Curiosity-Driven Exploration via Temporal Contrastive Learning

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Abstract

Effective exploration in reinforcement learning requires keeping track not just of where the agent has been, but also of how the agent thinks about and represents the world: an agent should explore states that enable it to learn powerful representations. Temporal representations can include the information required to solve any potential task while avoiding the computational cost of reconstruction. In this paper, we propose an exploration method that uses temporal contrastive representations to drive exploration, maximizing coverage *as seen through the lens of these temporal representations.* We demonstrate complex exploration behaviors in locomotion, manipulation, and embodied-AI tasks, revealing previously unknown capabilities and behaviors once achievable only via extrinsic rewards.

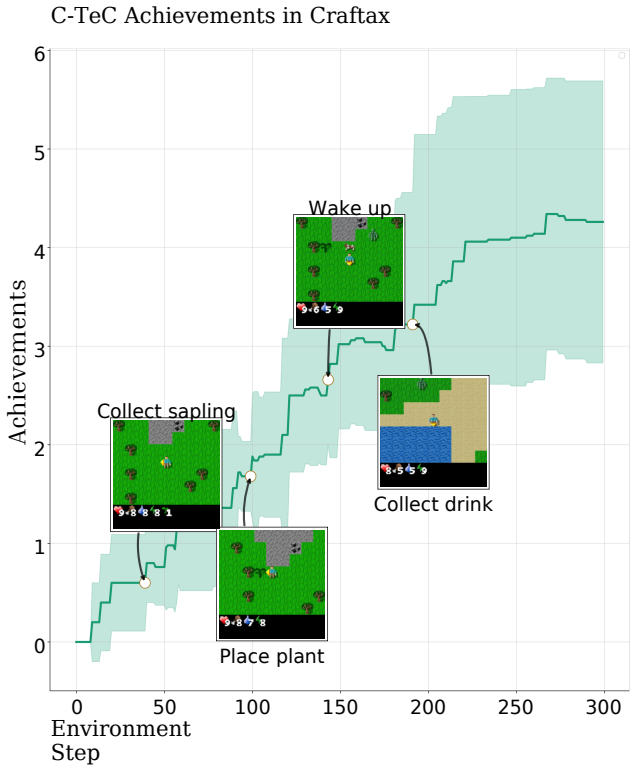

Figure 1: **C-TeC Achievements.** C-TeC unlocks interesting achievements in Craftax-Classic; the plot shows some unlocked achievements during an evaluation episode.

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1 Introduction

Exploration remains a key challenge in reinforcement learning (RL), especially in tasks that demand reasoning over increasingly long horizons (Thrun, 1992) with high-dimensional observations (Stadie et al., 2015; Burda et al., 2019b; Pathak et al., 2017). Perhaps the defining feature of RL, relative to other areas of ML, is the ability to find *new* strategies. Realizing this benefit would unlock important capabilities in robotics, LLM agents, and myriad other application domains.

A common approach to exploration in reinforcement learning (RL) is to estimate the density of visited states. This estimated density is then used to construct an intrinsic reward function that encourages agents to visit novel states, thereby promoting state coverage. To enhance exploration in high-dimensional environments, prior work has proposed representation-based methods that learn compact representations, those sufficient to predict actions (Pathak et al., 2017), entirely random encodings (Burda et al., 2019b), or reconstructions of original observations (Stadie et al., 2015). These methods guide exploration along the *manifold* of meaningful states by discarding irrelevant information, as determined by the learned representations. However, identifying which aspects of the observation space are truly relevant remains a fundamental challenge. As a result, recent research has focused on learning representations that are aligned with the underlying task structure (Gelada et al., 2019; Zhang et al., 2021). In this paper, we ask: *How can we learn representations that facilitate exploration and are provably linked to the RL objective, retaining task-relevant features while excluding irrelevant ones?*

For a representation to be suitable for exploration, it should satisfy several key properties. Most importantly: (1) it should be invariant to uncontrollable aspects of the environment, (2) it should be predictive of future states under the agent's policy, (3) it should scale with the dimensionality of the observation space, and (4) it should remain up to date with the agent's ongoing experience.

One of the main challenges with previous works is the complexity of the representation learning process Pathak et al. (2017); Burda et al. (2019b), which limits the agent's ability to keep the representation up-to-date with the agent's current distribution (Castanyer et al., 2024). Our proposed method aims to overcome these issues by building on temporal contrastive representations (Sermanet et al., 2018; Qian et al., 2021; Eysenbach et al., 2022; Dave et al., 2022), which are closely related to the successor representation (Dayan, 1993) and have been shown to be provably sufficient to represent Q-values for any reward function (Mazoure et al., 2023). While prior work has primarily leveraged these representations for encoding high-dimensional observations (Laskin et al., 2020) and for learning goal-directed skills (Eysenbach et al., 2022), we take a different direction: we use them to guide exploration. Specifically, we propose to reward the agent for visiting states that lie farther along its future trajectory, thereby encouraging it to expand the boundaries of its current state visitation and to explore less-visited regions of the environment.

This work makes two main contributions. The first is a new exploration algorithm that achieves state-of-the-art state coverage across navigation, manipulation, and open-world environments. Second, connections are made between this contrastive learning-based objective and information control objectives; we show that C-TeC results in a min-max game that approximates a form of empowerment.

2 Related Work

Unsupervised RL. Prior work on unsupervised RL (Laskin et al., 2021) has proposed various task-agnostic methods for learning behaviors. A key direction in this area is intrinsic motivation, which encourages novelty-seeking behavior by maximizing state coverage or surprise. In low-dimensional and/or discrete environments, count-based exploration methods (Gardeux et al., 2016; Bellemare et al., 2016; Tang et al., 2017; Ostrovski et al., 2017; Martin et al., 2017; Xu et al., 2017; Machado et al., 2020) have demonstrated effective exploration in Atari games. However, these methods often struggle in high-dimensional or continuous state spaces. In such settings, prediction-error-based exploration approaches (Pathak et al., 2017; Burda et al., 2019a;b; Lee et al., 2019) have been more effective, both in video game environments and in continuous control tasks. Another line of research focuses on

representation-based novelty, where a representation learning component is used to extract compact features from raw state inputs. An entropy estimator is then applied to these learned representations to assess state novelty Liu & Abbeel (2021); Laskin et al. (2022).

A different approach to unsupervised RL involves training the agent to control the environment by either maximizing mutual information between states and actions (empowerment)(kly, 2005; Klyubin et al., 2005) or minimizing surprise(Friston, 2010; Berseth et al., 2021; Rhinehart et al., 2021). Empowerment-based methods (Biehl et al., 2015; Zhao et al., 2021; Mohamed & Jimenez Rezende, 2015; Karl et al., 2019; Hayashi & Takahashi, 2025; Levy et al., 2024; Jung et al., 2011; Du et al., 2020; Myers et al., 2024) encourage the agent to take actions that exert significant influence over future states, although solving the full problem remains intractable. In contrast, surprise minimization drives the agent to regulate the environment and maintain an orderly niche, giving rise to complex behaviors in both fully observed (Berseth et al., 2021; Hugessen et al., 2024) and partially observed settings (Rhinehart et al., 2021).

Representation learning for RL. Prior work on representation learning for RL focuses on self-supervised methods to improve the data efficiency of RL agents. A notable approach in this category involves the use of unsupervised auxiliary tasks, where a pseudo-reward is added to the task reward to shape the learned representations and provide an additional training signal. Examples of this approach include (Jaderberg et al., 2017; Farebrother et al., 2023; Oord et al., 2018; Laskin et al., 2020; Schwarzer et al., 2021). Another line of work focuses on forward-backward representations (Touati & Ollivier, 2021; Touati et al., 2023), which aim to capture the dynamics under all optimal policies and have been shown to exhibit zero-shot generalization capabilities. Moreover, contrastive learning has been applied in various exploration settings, including goal-conditioned learning (Eysenbach et al., 2022; Liu et al., 2025), skill discovery (Laskin et al., 2022; Yang et al., 2023; Zheng et al., 2025), and state coverage or curiosity (Liu & Abbeel, 2021; Du et al., 2021; Yarats et al., 2021). In the context of curiosity-driven exploration, Du et al. (2021); Yarats et al. (2021) employ contrastive learning to learn visual representations in image-based environments, where the RL agent is trained to maximize the error of the representation learner (similar in spirit to prediction-error approaches). We consider C-TeC to fall under the state coverage category, while learning contrastive representations that facilitate more efficient downstream learning.

3 Background

We consider a controlled Markov process (i.e., an MDP without a reward function), defined by time-indexed states s_t and actions a_t. The initial state is sampled from $p_0(s_0)$, and subsequent states are sampled from the Markovian dynamics $p(s_{t+1} \mid s_t, a_t)$. Actions are selected by a stochastic, parameterized policy $\pi(a_t \mid s_t)$. Without loss of generality, we assume that episodes have an infinite horizon; the finite-horizon problem can be incorporated by augmenting the dynamics with an absorbing state. The key to C-TeC is to use a self-supervised, or intrinsic reward, built on temporal contrastive representations. We detail the necessary preliminaries below.

