Strengthening Interpretability: An Investigative Study of Integrated Gradient Methods

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Abstract

We conducted a reproducibility study on Integrated Gradients (IG) based methods and the Important Direction Gradient Integration (IDGI) framework. IDGI eliminates the explanation noise in each step of the computation of IG-based methods that use the Riemann Integration for integrated gradient computation. We perform a rigorous theoretical analysis of IDGI and raise a few critical questions that we later address through our study. We also experimentally verify the authors' claims concerning the performance of IDGI over IG-based methods. Additionally, we varied the number of steps used in the Riemann approximation, an essential parameter in all IG methods, and analyzed the corresponding change in results. We also studied the numerical instability of the attribution methods to check the consistency of the saliency maps produced. We developed the complete code to implement IDGI over the baseline IG methods and evaluated them using three metrics since the available code was insufficient for this study. Our code is readily usable and publicly available at [link-hidden-for-submission].

1 Introduction

Deep learning models for computer vision have become increasingly integrated into several vital domains like healthcare and security. There is a surge in research dedicated to studying the problem of attributing the prediction of a deep network to its input features. Gradient-based saliency/attribution map approaches (Sundararajan et al., 2017; Xu et al., 2020; Kapishnikov et al., 2021; 2019; Pan et al., 2021; Simonyan et al., 2013; Smilkov et al., 2017) form an important category of explanation methods. One of the first works that made a notable contribution to the field of explainability and also introduced a valid metric system to evaluate its results was by Kapishnikov et al. (2019). Other prominent gradient-based explanation methods include Integrated Gradients (IG) (Sundararajan et al., 2017) and its variants, BlurIG and GIG (Xu et al., 2020; Kapishnikov et al., 2021), that have garnered considerable attention due to their notable explanation performance and desirable axiomatic properties. However, IG-based methods integrate noise in their attribution. Previous works (Kapishnikov et al., 2021) have explored the possible origin of this attribution noise and attempted to eliminate it.

The Important Direction Gradient Integration (IDGI) framework is a recent development that has tackled this issue and reported better results. The paper (Yang et al., 2023) highlights the reason behind the noise in the explanation. It proposes a framework to mathematically eliminate the components in the integration calculation that contribute to the noise in the attribution. It also introduced a new measurement, AIC and SIC (Kapishnikov et al., 2019) using MS-SSIM to estimate the entropy of an image more accurately by improving upon previously proposed metrics (Kapishnikov et al., 2019; Kancharla & Channappayya, 2018; Ma et al., 2016; Odena et al., 2017). They further evaluate 11 standard, pre-trained ImageNet classifiers with the three existing IG-based methods (IG, BlurIG, and, GIG), and propose one attribution assessment technique (AIC and SIC using MS-SSIM).

A detailed examination of IDGI and related works encouraged us to put forward some well-thought inquiries that we attempt to resolve using our own mathematical observations and experimental findings. The necessity of this study arose because IDGI is a relatively new and under-explored work and requires testing and

