Proceedings of the IEEE Conference on Computer Vision and Pattern Recognition*, pp. 2129–2137, 2019.

Jaakko Lehtinen, Jacob Munkberg, Jon Hasselgren, Samuli Laine, Tero Karras, Miika Aittala, and Timo Aila. Noise2noise: Learning image restoration without clean data. *arXiv preprint arXiv:1803.04189*, 2018.

D. Martin, C. Fowlkes, D. Tal, and J. Malik. A database of human segmented natural images and its application to evaluating segmentation algorithms and measuring ecological statistics. In *Proc. 8th Int'l Conf. Computer Vision*, volume 2, pp. 416–423, July 2001.

Adam Paszke, Sam Gross, Francisco Massa, Adam Lerer, James Bradbury, Gregory Chanan, Trevor Killeen, Zeming Lin, Natalia Gimelshein, Luca Antiga, et al. Pytorch: An imperative style, high-performance deep learning library. In *Advances in neural information processing systems*, pp. 8026–8037, 2019.

Olaf Ronneberger, Philipp Fischer, and Thomas Brox. U-net: Convolutional networks for biomedical image segmentation. In *International Conference on Medical image computing and computer-assisted intervention*, pp. 234–241. Springer, 2015.

Roman Suvorov, Elizaveta Logacheva, Anton Mashikhin, Anastasia Remizova, Arsenii Ashukha, Aleksei Silvestrov, Naejin Kong, Harshith Goka, Kiwoong Park, and Victor Lempitsky. Resolution-robust large mask inpainting with fourier convolutions. In *Proceedings of the IEEE/CVF winter conference on applications of computer vision*, pp. 2149–2159, 2022.

Yaochen Xie, Zhengyang Wang, and Shuiwang Ji. Noise2same: Optimizing a self-supervised bound for image denoising. *Advances in Neural Information Processing Systems*, 33:20320–20330, 2020.

Dafeng Zhang, Feiyu Huang, Shizhuo Liu, Xiaobing Wang, and Zhezhu Jin. Swinfir: Revisiting the swinir with fast fourier convolution and improved training for image super-resolution. *arXiv preprint arXiv:2208.11247*, 2022.

A   TRAINING SETUP

All neural networks were implemented in PyTorch Paszke et al. (2019) and were trained on Tesla V100-PCIE-16GB or V100-SXM2-32GB GPUs. Training consisted of 80 000 iterations for BSD68 and 50 000 iterations for other datasets. We used batch size of 64 for each dataset and Adam optimizer (Kingma & Ba, 2014) with learning rate of 4×10^{-4}.

For models where U-Net's skip connection would merge global channels to local or vice versa, we added a 1×1 convolution so that model could better learn how to mix these channels. To address deviations from the *Noise2Same* design, we also added different baseline models with an extra layer in residual block or with 1×1 skip convolution (see Table 2).The ratio of global channels α was fixed to 0.5 for the FFC models.

B   DENOISING EXAMPLES

Figure 2: Visualization of testing results on BSD68 dataset. We compare one of our best models (twin pass without FFC decoder) against vanilla *Noise2Same* baseline.

Figure 3: Visualization of testing results on Imagenet dataset. We compare our best model (extra layer design with FFC encoder and decoder) against vanilla *Noise2Same* baseline.

C ABLATION STUDY & EXTENDED COMPARISON WITH OTHER METHODS

Table 2: Ablation study among different denoising FFC designs on different datasets, in terms of Peak Signal-to-noise Ratio (PSNR). Bold numbers indicate best performance for the dataset. Checkmarks indicate what components are present in the network. Different designs are ordered into three groups: designs which don't need 1×1 skip convolution, designs which need it and finally extra layer designs (also no need for 1×1 convolution). Baseline for each group is in top row. Parameter count and average inference time for a single 64×64 image is also given for networks.

ID	FFC encoder	FFC decoder	extra layer	twin pass	1x1 skip conv	ImageNet	Hanzi	BSD68	Params	Inference time (ms)
1						22.84	14.83	28.14	5.8M	3.68
2	✓					22.34	15.19	**28.16**	5.5M	10.04
3	✓	✓		✓		22.19	15.21	28.13	4.4M	17.38
4					✓	22.81	14.84	28.13	6.0M	5.35
5	✓	✓			✓	22.49	15.18	**28.16**	5.4M	14.20
6	✓			✓	✓	22.34	15.28	**28.16**	5.3M	11.46
7			✓			**23.06**	15.42	**28.16**	7.9M	6.39
8	✓	✓	✓			22.65	**15.72**	28.13	7.6M	13.67
9	✓		✓			22.39	15.04	28.09	7.6M	9.71
Noisy input						9.69	6.45	20.19	-	-

Table 3: Comparisons among denoising methods on different datasets, in terms of Peak Signal-to-Noise Ratio (PSNR). *Noise2Self-Noise* and *Noise2Self-Donut* refer to two masking strategies mentioned in Batson & Royer (2019), where the original results presented in Batson & Royer (2019) are produced by the noise masking. Bold numbers indicate the best performance among self-supervised methods.

		Datasets		
	Methods	ImageNet	HànZì	BSD68
Traditional	Input	9.69	6.45	20.19
	NLM Buades et al. (2011)	18.04	8.41	22.73
	BM3D Dabov et al. (2007)	18.74	10.90	28.59
Supervised	Noise2True	23.39	15.66	29.06
	Noise2Noise Lehtinen et al. (2018)	23.27	14.30	28.86
Self-Supervised	Noise2Void Krull et al. (2019)	21.36	13.72	27.71
	Noise2Self-Noise Batson & Royer (2019)	20.38	13.94	26.98
	Noise2Self-Donut Batson & Royer (2019)	8.62	13.29	**28.20**
	Noise2Same Xie et al. (2020)	22.26	14.38	27.95
	Noise2Same (ours)	**22.84**	14.83	28.14
	Extra Layer (enc&dec)	22.65	**15.72**	28.13
	Twin Pass (enc)	22.34	15.28	28.16

D   FFC DESIGNS VISUALIZED

Figure 4: (a) Vanilla FFC design. (b) Extra Layer design. (c) Twin Pass design. All are modified residual blocks from U-Net encoder. Decoder designs are mirrored. Residual block shortcuts are not included in the figures.