Discounted state occupancy measure Formally, we define the γ-discounted state occupancy measure conditioned on a state and an action (Ho & Ermon, 2016; Eysenbach et al., 2021; 2022) as

$$p(s_f \mid s, a) \triangleq (1-\gamma) \sum_{t=0}^{\infty} \gamma^t p(s_t = s_f \mid s, a), \tag{1}$$

where $p(s_t = s_f \mid s, a)$ is the probability of being at future state s_f at time step t conditioned on s, a. In continuous settings, the future state distribution $p(s_t = s_f \mid s, a)$ is a probability *density*.

Traditionally, the discounted state occupancy measure is defined with respect to a policy as $p_\pi(s_f \mid s, a)$. However, in this work, the intrinsic reward r_{intr} is defined using a discounted state occupancy

measure over the trajectory buffer $\mathcal{T}$, which contains trajectories collected from a history of policies:

$$p_{\mathcal{T}}(s_f \mid s, a) \triangleq (1-\gamma) \sum_{0}^{\infty} \gamma^t p_{\mathcal{T}}(s_t = s_f \mid s, a).$$

To sample from the *trajectory buffer* distribution $p_{\mathcal{T}}(s_t = s_f \mid s, a)$, we first sample an offset $\Delta \sim \textsc{Geom}(1-\gamma)$, then set the future state $s_f = s_{t+\Delta}$. Here, future state $s_f = s_{t+\Delta}$ is the state reached from (s, a) after executing Δ-number of actions within a sampled stored trajectory.

Contrastive learning Contrastive representation learning methods (cho, 2005; Oord et al., 2018; Chen et al., 2020) train a critic function C_θ that takes as input pairs of positive and negative examples, and learn representations so that positive pairs have similar representations and negative pairs have dissimilar representations. To estimate the discounted state occupancy, positive examples are sampled from a joint distribution $p_{\mathcal{T}}((s, a), s_f) = p_{\mathcal{T}}(s, a) p_{\mathcal{T}}(s_f \mid s_t, a_t)$, while the negative examples are sampled from the product of marginal distributions $p_{\mathcal{T}}(s, a) p_{\mathcal{T}}(s_f)$. Here, $p_{\mathcal{T}}(s_f)$ is the marginal discounted state occupancy:

$$p_\tau(s_f) = \int p_\tau(s_f \mid s, a) p_{\mathcal{T}}(s, a) \; ds\, da.$$

We use the infoNCE loss to train the contrastive learning model Oord et al. (2018). Let $\mathcal{B} = \{(s_i, a_i, s_f^{(i)})\}_{i=1}^K$ be the sampled batch, where $s_f^{(1)}$ is the positive example sampled from conditional distribution $p_{\mathcal{T}}(s_f \mid s_i, a_i)$ and $\{s_f^{(2:K)}\}$ are the $K-1$ negatives sampled from the marginal distribution $p_{\mathcal{T}}(s_f)$ (independently from (s_i, a_i)). In addition to the standard infoNCE objective, prior work has shown that a LogSumExp regularizer is necessary to learn a critic function for control Eysenbach et al. (2021). The full contrastive reinforcement learning (CRL) loss is as follows:

$$\mathcal{L}_{\text{CRL}}(\theta) = -\mathbb{E}_{\substack{(s,a)\sim p_{\mathcal{T}}(s,a) \\ s_f^{(1)} \sim p_{\mathcal{T}}(s_f \mid s,a) \\ s_f^{(2:K)} \sim p_{\mathcal{T}}(s_f)}} \left[\log \left(\frac{e^{C_\theta((s_i,a_i),s_f^{(i)})/\tau}}{\sum_{j=1}^{K} e^{C_\theta((s_i,a_i),s_f^{(j)})/\tau}} \right) - 0.01 \cdot \log \left(\sum_{j=1}^{K} e^{C_\theta((s_i,a_i),s_f^{(j)})} \right)^2 \right]. \tag{2}$$

The optimal critic $C^*((s_t, a_t), s_f)$ corresponds to the following log probability ratio (Ma & Collins, 2018)

$$C^*((s_t, a_t), s_f) \approx \log \frac{p_{\mathcal{T}}(s_f \mid s_t, a_t)}{p_{\mathcal{T}}(s_f)},$$

where we use the following two parametrizations of the critic:

$$C_\theta((s_t, a_t), s_f)_{L2} = -||\phi_\theta(s_t, a_t) - \psi_\theta(s_f)||_2 \tag{3}$$

$$C_\theta((s_t, a_t), s_f)_{L1} = -||\phi_\theta(s_t, a_t) - \psi_\theta(s_f)||_1. \tag{4}$$

Conceptually, the critic C_θ gives a temporal similarity score between state-action pairs (s, a) and future states s_f via learned representation ϕ_θ and ψ_θ. A visual overview of the contrastive model architecture is shown in Fig. 2. These representations are powerful yet simple tools that capture complex temporal correlations between states-actions and goals. In our method C-TeC, we leverage these learned temporal contrastive representations to do exploration.

4 Curiosity-Driven Exploration via Temporal Contrastive Learning

To improve exploration, we learn representations that encode the agent's future state occupancy using C-TeC. We begin by describing how contrastive representation learning can be used to estimate state occupancy by learning a similarity function that assigns high scores to frequently visited future states and low scores to rarely visited ones (Eysenbach et al., 2022; Oord et al., 2018). We then explain how this similarity score can be leveraged to derive an intrinsic reward signal for exploration.

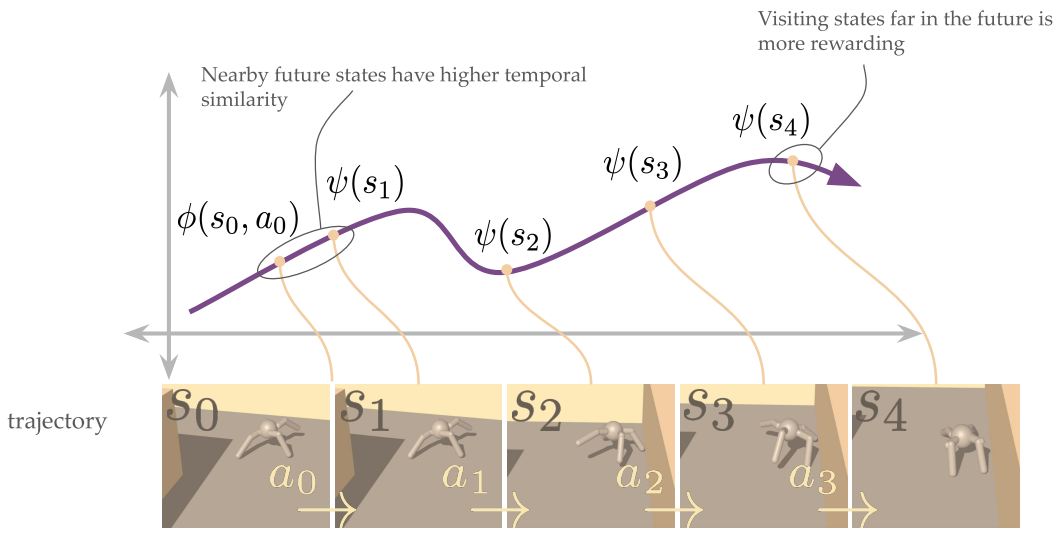

Figure 2: **Curiosity-Driven Exploration via Temporal Contrastive Learning** The agent's starting state is (s_0). We train a contrastive model such that the temporal similarity between the representation of $((s_0, a_0))$ and $(s_{2,3,4,\ldots})$ is high, and we reward the agent for visiting states that are further in the future. For example, the reward for visiting (s_4) from (s_0) should be larger than the reward for visiting (s_3) from the same (s_0).

4.1 Training the contrastive model

As detailed in 3, the contrastive model $C_\theta(s_t, a_t, s_f)$ is trained on batches $\mathcal{B}$ of (s_t, a_t, s_f) tuples, where each s_f is sampled from the discounted future state distribution. Specifically, a geometric offset $\Delta \sim \textsc{Geom}(1-\gamma)$ is sampled, and the future state is set to $s_f = s_{t+\Delta}$.

We use two parameterized encoders to define the contrastive model: $\phi_\theta(s_t, a_t)$ for state-action pairs and $\psi_\theta(s_f)$ for future states. A batch of state-action pairs $\{(s_t^{(i)}, a_t^{(i)})\}_{i=1}^K$ is passed through ϕ_θ, while the corresponding batch of future states $\{s_f^{(i)}\}_{i=1}^K$ is passed through ψ_θ. The resulting representations are then normalized to have unit norm.

To compute the similarity between representations in practice, we found that using either the negative L_1 distance or the negative L_2 distance was effective, depending on the environment. The contrastive encoder is trained to minimize the infoNCE loss (Equation (2)) (Oord et al., 2018) . For each batch sample, the positive examples of other samples are treated as negatives, following common practice (Chen et al., 2020). The temperature parameter τ is learned during training as a learnable parameter. Figure 2 illustrates the contrastive model architecture and the resulting intrinsic reward. Implementation details are provided in Appendix X.