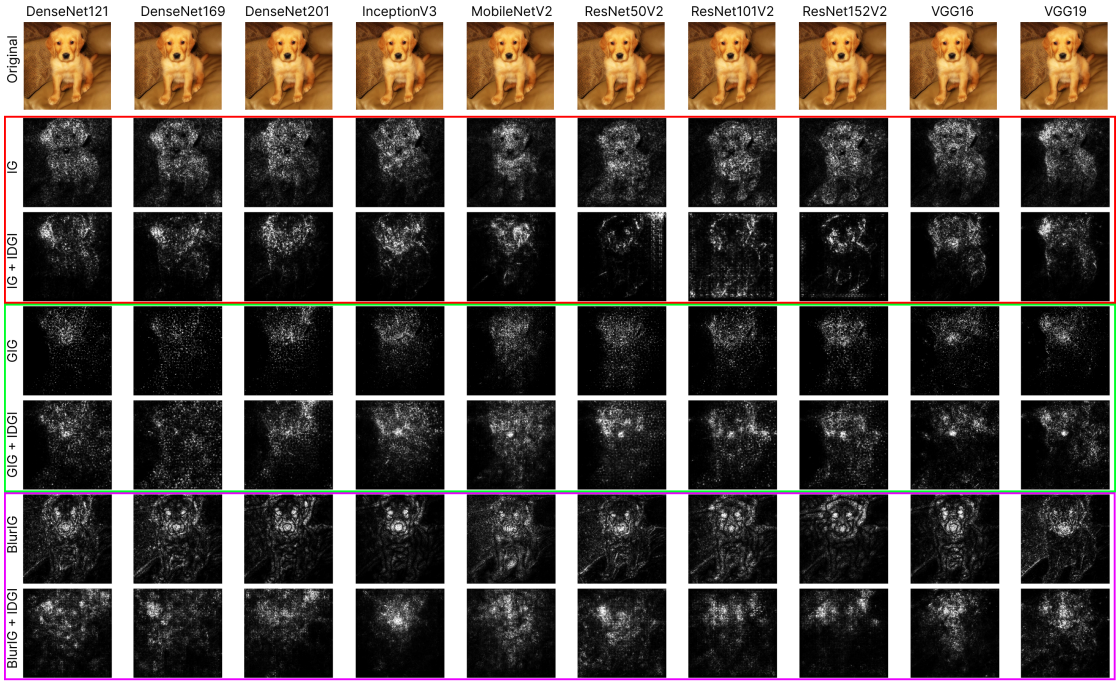

Figure 1: Saliency maps of the existing IG-based methods and those with IDGI on explaining the prediction from all models. While no comments can be made about IDGI's results being objectively better or worse for this instance, it can be seen that IDGI's saliency maps tend to be more patch-like and do not highlight edges of the input image as observed without IDGI.

verification before we can judge its soundness. It was thus important to meticulously question the theoretical basis of the work. Moreover, the official repository of the original paper does not contain the complete code used to produce the results.

During our study, we observed incompleteness in the resources and code provided in the paper; for example, there was no publicly available code for weakly supervised localization methods (Xu et al., 2020; Kapishnikov et al., 2019; Cong et al., 2018), and ambiguity in their implementation details, specifically which dataset was used to compute them. We thus identified the need to perform an elaborate investigation to understand better the contributions made in the paper.

In our work, we address these concerns, and based on our study and experiments, we ask ourselves:

- **Q1**: What is the validity of the claim that IDGI improves upon its baseline methods?
- **Q2**: What are the theoretical implications of IDGI? Under what conditions is it valid?
- **Q3**: The number of steps used in the Riemann approximation of the integral used in IG-based methods is an important parameter. In most previous works, it has been overlooked, and the choice of step size remains vague. We thus ask ourselves: How does the variation in step size impact the performance of IDGI compared to the underlying IG methods?
- **Q4**: During our initial experimentation, we observed stark visual differences in the saliencies computed for GIG on GPU and CPU. This led us to ask whether or not IDGI affects the numerical stability of the underlying attribution method.

Our contributions and findings are as follows:

- We answer **Q1** in Section 4, where we present the results obtained from experiments to compare our results with the authors' findings. We observed that our results mostly matched their claims.

- We answer **Q2** in Section 3. Firstly, we report two errors in the illustration of IDGI provided in the original paper and present our improved illustration of IDGI that correctly demonstrates the path corresponding to IG, GIG, and BlurIG. Secondly, we derive the expression for x_{j_p}, an important term in the IDGI algorithm. While the original paper mentions the expression, it does not discuss how it was obtained. The expression's derivation gives us insights into how IDGI's performance is affected by step size variations. This led us to ask **Q3**.

- We answer **Q3** in Section 4.5.1. We verify the insights we obtained from the theoretical analysis of the expression for the abovementioned x_{j_p} term. We also vary the step size used to compute the Riemann sum for IG and BlurIG. We arrive at a noteworthy conclusion: IDGI is more sensitive to step-size variation than its underlying IG method. We successfully proved this through rigorous theoretical analysis of how the step size and the performance of IDGI are linked. We then confirmed our theory through our experimental findings.