4.2 Extracting an exploration signal from the contrastive model

Given the contrastive model, a useful intrinsic reward can be constructed. We begin with intuition for a proper intrinsic reward to encourage exploration behavior. In this method, our aim is to reach unexpected but *meaningful* states. This is in contrast to, for example, surprise maximization, which may prioritize unexpected but meaningless (i.e. random) states a la the noisy TV problem Gruaz et al. (2024).

Recall from the background section that training the critic function with the infoNCE loss (Equation (2)) produces a similarity score between a state-action pair (s_t, a_t) and a future state s_f. This similarity score is proportional to the probability of reaching s_f from (s_t, a_t) based on the trajectory buffer. *Negating* this similarity score results in our exploration signal r_{intr}: this signal encourages the agent to visit states that, in expectation, *have previously had unpredictable futures*. Because the

Algorithm 1 Curiosity-Driven Exploration via Temporal Contrastive Learning

Initialize: $\pi, \phi_\theta, \psi_\theta$,trajectory buffer $\mathcal{T}$
for each iteration **do**
  for each environment step $1 \leq t \leq T$ **do**
    $a_t \sim \pi(a_t \mid s_t)$
    $s_{t+1} \sim p(s_{t+1} \mid s_t, a_t)$
    $\tau_j \leftarrow \tau_j \cup \{s_t, a_t, s_{t+1}\}$
  $\mathcal{T} \leftarrow \mathcal{T} \bigcup \tau_j$
  Sample $\{(s_t^i, a_t^i)\}_{i=1}^{|\mathcal{B}|} \sim \mathcal{T}$ ▷ Sample a batch of state,action pairs
  Sample $\Delta_i \sim \textsc{Geom}(1-\gamma)\ \forall i \in \{1, 2, \ldots, |\mathcal{B}|\}$ ▷ Sample a geometric offsets
  Set $s_f^i = s_{t+\Delta_i}^i \forall i \in \{1, 2, \ldots, |\mathcal{B}|\}$ ▷ Set the future state s_{f_i} according to Δ_i
  Compute intrinsic rewards: $\mathbf{r}_i = -C_\theta((s_t^i, a_t^i), s_f^i)$ ▷ Eq. Equation (5)
  Update representations: $\theta \leftarrow \theta - \eta \nabla_\theta \mathcal{L}_{\text{infoNCE}}(\mathcal{B} = \{(s_t^i, a_t^i, s_f^i)\}_{i=1}^{|\mathcal{B}|}; \theta)$ ▷ Eq. Equation (2)
  RL update using $\{(s_t^i, a_t^i, \mathbf{r}_t^i)\}_{i=1}^{|\mathcal{B}|}$ ▷ Update the policy using PPO/SAC

intrinsic reward has stochasticity from the future state sampling procedure (see 4.1), we write the expression for the expectation of r_{intr}:

$$\mathbb{E}[r_{\text{intr}}(s_t, a_t)] = \mathbb{E}_{p_{\mathcal{T}}(s_f|s_t,a_t)}\left[-C_\theta((s_t, a_t), s_f)\right] = \mathbb{E}_{p_{\mathcal{T}}(s_f|s_t,a_t)}\left[||\phi_\theta(s_t, a_t) - \psi_\theta(s_f)||\right]. \quad (5)$$

The norm can be taken to be the ℓ^1 norm or ℓ^2 norm (See Sec. 5.). This reward may seem counterintuitive – we should, perhaps, prioritize reaching states with high empowerment or surprise minimization. However, we claim that Eq. 5 rewards meaningful exploration: the reward can be interpreted as identifying possible inconsistencies in the contrastive model, where the contrastive model overestimates the distance between state-actions and their futures. If the policy *were* to easily reach future states that the internal model wrongly believes are distant, this would lead to a stronger update of the internal model. We expand on information-theoretic interpretations of r_{intr} in 4.4.

After learning the contrastive representations that define the r_{intr}, we train the parameterized policy $\pi(a_t \mid s_t)$ to maximize the discounted sum of rewards:

$$J(\pi) = \mathbb{E}_{\pi(a_t|s_t)}\left[\sum_{t=0}^{\infty} \gamma^t r_{\text{intr}}(s_t, a_t)\right]. \quad (6)$$

The experiments use PPO (Schulman et al., 2017) and SAC (Haarnoja et al., 2018b;a;c) for policy training (pseudocode in Algorithm 1). In practice, we found that using a single sample future state to approximate the expectation in Equation (5) works well, except in Craftax, where we used a Monte Carlo estimate. Additional details are provided in Section 4.4 and Appendix Y.

4.3 Future states sampling

An important design choice is how to sample the future state when computing the intrinsic reward. For example, consistent sampling from states far in the future could lead to a high variance reward signal that might hinder the agent's learning, and sampling from the nearby states can be inefficient as the agent might already have a strong model over these states. One natural strategy is to sample according to the discounted occupancy measure, as described in Equation (1). Alternatively, we can sample uniformly from the future states (conditioned on the current state and action). We observe that sampling from the according to the discounted occupancy measure yields good performance across environments and we stick to this strategy in our experiments. We also show the performance differences between these sampling strategies in the experiments section Section 5.3.

4.4 Information-Theoretic Interpretation of C-TeC

In addition to quantifying temporal similarity, the converged infoNCE loss $\mathcal{L}^*_{\text{CRL}}$ provides a lower bound on the mutual information Oord et al. (2018); Eysenbach et al. (2021):

$$I(S_f; S_t, A_t) \geq \log K - \mathcal{L}^*_{\text{CRL}}(\mathcal{B}; \theta).$$

Thus, we can think of contrastive learning as finding representations that maximize the possible mutual information between *current* states and actions and *future* state distributions.

The intrinsic reward has a complementary information-theoretic interpretation as a *minimizer* of the same mutual information, thus revealing C-TeC as a two-player information-theoretic game. In expectation, the intrinsic reward evaluates to the negative of the KL-divergence between the conditional future-state distribution $p_{\mathcal{T}}(s_f \mid s_t, a_t)$ and the marginal future-state distribution $p_{\mathcal{T}}(s_f)$:

$$\begin{aligned}
\mathbb{E}[r_{\text{intr}}(s_t, a_t)] &= -\mathbb{E}_{p_{\mathcal{T}}(s_f \mid s_t, a_t)}\left[\log \frac{p_{\mathcal{T}}(s_f \mid s_t, a_t)}{p_{\mathcal{T}}(s_f)}\right] \\
&= -D_{\text{KL}}[p_{\mathcal{T}}(s_f \mid s_t, a_t) \,||\, p_{\mathcal{T}}(s_f)] \leq 0. \qquad (D_{\text{KL}} \text{ is always non-negative.})
\end{aligned}$$

This intrinsic reward leads to mode-seeking behavior: notably, the probability distribution $p_{\mathcal{T}}(s_f \mid s_t, a_t)$ only has support where $p_{\mathcal{T}}(s_f)$ has support, promoting a mode-seeking "coverage" over the broader marginal state distribution.

While the KL-divergence itself has an information-theoretic interpretation, the effect of this reward is, perhaps, more obvious in another form:

$$\begin{aligned}
\mathbb{E}[r_{\text{intr}}(s_t, a_t)] &= -D_{\text{KL}}[p_{\mathcal{T}}(s_f \mid s_t, a_t) \,||\, p_{\mathcal{T}}(s_f)] \\
&= \underbrace{H[S_f \mid s_t, a_t]}_{\text{surprise}} + \underbrace{\mathbb{E}_{p_{\mathcal{T}}(s_f \mid s_t, a_t)}[\log p_{\mathcal{T}}(s_f)]}_{\text{"familiarity" term}},
\end{aligned}$$

where S_f denotes the future state *random variable* and $s_f \sim p_{\mathcal{T}}(s_f \mid s_t, a_t)$. The first term is reminiscent of surprise, traditionally defined as $H[S' \mid s_t, a_t]$ and, at a high level, rewards diversity. The latter term encourages "familiarity," rewarding exploration over states that have been seen at any point during training.

The crucial difference between this "surprise" term and traditional surprise is in the sampling scheme: we reward the agent for state-action pairs that, according to a compressed internal model of the trajectory buffer via representations, have led to unexpected future states. However, this internal model also evolves with each iteration of C-TeC and seeks to correlate such diverse states. Viewed differently, the policy and contrastive representations engage in a **two-player game**: the policy seeks out states with futures that *appear* temporally distant under the current representations (expansion), while the representations update to make these states (and their futures) appear temporally closer (compression).