- We answer **Q4** in Section 4.5.2. We perform an additional experiment with the aim of quantitatively comparing the saliency map produced for an image and a compressed version of the same image.

- We could not directly use the existing code for our study This led us to integrate the code for IDGI [1] provided by the authors and use the original implementations [2] of the authors' code for IG, GIG, and BlurIG. The code provided by the repository was not usable for reproducing results at scale. Our code makes better use of HPC resources and is better structured for reproducing results. We provide more details regarding this in later sections.

This paper has been organized as follows: We begin with a brief background on the original Integrated Gradients method and its variants, BlurIG and GIG, in Section 2. Readers familiar with these can skip to Section 3, where we summarize the IDGI algorithm, followed by the complete derivation of x_{j_p}, as previously mentioned, and an in-depth discussion on IDGI's sensitivity to step-size variation. We also present an improved illustration of IDGI. Finally, Section 4 presents our experimental results, including implementation details, computational requirements, and results beyond the original paper. We also use this section to describe the difficulties we faced during the study due to the lack of details on implementation.

2 Background

2.1 Integrated Gradients

Let f be a classifier, c, a class, and x, an input, then, the output $f_c(x)$ represents the confidence score for predicting x to class c. Given $\gamma^{IG}(\alpha), \alpha \in [0,1]$ as the parametric function representing the path from x', the baseline or the reference point, to x, the final or the input image, $\gamma^{IG}(0) = x', \gamma^{IG}(1) = x$, IG specifies γ^{IG} to be a straight line that connects x' and x.

The attribution per feature is calculated by computing the line integral between the reference point x' and image x in the vector field that the model creates. The vector is formed by the gradient of $f_c(x)$ with respect to the input space. The Integrated Gradient for the ith dimension for an input x is defined as below:

$$I_i^{IG}(x) = \int_0^1 \frac{\partial f_c(\gamma^{IG}(\alpha))}{\partial \gamma_i^{IG}(\alpha)} \frac{\partial \gamma_i^{IG}(\alpha)}{\partial \alpha} d\alpha, \tag{1}$$

2.2 Blur Integrated Gradients

Assuming $\gamma(\alpha), \alpha \in [0,1]$ still represents the path from x' to x, BlurIG takes into account this path produced by sequentially blurring the input with a Gaussian blur filter. Let us consider the image to have a 2D shape $M \times N$, and let $x(p,q)$ represent the value of the image x at the location of pixels p and q. The discrete

[1] https://github.com/yangruo1226/IDGI
[2] https://github.com/PAIR-code/saliency

convolution of the input signal with a 2D Gaussian kernel with variance α is then defined as follows:

$$\begin{aligned}\gamma^{BlurIG} &::= L(x, p, q, \alpha) \\ &= \sum_{m=-\infty}^{\infty} \sum_{n=-\infty}^{\infty} \frac{1}{\pi\alpha} e^{-\frac{q^2+p^2}{\alpha}} x(p-m, q-n)\end{aligned} \tag{2}$$

The final BlurIG computation is as follows:

$$I_{p,q}^{BlurIG}(x) = \int_{\infty}^{0} \frac{\partial f_c(\gamma^{BlurIG}(\alpha))}{\partial \gamma_{p,q}^{BlurIG}(\alpha)} \frac{\partial \gamma_{p,q}^{BlurIG}(\alpha)}{\partial \alpha} d\alpha, \tag{3}$$

2.3 Guided Integrated Gradients

Guided Integrated Gradients (GIG) iteratively find the integration path $\gamma^{IG}(\alpha), \alpha \in [0, 1]$ to avoid the high curvature points in the output shape of DNNs (due to which the larger-magnitude gradients from each feasible point on the path would have a significantly larger effect on the final attribution values.) The new path is defined as follows:

$$\gamma^{GIG} = \arg\min_{\gamma \in \Gamma} \sum_{i=1}^{N} \int_{0}^{1} |\frac{\partial f_c(\gamma(\alpha))}{\partial \gamma_i(\alpha)} \frac{\partial \gamma_i(\alpha)}{\partial \alpha}| d\alpha, \tag{4}$$

where Γ is the set containing all possible path between $x^{'}$ and x. After finding the optimal path γ^{GIG}, GIG uses it and computes the attribution values similar to IG. Formally,

$$I_i^{GIG}(x) = \int_{0}^{1} \frac{\partial f_c(\gamma^{GIG}(\alpha))}{\partial \gamma_i^{GIG}(\alpha)} \frac{\partial \gamma_i^{GIG}(\alpha)}{\partial \alpha} d\alpha. \tag{5}$$