This two-player game becomes clearer after taking another expectation over states, revealing the intrinsic reward as the negative of the mutual information:

$$\begin{aligned}
\mathbb{E}_{p(s_t)}\mathbb{E}_{\pi(a_t \mid s_t)} r_{\text{intr}}(s_t, a_t, s_f) &= -\mathbb{E}_{p(s_t)}[D_{KL}[p_{\mathcal{T}}(s_f \mid s_t, a_t) \,||\, p_{\mathcal{T}}(s_f)]] \\
&= -\mathbb{E}_{p(s_t)}\Big[I(S_f; A_t \mid s_t) + D_{KL}[p(s_f \mid s_t) \,||\, p(s_f)]\Big] \\
&= -I(S_f; A_t \mid S_t) - I(S_f; S_t) \\
&= -I(S_f; S_t, A_t), \qquad \text{(by chain rule)}
\end{aligned}$$

where $p(s_t)$ is the discounted state-occupancy measure. Recalling the infoNCE preliminaries, minimizing the objective is equivalent to maximizing a lower bound on the mutual information $I(S_f; S_t, A_t)$. Because the distribution S_f is constantly expanding from round-to-round, this game does not collapse to a degenerate point, and leads to strong exploration behavior.

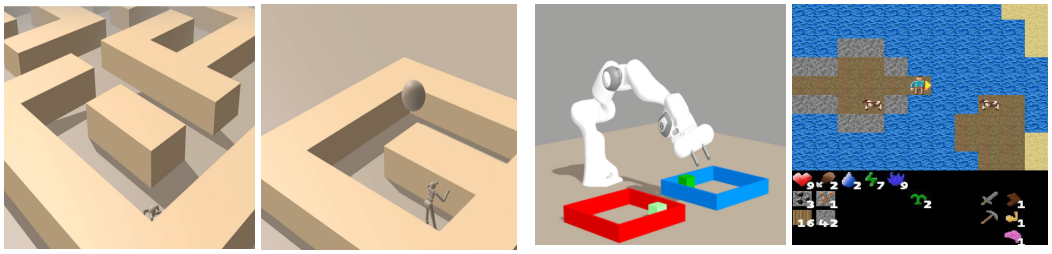

Figure 3: **Environments**. Maze coverage, robotic manipulation, and the survival game Craftax.

5 Experiments

Our experiments show that contrastive representations can be used to reward the agent for visiting less-occupied or distant future states. We then use the contrastive reward function for exploration in robotic environments and Craftax. We mainly study the following questions: (**Q1**) How well does C-TeC reward capture the agent's future state distribution? (**Q2**) How effectively does C-TeC explore in locomotion, manipulation, and Craftax environments compared to prior work? (**Q3**) How sensitive is C-TeC to the future state sampling strategy?

Environments We use environments from the JaxGCRL codebase (Bortkiewicz et al., 2025). Specifically, we evaluate C-TeC on the `ant_large_maze`, `humanoid_u_maze`, and `arm_binpick_hard` environments, which require solving long directed plans to reach goal states. In the maze-based environments, the agent's objective is to reach a designated goal specified at the start of each episode. Exploration in these settings corresponds to maze coverage: an agent that visits more unique positions in the maze demonstrates better exploration capabilities. In the `arm_binpick_hard` environment, which differs from the more navigation-themed tasks used in prior work, the agent must pick up a cube from a blue bin and place it at a specified target location in a red bin. This represents a challenging exploration task, as the agent must locate the cube, grasp it, and successfully place it at the correct target location.

Our experiments with the `ant` and `humanoid` agents assess the method's ability to achieve broad state coverage using two complex embodiments. Meanwhile, the `arm_binpick_hard` task evaluates the method's effectiveness at exploration in an object manipulation setting. We also run C-TeC on Craftax-Classic (Matthews et al., 2024), a challenging open-world survival game resembling a 2D Minecraft. The agent's goal is to survive by crafting tools, maintaining food and shelter, and defeating enemies

In the locomotion and manipulation environments, we compare C-TeC to common prior methods for exploration: **Random Network Distillation (RND)** (Burda et al., 2019b) and **Intrinsic Curiosity Module (ICM)** (Pathak et al., 2017) which are both popular intrinsic motivation methods for exploration. **Active Pre-training (APT)** (Liu & Abbeel, 2021): APT learns observation representations using contrastive learning, where positives are augmentations of the same observation and negatives are different observations. It uses the KNN distance between state representations as an exploration signal, which correlates with state entropy. Unlike C-TeC, APT does not learn representations predictive of the future. In Craftax, we compare against RND, ICM, and **exploration via elliptical episodic bonuses (E3B)** (Henaff et al., 2022), a count-based exploration method. We found that using the negative L_1 distance (Equation (4)) as the critic function works best in the robotics environments, while the negative L_2 distance (Equation (3)) performs best in Craftax. A comparison of different critic functions can be found in the appendix.

5.1 Capturing the future state distribution (Q1)

The goal of this experiment is to demonstrate that the C-TeC reward captures the future state distribution. As a result, it can be used to incentivize the agent to visit less-occupied and more distant future

states. We visualize the C-TeC reward at different stages of training in the `ant_hardest_maze` environment. The contrastive critic is defined as the negative L_1 distance (Equation (4)), and the policy is trained to maximize the intrinsic reward defined in Equation (5). Figure 4 shows the reward

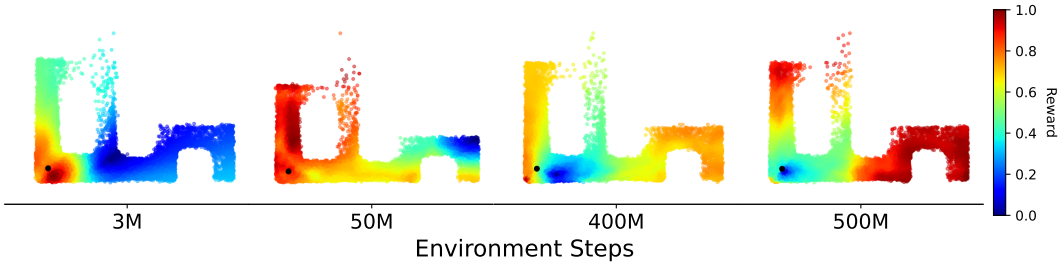

Figure 4: **Evolution of the C-TeC reward during training**. This figure shows how the intrinsic reward changes over the course of training based on future state visitation. The black circle in the lower-left corner represents the starting state. Early in training (3M steps), higher rewards are assigned to nearby states. As training progresses, the agent explores farther, and the reward increases for more distant regions. All reward values are normalized for visualization.

values in a section of the maze, with the black circle in the lower-left corner indicating the starting state. In the early stages of training (3M steps), the reward is highest for nearby states. As training progresses, the agent explores farther, and the reward increases for more distant regions (e.g., at 400M and 500M steps). Over time, the reward becomes increasingly aligned with the maze's geometry.

5.2 Exploration results (Q2)

In this experiment, we evaluate C-TeC in the `ant_large_maze`, `humanoid_u_maze`, and `arm_binpick_hard` environments. We run two variants of the experiment: (1) using the complete state vector as the future state, which is common in exploration tasks where the agent is encouraged to explore the entire state space; and (2) incorporating prior knowledge by restricting the future state to specific components of the state vector. The latter allows us to assess whether C-TeC can flexibly explore subspaces of the state space, which is often useful in practice. In `ant_large_maze`, we define the future state as the future (x, y) position of the ant's torso. In `humanoid_u_maze`, we use the future (x, y, z) position of the humanoid's torso. Finally, in `arm_binpick_hard`, we define the future state as the future position of the cube.

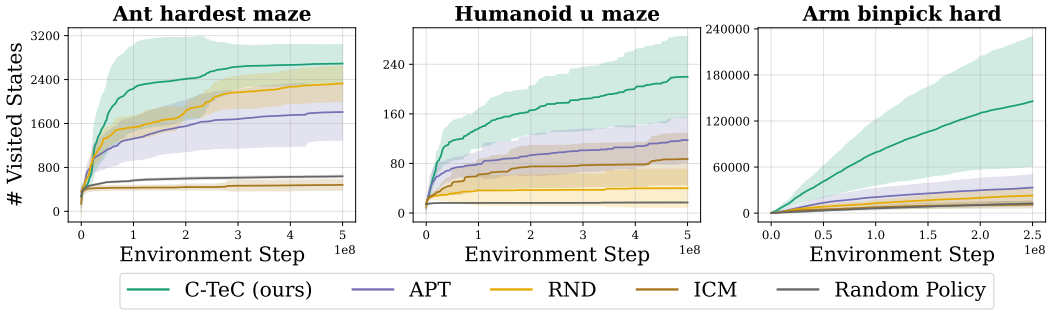

Figure 5: **C-TeC explores more states than prior methods.** We compare the state coverage of C-TeC to APT (Liu & Abbeel, 2021), RND (Burda et al., 2019b) and ICM (Pathak et al., 2017). We include a uniform random policy as well.