3 Theoretical Analysis of IDGI

Regardless of whichever IG-based approach is used for calculating the attributions, the final attribution map is produced from Riemann Integration in all IG-based algorithms. Yang et al. (2023) explains that each path segment has a noise direction where gradient integration with that direction has a net contribution of zero to the attribution scores.

They also provide an illustration to demonstrate the direction of the noise vector. We make two remarks about the original illustration of IDGI with regard to how it could be misleading:

- The relationship between $f_c(x)$ and x for IG is portrayed as linear; however, that is not so. The relationship between x and α is linear. Thus, this can be an origin of confusion among readers.
- The function $x \to f_c(x)$ should be one-to-one; however the original illustration portrays it to be a one-to-many function, which is not possible.

We present an improved illustration in Figure 2, that counters the two issues we observed.

We now shift our attention to the IDGI algorithm, as present in the original work by Yang et al. (2023). For new readers, we provide a brief summary of the mathematics leading to the IDGI algorithm, as follows: Consider the point $x_j = \gamma(\alpha_j)$ and the next point $x_{j+1} = \gamma(\alpha_{j+1})$ on the path from reference point $x^{'}$ to the input point x. IG-based methods compute the gradient, g, of $f_c(x_j)$ with respect to x and use Riemann integration to perform element-wise multiplication of the gradient and the step, $x_{j+1} - x_j$, which the authors refer to as the *original direction*. Further, they refer to the direction $\frac{g}{|g|}$ as the *important direction*. The gradient of the function value f_c at each point in space defines the conservative vector field, where an infinite number of hyperplanes h exist, and each hyperplane contains all points. x with the same functional value. In the conservative vector field, separate hyperplanes never intersect, meaning each point has its own projection point with regard to the other hyperplanes. For point x_j, if one moves x_j along the *Important direction*, there

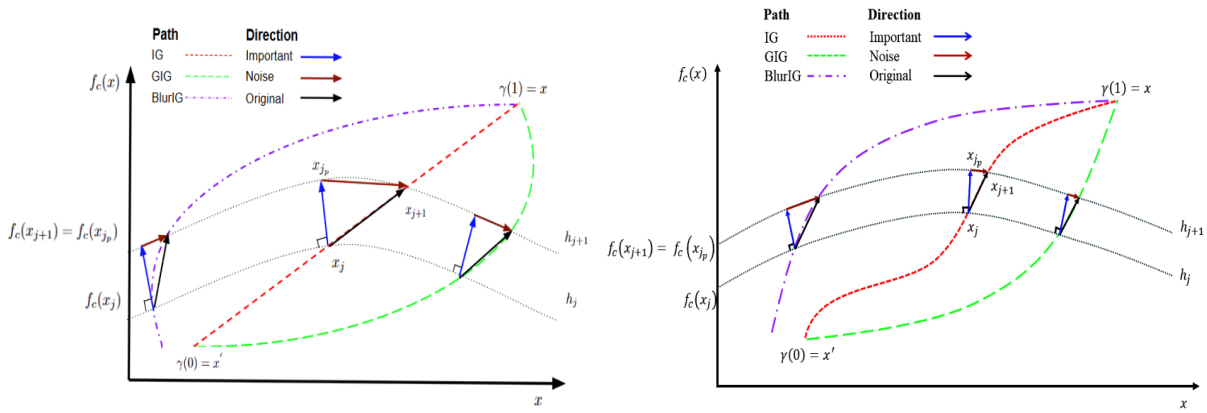

Figure 2: The original illustration of IDGI Yang et al. (2023) (left), our improved illustration(right).

exists a unique projection point x_{j_p} on the hyperplane h_{j+1} where $f_c(x_{j_p}) = f_c(x_{j+1})$. Then the authors present the following theorem, which illustrates that while for a feature, i, the value of the attribution computed from the original direction and the important direction can be different, the change in the value of f_c remains the same.