As an evaluation metric, we count the number of unique discretized states covered by each agent. In `ant_large_maze`, we count the number of unique (x, y) positions in the maze visited by each agent. Similarly, in `humanoid_u_maze`, we count the number of visited (x, y, z) positions, and in `arm_binpick_hard`, we count the number of unique cube positions. We compare C-TeC to RND, ICM, APT, and a uniformly random policy. Figure 5 shows the learning curve when using the complete future state vector while Figure 6 shows the performance when using subspace of the future

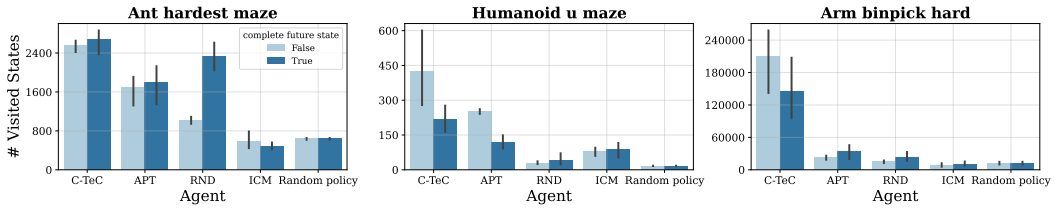

Figure 6: **State coverage when the future state is a subspace of the state vector.** C-TeC outperforms prior methods (Liu & Abbeel, 2021; Burda et al., 2018; Pathak et al., 2019) and can explore effectively when we use a subspace of the future state. This shows the flexibility of C-TeC in incorporating prior knowledge by restricting the exploration space. Prior work does not offer this flexibility, as shown in the results.

state. Each agent is run with 5 random seeds, and we plot the mean and standard deviation (Patterson et al., 2024).

Our agent outperforms the baselines in both variants of the experiment and learns interesting behaviors in the challenging `humanoid_u_maze` environment. Figure 7 shows screenshots of C-TeC behavior and more visuals are provided appendix E. This improvement can be the result of C-TeC's consistent reward properties. Methods like RND, ICM will eventually tend to a reward of 0 as the state distribution is covered. A nice property of C-TeC is that it does not have zero reward in the limit.[1]

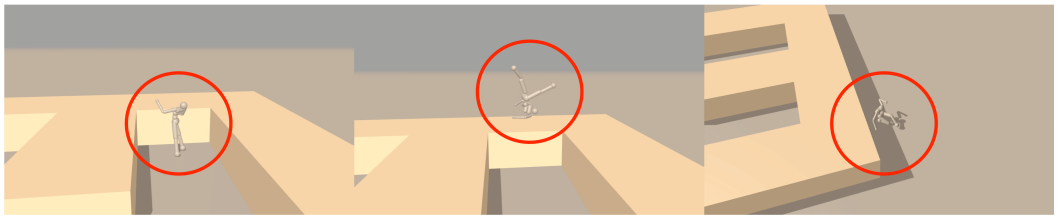

Figure 7: **C-TeC behavior in humanoid-u-maze**.C-TeC agent learns to escape the u-maze by jumping over the wall, none of the baselines discovered this kind of unexpected novel behavior.

5.2.1 Learning complex behavior in Craftax

Can an RL policy learn complex behavior in Craftax without any task reward? To answer this question, we run C-TeC on Craftax-Classic (Matthews et al., 2024), a complex survival game where the agent's goal is to survive by crafting tools, maintaining food and shelter, and defeating enemies.

In this experiment, we use the same PPO implementation as used in the baselines in the Craftax paper (Matthews et al., 2024), adding the contrastive reward on top of it. We compare against RND, ICM, and E3B. We found that using PPO with memory (PPO-RNN) yields the best performance.

Figure 8 shows the results. The Y-axis represents the achievement score, which measures how many capabilities and useful objects the agent has discovered. C-TeC outperforms the baselines and unlocks more achievements. Figure 1 visualizes some of the achievements of the C-TeC agent during an evaluation episode.

5.3 Sensitivity to future state sampling strategy (Q3)

In this experiment, we investigate the sensitivity of C-TeC to the future state sampling strategy. Specifically, we consider two variants in addition to the geometric sampling: (1) sampling uniformly from the future. Unlike geometric sampling, uniform sampling does not prefer states that are sooner in the future over later ones. (2) geometric sampling with an increasing γ value. The intuition behind

[1]Videos are in the project website: `https://temp-contrastive-explr.github.io/`

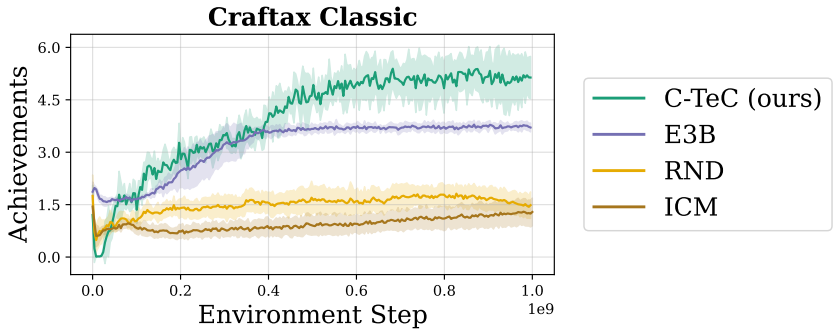

Figure 8: **Exploration in Craftax.** C-TeC outperforms the baselines in discovering more achievements in Craftax-Classic, E3B (Henaff et al., 2022) is the most competitive baseline.

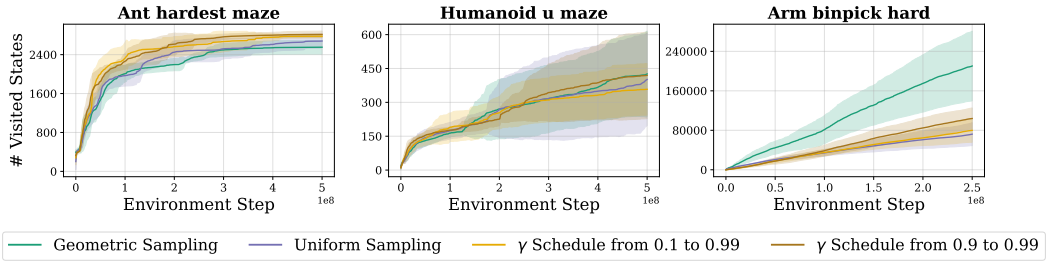

Figure 9: **Sensitivity to future state sampling strategy.** We compare variants of C-TeC with different future state sampling strategy, the method is robust to the choice of the sampling strategy and all the variants outperform the baselines.

this strategy is that exploring nearby states is easier for the agent at the start of training, and as the agent becomes better at exploring them, it can progressively explore farther states in the future. We refer to this strategy as the γ-schedule, and we experiment with two different starting values of γ: one ranging from $\gamma = 0.9$ to $\gamma = 0.99$, and another from $\gamma = 0.1$ to $\gamma = 0.99$.

The results are shown in Figure 9. First, we note that regardless of the future state sampling strategy, the contrastive method explores better than the baselines in all three environments. However, the best-performing strategy is environment-specific. For example, in `ant_hardest_maze`, sampling according to the γ-schedule performs best, while in `arm_binpick_hard`, geometric sampling tends to perform slightly better. Overall, the method appears robust to future state sampling strategies.

6 Conclusion

This work has shown how to learn contrastive representations for intrinsic exploration. These representations over state action pairs and another model for future states can be combined to estimate the distribution over state visitation. It is shown that constructing a reward function that seeks out states with *unexpected* future states results in a significant performance gain over prior intrinsic objectives that also aim to estimate the state visitation. This is also shown via visualization of the state visitation distribution. These results are also demonstrated with different RL algorithms, and across environments, illustrating that the benefits are robust. In the future, this representation learning algorithm could be applied to image-based environments to better understand its capabilities on partially observed environments.

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Supplementary Materials

The following content was not necessarily subject to peer review.

Broader Impact Statement

This work proposes an exploration method for deep RL agents that facilitates finding better solutions across a broad range of sequential decision-making problems. Depending on the intended task and the reward function, the resulting policy may lead to either positive or negative consequences.

A Training Details and Ablations

We summarize the hyperparameters and model architectures for all experiments. In Appendix A.1, we provide the training details for the locomotion and manipulation experiments. In Appendix A.2, we provide the details of the Craftax experiments. In Appendix A.3, we provide the details of all the environments. In Appendix A.4, we include the codebase.

Finally, in Appendix A.5, we include the ablation experiments.

A.1 Robotics Environments

In the robotics environments, we used SAC as the RL algorithm. Table 1 shows the hyperparameters that are shared across all methods. Tables 2 and 3 show the algorithm-specific hyperparameters for C-TeC and the baselines, respectively.