Theorem 1 *Given a function $f_c(x) : R^n \to R$, points $x_j, x_{j+1}, x_{j_p} \in R^n$, then the gradient of the function with respect to each point in the space R^n forms the conservative vector fields $\overrightarrow{F}$ and further define the hyperplane $h_j = \{x : f_c(x) = f_c(x_j)\}$ in $\overrightarrow{F}$ Assume the Riemann Integration accurately estimates the line integral of the vector field $\overrightarrow{F}$ from points x_j to x_{j+1} and x_{j_p}, e.g., $\int_{x_j}^{x_{j_p}} \frac{\partial f_c(x)}{\partial x} dx \approx \frac{\partial f_c(x_j)}{\partial x_j}(x_{j_p} - x_j)$, and $x_j \in h_j$, $x_{j_p}, x_{j+1} \in h_{j+1}$ Then:*

$$\int_{x_j}^{x_{j+1}} \frac{\partial f_c(x)}{\partial x} dx \approx \int_{x_j}^{x_{j_p}} \frac{\partial f_c(x)}{\partial x} dx.$$

We now derive the expression for x_{j_p}: Let x be a given input with target class c, f be a given classifier, $[x^{'}, ..., x_j, ...x]$ be a given path from any IG-based method and g be the gradient of $f_c(x_j)$ with respect to x. Then, according to the IDGI Algorithm, the important direction vector of g is determined as $\frac{g}{|g|}$ and the step size as $\frac{f_c(x_{j+1}) - f_c(x_j)}{|g|}$. The projection of x_j onto the hyperplane h_{j+1}, formed as $x_{j_p} = x_j + \frac{g}{|g|} \frac{f_c(x_{j+1}) - f_c(x_j)}{|g|}$, has the same functional value as point x_{j+1}, i.e., $f_c(x_{j+1}) = f_c(x_{j_p})$.

Here, we observed that the Taylor series approximation is necessary to arrive at the expression for x_{j_p}. Assuming x_{j_p} lies on the given path from any IG-based method such that it is defined as $x_{j_p} = x_j + c \cdot \frac{g}{|g|}$, where c is the length of the projection that we wish to approximate.

Derivation.

$$x_{j_p} = x_j + c \cdot \frac{g}{|g|} \implies f_c(x_{j_p}) = f_c(x_j + c \cdot \frac{g}{|g|})$$

By Taylor series approximation,

$$f_c(x_{j+1}) = f_c(x_{j_p}) \approx f_c(x_j) + \nabla f \cdot (c \cdot \frac{g}{|g|})$$

$$\therefore f_c(x_{j+1}) \approx f_c(x_j) + c \cdot |g| \implies c \approx \frac{f_c(x_{j+1}) - f_c(x_j)}{|g|}$$

$$\therefore x_{j_p} \approx x_j + \frac{g}{|g|} \cdot \frac{f_c(x_{j+1}) - f_c(x_j)}{|g|}$$

We arrive at the final expression for x_{j_p} using the Taylor series approximation, implying that the value of $f_c(x_j + \frac{g}{|g|} \cdot \frac{f_c(x_{j+1}) - f_c(x_j)}{|g|}) \approx f_c(x_{j+1})$. Hence, while x_{j_p} and x_{j+1} theoretically lie on the same hyperplane, the approximated value of x_{j_p} (used in practice) and x_{j+1} only approximately lie on the same hyperplane.

This implies that the more accurate derivation of x_{j_p} comes not from Theorem 1, as the authors suggest, but from the Taylor series approximation.

How does IDGI vary with step size?