Table 1: Hyperparameters for all methods in robotics environments

Hyperparameter	Value
num_timesteps	500,000,000
max_replay_size	10,000
min_replay_size	1,000
episode_length	1,000
discounting	0.99
num_envs	1024 (256 for humanoid_u_maze)
batch_size	1024 (256 for humanoid_u_maze)
multiplier_num_sgd_steps	1
action_repeat	1
unroll_length	62
policy_lr	3e-4
critic_lr	3e-4
hidden layers (for both actor and critic)	[256,256]

Table 2: Hyperparameters for C-TeC in robotics environments

Hyperparameter	Value
contrastive_lr	3e-4
contrastive_loss_function	infoNCE
similarity_function	L1
logsumexp_penalty	0.1
hidden layers (for both encoders)	[1024,1024]
representation dimension	64

Table 3: Hyperparameters for baselines in robotics environments

Hyperparameter	Value
rnd encoder lr	3e-4
rnd embedding dim	512
rnd encoder hidden layers	[256, 256]
icm encoder lr (forward and inverse models)	3e-4
icm embeddings_dim	512
icm encoders hidden layers	[1024, 1024]
icm weight on forward loss	0.2
apt contrastive lr	3e-4
apt similarity function	L1
apt contrastive hidden layers	[1024, 1024]
apt representation dimension	64
Augmentation type	$\mathcal{N}(0, 0.5)$

A.2 Craftax

In Craftax, we used PPO as the RL algorithm[2]. Table 4 shows the hyperparameters shared across all methods. Tables 5 and 6 show the algorithm-specific hyperparameters for C-TeC and the baselines, respectively.

Table 4: Hyperparameters for all methods in robotics environments

Hyperparameter	Value
num_timesteps	1,000,000,000
num_steps	64
learning_rate	2e-4
anneal_learning_rate	True
update_epochs	4
discounting	0.99
gae_lambda	0.8
clip_epsilon	0.2
ent_coef	0.01
max_grad_norm	1.0
activation	tanh
action_repeat	1
RNN_layers (GRU)	[512 (embedding dim),512 (hidden dim)]
hidden layers (both actor and value)	[512, 512]

[2] https://github.com/MichaelTMatthews/Craftax_Baselines

Table 5: Hyperparameters for C-TeC in Craftax

Hyperparameter	Value
contrastive_lr	3e-4
contrastive_loss_function	infoNCE
similarity_function	L2
logsumexp_penalty	0.0
hidden layers (for both encoders)	[1024,1024,1024]
representation dimension	64

Table 6: Hyperparameters for baselines in Craftax

Hyperparameter	Value
rnd encoder lr	3e-4
rnd embedding dim	512
rnd encoder hidden layers	[256, 256]
icm encoder lr (forward and inverse models)	3e-4
icm embeddings_dim	512
icm encoders hidden layers	[256, 256]
icm weight on forward loss	1.0
e3b (icm) lambda	0.1

A.3 Environment Details

- **Ant-hardest-maze** The observation space of this environment has 29 dimensions, consisting of joint angles, angular velocities, and the x,y position of the ant's torso. The action space is 7-dimensional, representing the torque applied to each joint.
- **Humanoid-u-maze** The observation space of this environment has 268 dimensions, consisting of joint angles, angular velocities, and the x,y position of the humanoid's torso. The action space is 17-dimensional, representing the torque applied to each joint.
- **Arm-binpick-hard** The observation space of this environment has 18 dimensions, consisting of joint angles, angular velocities, the cube position, and the end-effector position and offset. The action space is 5-dimensional, representing the displacement of the end-effector.
- **Craftax-Classic** The observation space is a one-hot encoding of size 1345, capturing player information (inventory, health, hunger, attributes, etc.) as well as the types of blocks and creatures within the player's visual field. The action space is discrete and consists of 17 actions.

A.4 Codebase

Our codebase for the robotics experiments and Craftax is provided below:

- **Robotics Environments** https://anonymous.4open.science/r/c-tec-DFE7/README.md
- **Craftax** https://anonymous.4open.science/r/c-tec-5E12/README.md

A.5 Ablation Study

To understand the contribution of each component to the overall performance of C-TeC, we conduct an ablation study on several key elements of the algorithm, illustraed in the following section.

A.5.1 Representation Normalization

Is it important to normalize the contrastive representations when computing the intrinsic reward? To answer this question, we compare the exploration performance of C-TeC across all environments, keeping all hyperparameters fixed except for the normalization of the representations.

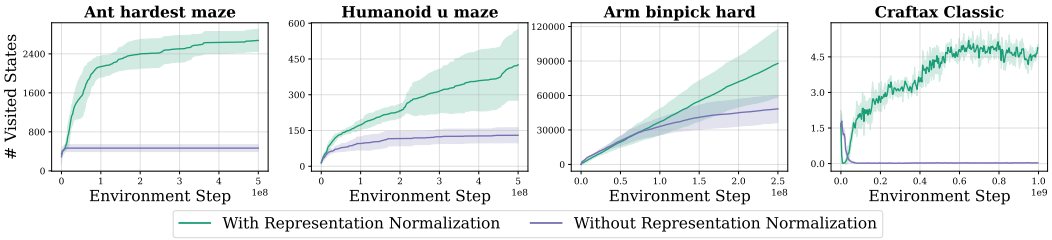

Figure 10: **Normalizing the contrastive representations.** Normalizing the representations is crucial for effective exploration—using unnormalized representations significantly degrades exploration performance.

A.5.2 Contrastive Losses

We compare the performance of C-TeC using different contrastive loss functions. Specifically, we evaluate InfoNCE, symmetric InfoNCE, NCE (Hjelm et al.), FlatNCE (Chen et al., 2021), and a Monte-Carlo version of the forward-backward (FB) Touati & Ollivier (2021) loss, as defined in Equations [7–11]. Figure 11 presents the results. Overall, NCE leads to poorer exploration, particularly in Craftax. InfoNCE and symmetric InfoNCE exhibit similar performance across all environments. In general, the method is reasonably robust to the choice of contrastive loss.

$$\mathcal{L}_{\text{infoNCE}}(\theta) = -\sum_{i=1}^{K} \log \left(\frac{e^{C_\theta((s_i,a_i),s_f^{(i)})}}{\sum_{j=1}^{K} e^{C_\theta((s_i,a_i),s_f^{(j)})}} \right) \tag{7}$$

$$\mathcal{L}_{\text{symmetric_infoNCE}}(\theta) = -\left[\sum_{i=1}^{K} \log \left(\frac{e^{C_\theta((s_i,a_i),s_f^{(i)})}}{\sum_{j=1}^{K} e^{C_\theta((s_i,a_i),s_f^{(j)})}} \right) + \log \left(\frac{e^{C_\theta((s_i,a_i),s_f^{(i)})}}{\sum_{j=1}^{K} e^{C_\theta((s_j,a_j),s_f^{(i)})}} \right) \right] \tag{8}$$

$$\mathcal{L}_{\text{Binary(NCE)}}(\theta) = -\left[\sum_{i=1}^{K} \log \left(\sigma \left(C_\theta((s_i,a_i),s_f^{(i)}) \right) \right) - \sum_{j=2}^{K} \log \left(1 - \sigma \left(C_\theta((s_i,a_i),s_f^{(j)}) \right) \right) \right] \tag{9}$$

$$\mathcal{L}_{\text{FlatNCE}}(\theta) = -\sum_{i=1}^{K} \log \left(\frac{\sum_{j=1}^{K} e^{C_\theta(s_i,a_i,s_f^{(j)}) - C_\theta(s_i,a_i,s_f^{(i)})}}{\text{detach}\left[\sum_{j=1}^{K} e^{C_\theta(s_i,a_i,s_f^{(j)}) - C_\theta(s_i,a_i,s_f^{(i)})} \right]} \right) \tag{10}$$

$$\mathcal{L}_{\text{FB}}(\theta) = -\sum_{i=1}^{K} \left(e^{C_\theta(s_i,a_i,s_f^{(i)})} \right) + \frac{1}{2(K-1)} \sum_{i=1}^{K} \sum_{\substack{j=1 \\ j \neq i}}^{K} \left(e^{C_\theta(s_i,a_i,s_f^{(j)})} \right)^2 \tag{11}$$

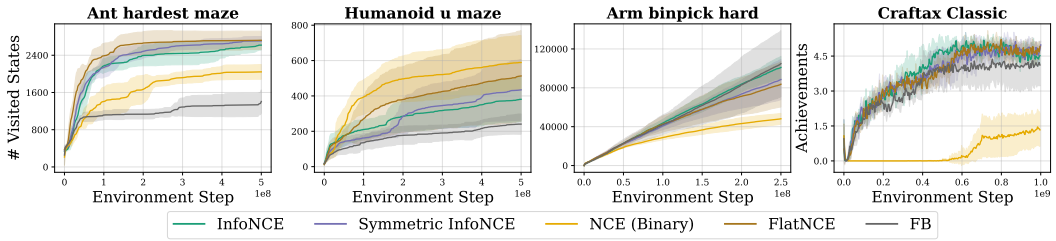

Figure 11: **Comparison of Different Contrastive Losses.** Overall, C-TeC is robust to the choice of contrastive loss. A notable exception is the Binary NCE loss in Craftax, where it performs relatively poorly.