As previously mentioned, the derivation for x_{j_p} gives us insights into how IDGI's performance is affected by step size variations. The expression for c, the length of the projection, determines the validity of the Taylor series approximation. The smaller the value of c, the more valid the approximation. We observe that c is directly proportional to $f_c(x_{j+1}) - f_c(x_j)$. Here, x_{j+1} and x_j are consecutive points in the path of an IG-based method. It is easy to observe that for the same path, these two points are closer to each other for a larger number of steps (since the number of steps denotes the finite number of small piece-wise linear segments that we discretize the path between $x^{'}$ and x into.) This implies that $f_c(x_{j+1})$ and $f_c(x_j)$ are closer in value. Therefore, a larger number of steps is required for a smaller c. The expression of x_{j_p} is thus directly linked to the number of steps, and thus, the step size used for the algorithm. This, in turn, means that IDGI is sensitive to step size variation.

4 Experimental Methodology and Results

Before detailing the experimental setting and presenting our results, we address the difficulties we faced while carrying out our experiments. We found that the official code for IDGI contained only the algorithmic implementation of the method, and the PAIR Saliency page showed the results for each method on a single image and a single model. Thus, the available code was insufficient to reproduce all the results of IDGI. We had to perform the following tasks ourselves,

- The saliency masks had to be calculated for 10 models and 6 methods, each followed by every quantitative metric used by the authors of IDGI, and on $\sim$ 35K images. We thus had to optimize the code and implement batched computations to improve speed due to limited time and resources.
- To run the code, we wrote scripts to automate calculating the saliencies on all the 6 methods. Following this task, we also ran scripts to compute the metrics, which was computationally expensive.
- We had to write the code ourselves to compute Insertion Scores, SIC, and AIC using MS-SSIM as well as Normalized Entropy since the authors had modified the original implementation and had not provided the modified code for it.

4.1 Experimental Setup

We use the same baseline methods (IG, GIG, and BlurIG) as the authors' original work. Following the implementations of IDGI, we also use the original implementations with default parameters in the authors' code for IG, GIG, and BlurIG. We use the black image as the reference point for IG and GIG. Finally, as previously mentioned, we use different step sizes (8, 16, 32, 64, and 128) as an additional experiment beyond the original paper to verify our hypothesis on how sensitive IDGI is to step size. We also report our findings on the effect of IDGI on the numerical stability of the attribution methods.

Models. We use the Pytorch (1.13.1) pre-trained models: DenseNet121, 169, 201, InceptionV3, MobileNetV2, ResNet50,101,151V2, and VGG16,19. We did not use Xception due to computational constraints.
Datasets. We used the same dataset as that used in the original paper - The Imagenet validation dataset, which contains 50K test samples with labels and annotations. We also tested the explanation methods for each model on images that show that the model predicted the label correctly, which varies from 33K to 39K, corresponding to different models.

Evaluation Metrics. We use four evaluation metrics - Insertion Score (Pan et al., 2021; Petsiuk et al.), the Softmax information curves (SIC), and the Accuracy information curves (AIC) (Kapishnikov et al., 2021;

2019) using Normalized Entropy and the modified version of SIC and AIC with MS-SSIM as introduced in the original IDGI paper. We follow the implementation details described in previous works, as is done in the original paper. We did not compute the three Weakly Supervised Localization metrics because, according to previous works from which Yang et al. (2023) borrowed the implementation details, we require the Imagenet segmentation dataset to compute these metrics. There exist three versions of this dataset, and neither the previous works (Xu et al., 2020; Kapishnikov et al., 2021; 2019) nor Yang et al. (2023) mention which version of the dataset they used. Calculating the metrics for all three dataset versions was not computationally feasible. Furthermore, none of the works provide the code to calculate these metrics.

Computational Requirements. We used a single NVIDIA Tesla V100 GPU with 16 GB of VRAM for our reproducibility experiments. The compute time varies slightly with the model, the method, and the step size. We report the average compute time per method per model for 128 steps: computing the saliencies took approximately 9 hours, computing SIC and AIC using Normalized Entropy and MS-SSIM took 90 minutes in total, and computing insertion scores took 70 minutes.