A.5.3 Contrastive Critic Functions

We compare four critic similarity functions shown below:

$$C_\theta((s_t, a_t), s_f)_{L1} = -||\phi_\theta(s_t, a_t) - \psi_\theta(s_f)||_1. \tag{12}$$

$$C_\theta((s_t, a_t), s_f)_{L2} = -||\phi_\theta(s_t, a_t) - \psi_\theta(s_f)||_2 \tag{13}$$

$$C_\theta((s_t, a_t), s_f)_{L2-w/o-sqrt} = -||\phi_\theta(s_t, a_t) - \psi_\theta(s_f)||_2^2 \tag{14}$$

$$C_\theta((s_t, a_t), s_f)_{dot} = -\phi_\theta(s_t, a_t)^\top \psi_\theta(s_f) \tag{15}$$

Fig. 13 shows the results. In general, using the L_1 distance yields the best performance across the robotic environments, while L_2 performs better in Craftax. This highlights the importance of this design choice and suggests that some tuning may be required to select the most effective critic function.

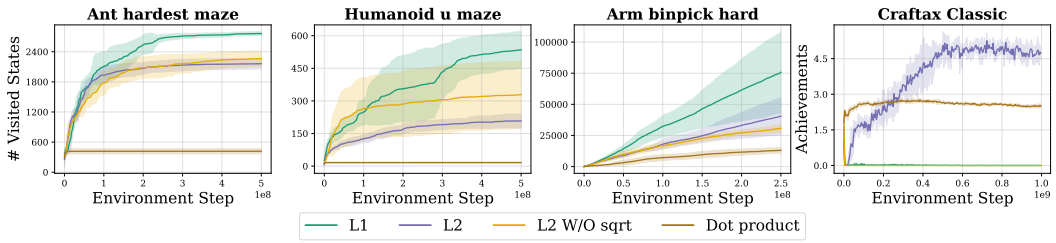

Figure 12: **Comparison of Critic function.** Overall,the L_1 distance yields the best performance across the robotic environments, while L_2 performs better in Craftax.

A.5.4 Contrastive Critic Architecture

In this ablation we compare two architectures of the contrastive critic, the separable architecture $(\phi_\theta(s_t, a_t), \psi_\theta(s_f))$, which is the one we use in all of our experiment, and the monolithic critic f_θ i.e., a single model that takes

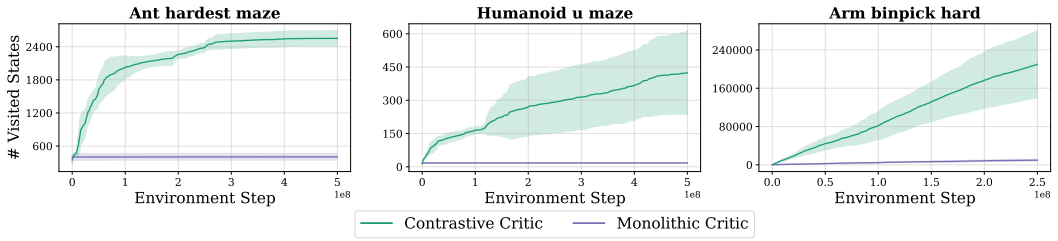

Figure 13: **Critic architecture** Using a monolithic critic results in poor exploration performance, while using the separable architecture results in much better exploration, this shows the importance of the architecture choice and how it can affect exploration.

B Compute Resources

In all experiments, we use 2 CPUs, a single GPU, and 8 GB of RAM. The specific GPU type varies depending on the job scheduling system, but most experiments run on NVIDIA RTX 8000 or V100 GPUs. Training in the robotics environments takes approximately 24 hours on average, while Craftax experiments require around 30 hours.

C Exploration in Noisy TV setting

We investigate C-TeC performance in the presence of a noisy TV state, we run this experiment on a modified grid environment from xland-minigrid (Nikulin et al., 2024) with a noisy TV region. We did not observe any evidences of worse exploration performance namely the agent has covered all the states in the grid world.

D C-TeC as an Info-Theoretic Two-Player Game

We formalize C-TeC as an approximate information-theoretic two-player game. See Section D.3 for an extended discussion of comparisons with prior intrinsic motivation objectives.

Let $Z_\pi = \phi(S_\pi, A_\pi)$ be the random variable given by encoding a state–action pair with ϕ, where S_π, A_π is drawn from the discounted state–action occupancy measure of policy π. Likewise, let $F_\mathcal{T} = \psi(S_f)$ be the random variable given by encoding a state with ψ, where S_f is drawn from the trajectory buffer $\mathcal{T}$.

Then, maximizing J^π and minimizing the InfoNCE loss corresponds to the following max/min equations, in expectation:

$$\min_\pi \; I\big(Z_\pi \; ; \; F_\mathcal{T}\big) = \min_\pi \; I\big(\phi(S_\pi, A_\pi); \; \psi(S_f)\big), \tag{16}$$

$$\max_{\phi,\psi} \; [\log K - \mathcal{L}_{\phi,\psi}(Z_\mathcal{T}, F_\mathcal{T})] \leq \max_{\phi,\psi} \; I\big(\phi(S_\mathcal{T}, A_\mathcal{T}); \; \psi(S_f)\big). \tag{17}$$

We note that this is not a min-max game, and should be thought of as a general two-player game. First, the objectives that are being minimized and maximized are not exactly the same – the contrastive objective gives a lower bound on the mutual information (MI), which is only tight at convergence. Second, the actual random variables used to calculate the MI measures are different: one MI is defined with respect to Z_π, while the other is defined with respect to $Z_\mathcal{T}$. Third, all the trajectories collected by π is later added to the buffer – the objective continually changes. In words, the intrinsic reward is prioritizing *reaching* a distribution of state-actions that minimize this MI with the buffer, while the contrastive objective learns representations that maximizes (a lower bound of) the MI over updated buffer state-actions *and* future states.

D.1 No (Achievable) Trivial Fixed Points

One may ask: what is the fixed point of this game? Without additional simplifications, this problem is intractable. Notably, standard analysis would fail to prove convergence due to the nonconvexity/concavity of the objectives. While the zero-gradient condition for the InfoNCE objective is clear, the zero-gradient condition for the objective is not obvious due to the complex relationship between π and the state occupancy measure.

A more aggressive simplification that can yield analysis of the global optimum is to assume that the policy optimization is done directly over S_π and A_π and that the representations are infinitely expressive. In practice, these assumptions are very unrealistic; however, such simplifications have been used in prior work on unsupervised RL to give a conceptual picture of similar games Pitis et al. (2020).

With these simplifications, the InfoNCE objective reduces to:

$$\max_{\phi,\psi} \; [\log K - \mathcal{L}_{\phi,\psi}(Z_\mathcal{T}, F_\mathcal{T})] \underset{K\to\infty}{\longrightarrow} I\big(S_\mathcal{T}, A_\mathcal{T};\, S_f\big).$$

Furthermore, because the "policy" optimization is fixed in $P(S_f \mid S_\pi, A_\pi)$, the MI is concave in $P(S_\pi, A_\pi)$. Our objective has now reduced to a constrained optimization problem with conditions $\sum_{s,a} p_\pi(s,a) = 1$ and $p_\pi(s,a) \geq 0$ for all $(s,a) \in \mathcal{S} \times \mathcal{A}$. Clearly, a trivial global optimum is the delta function at some (s,a).

However, we are generally uninterested in (and unable to achieve) this global optimum, assuming a nontrivial transition kernel. Instead, consider the stationarity conditions given by the lagrangian. Let λ and $\mu(s,a)$ denote the lagrange mutlipliers for the normalization and non-negativity conditions respectively. Then, the full Lagrangian $\mathcal{L}_{\text{Lagrangian}}$ is as follows:

$$\mathcal{L}_{\text{Lagrangian}}(p_\pi, \lambda, \mu) = I(S_\pi, A_\pi; S_f) + \lambda\Big(\sum_{s,a} p_\pi(s,a) - 1\Big) - \sum_{s,a} \mu(s,a) p_\pi(s,a).$$

Note that by complementary slackness, we have $\mu(s,a)p(s,a) = 0$. Taking the functional derivative of $\mathcal{L}_{\text{Lagrangian}}$ with respect to distribution $p(s,a)$ yields the KL-divergence:

$$\frac{\delta \mathcal{L}_{\text{Lagrangian}}}{\delta p_\pi}[s,a] = D_{KL}[p_\mathcal{T}(s_f \mid s,a) || p_\mathcal{T}(s_f)] - 1 + \lambda - \mu(s,a).$$

Thus, by the complementary slackness, the distribution $p_\pi(s,a)$ is stationary local optima only if the KL-divergence $D_{KL}[p_\mathcal{T}(s_f \mid s,a) || p_\mathcal{T}(s_f)]$ is *constant* for any (s,a) where $p_\pi(s,a)$ has support. Any deviation would lead to a non-zero gradient at that point (s,a). In other words, all conditional trajectory future state distributions look equally "far" from the marginal.

In addition to the trivial, but unobtainable, case of the delta function, distributions that would satisfy the stationarity condition include a uniform marginal and conditional distribution over future states, for all reachable (s,a). However, in practice, this condition (and having fixed KL-divergence from the marginal) is generally impossible. As an example, let us consider the limit $\gamma \ll 1$ where the future state is almost always the next state. Then, the conditional distribution $p(s_f \mid s,a)$ is approximately the transition kernel $T(s_f \mid s,a)$ – meaning that transitions are the same for all states, a degenerate MDP.

This analysis shows that there are no easily achievable trivial fixed points in this game for standard MDPs even under aggressive simplifications.

D.2 Representation-Driven Expansion of Temporally-Distant Futures

We have shown that the optimization, even with aggressive simplifications, does not lead to easily achievable trivial fixed points. However, this analysis still does not concretely explain the performance

of the exploration method. Here, we outline a mathematical argument for the effectiveness of the method.

Concretely, the below analysis shows that the method is incentivized to lower the temporal distance predicted *from* state-action (s, a) pairs. The predicted temporal distance can be lowered in two ways: (1) by reducing errors, or overestimates, of the predicted distance from (s, a) to future states $s_f \sim p_{\mathcal{T}}(s_f \mid s, a)$ and/or (2) by effectively navigating towards the future states s_f. We detail these effects here.

We begin with notation. Let

$$C_{\text{true}}(s, a, s_f) \;=\; \log \frac{p_{\mathcal{T}}(s_f \mid s, a)}{p_{\mathcal{T}}(s_f)}$$

be the true relative density. Let

$$C_{\phi_{\text{k}},\psi_{\text{k}}}(s, a, s_f) = -||\phi_k(s, a) - \psi_k(s_f)|| \;\approx\; \log \frac{p_{\mathcal{T}}(s_f \mid s, a)}{p_{\mathcal{T}}(s_f)}$$

be the estimated relative density at round k, where the (random variable) intrinsic reward at round k is given by

$$r_{\text{intr},k} = ||\phi_k(s, a) - \psi_k(s_f)|| \approx -\log \frac{p_{\mathcal{T}}(s_f \mid s, a)}{p_{\mathcal{T}}(s_f)}$$

for a randomly drawn s_f from the conditional distribution $p_{\mathcal{T}}(s_f \mid s, a)$.

The expected *representation error* is as follows:

$$\begin{aligned}
\delta_k(s, a, s_f) &= C_{\text{true}}(s, a, s_f) - C_{\phi_{\text{k}},\psi_{\text{k}}}(s, a, s_f) \\
&= \mathbb{E}[r_{\text{intr},k}(s, a)] + C_{\text{true}}(s, a, s_f) \\
&= ||\phi_k(s, a) - \psi_k(s_f)|| - \log \frac{p_{\mathcal{T}}(s_f)}{p_{\mathcal{T}}(s_f \mid s, a)}.
\end{aligned}$$

The intrinsic reward is thus

$$\mathbb{E}[r_{\text{intr},k}] = \delta_k(s, a, s_f) + \log \frac{p_{\mathcal{T}}(s_f)}{p_{\mathcal{T}}(s_f \mid s, a)}.$$

Therefore, the intrinsic reward encourages the agent to visit state-action pairs (s, a) where representation error is high and/or lead to temporally-distant futures. If the intrinsic reward successfully leads to a policy that reaches these states, the trajectory buffer $\mathcal{T}$ will now have *more transitions* at these inconsistent, or distant states. Thus, the updated representations over this buffer $\mathcal{T}$ will, in expectation (given successful reaching of these states under standard PPO/SAC), "relabel" the pair (s, a) as temporally closer.

This leads the intrinsic reward to prioritize other states with more unpredictable futures, and the cycle of exploration and updating representations repeats.

D.3 Comparison with Previous Methods

At a high level, C-TeC is related to other intrinsic exploration objectives that reward uncertainty. Objectives such as RND Burda et al. (2019b) and Disagreement Pathak et al. (2019) explore unfamiliar states, presumably leading to these states becoming more familiar in future rounds. Such methods avoid trivial fixed points found in count-based (lose reward signal after reaching a uniform distribution, not easily scalable) Ostrovski et al. (2017), curiosity (lose reward signal after perfectly capturing local transitions) Gruaz et al. (2024), or empowerment objectives (focus in controllable, but not novel, areas) kly (2005).

However, the key difference between prior methods and C-TeC lies in the prioritization of states that have *previously led to distant futures* according to an internal contrastive model. Our method

drives the agent to explore areas where future outcomes remain unpredictable. This objective is markedly different from next-step prediction error Pathak et al. (2017); Burda et al. (2019a): C-TeC does not use a decoder in latent or real space, relies on learned temporal correlations via a lightweight contrastive objective, and is designed to leverage long-horizon relations between states beyond next-step transitions. Importantly, our analysis in Sec. D.2 shows that these temporal representations not only encourage the model to reach states that reduce error, but also naturally "compress" these distant futures to appear closer: the error-reduction and exploration effects are contained in a single term. Taken together, our analysis and results show that temporal contrastive representations are simple yet powerful frameworks for intrinsic motivation.

E Emergent Exploration Behavior

Figure 15 shows some of the learned behaviors of C-TeC in the `humanoid-u-maze`, where the agent learns to jump over the wall to escape the maze.

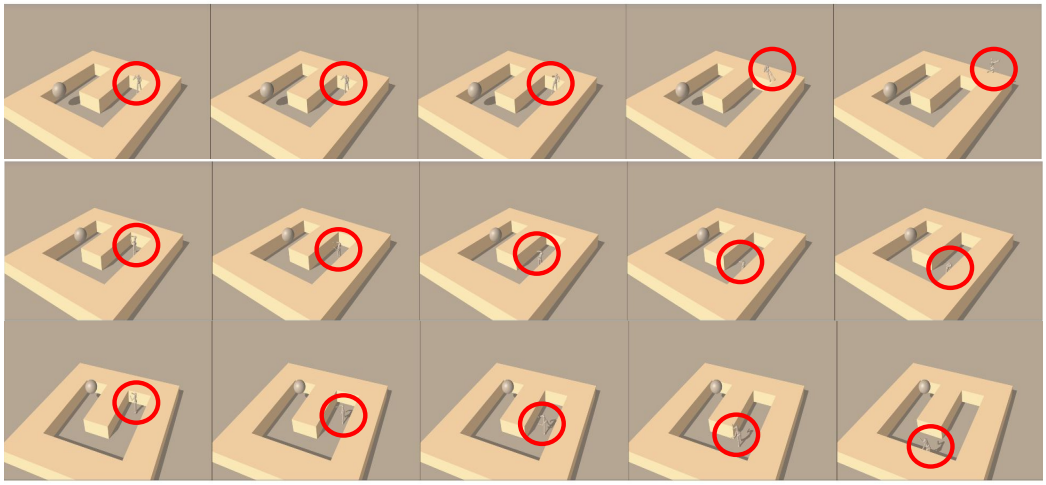

Figure 14: **Emergent Exploration Behavior in `humanoid-u-maze`.** C-TeC exhibits interesting emergent behaviors; for example, in the `humanoid-u-maze` environment, the agent learns to jump over the maze walls to escape the maze. Each row represents an independent evaluation epsidoe.

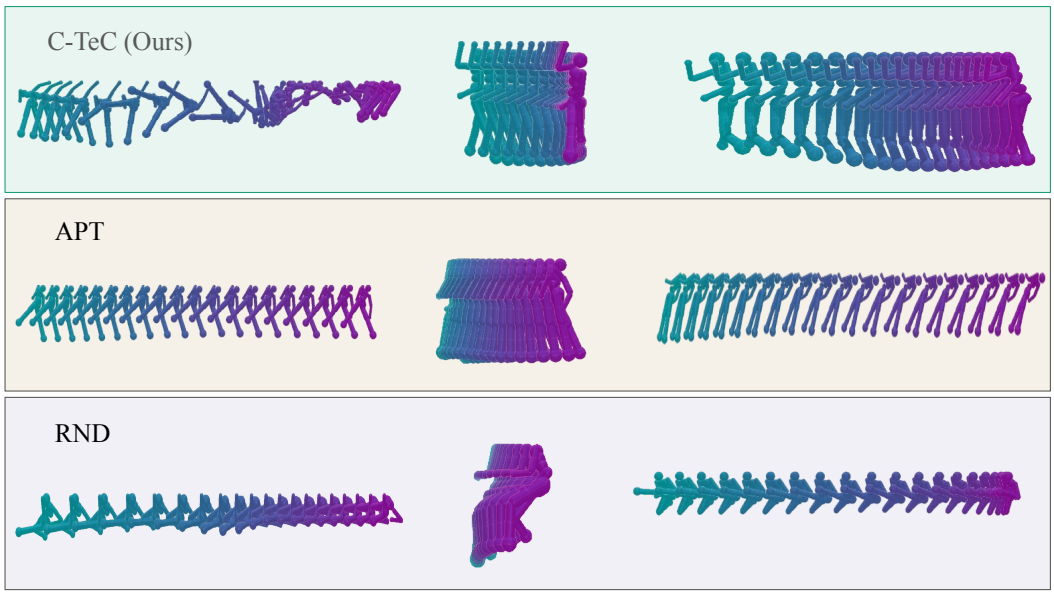

Figure 15: **Qualitative Comparison in `humanoid-u-maze`.**