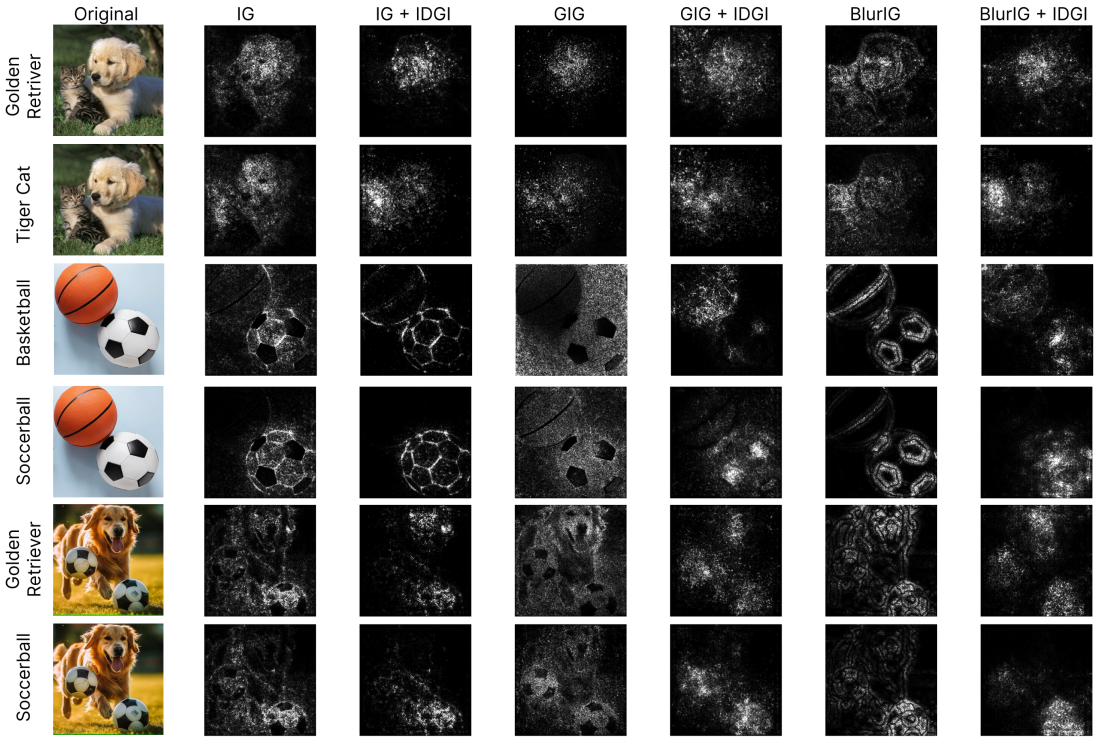

Figure 3: Saliency map of the existing IG-based methods and those with IDGI on explaining the prediction from InceptionV3. We compare two sets of saliencies for each image by taking the top 2 distinct classes as the predicted class by the model. While the top class object is always more highlighted, we observe that all IG-based methods with IDGI are slightly better at highlighting each class than methods without IDGI.

4.2 Insertion Score

We begin by assessing the explanation approaches with the Insertion Score from prior works (Pan et al., 2021; Petsiuk et al.). We re-wrote the available code according to the modified implementation details introduced in the paper (Yang et al., 2023) and evaluated each of the three baselines (IG, GIG, and BlurIG) across 10 models. We report the insertion scores for 128 steps in Table 1.

Based on the results we obtained, we find that our results match the claims made in the original paper for the most part, and the better explanation method has a higher insertion score. However, we observed that for MobileNetv2, ResNet50v2, and ResNet101v2, IDGI worsens the insertion scores for BlurIG.

Metrics	Models	IG-based Methods					
		IG	+IDGI	GIG	+IDGI	BlurIG	+IDGI
Insertion Score with Probability (↑)	*DenseNet121*	.127	**.374**	.155	**.299**	.080	**.281**
	DenseNet169	.130	**.388**	.152	**.320**	.088	**.291**
	DenseNet201	.152	**.390**	.177	**.333**	.107	**.316**
	InceptionV3	.135	**.419**	.160	**.399**	.102	**.379**
	MobileNetV2	.038	**.149**	.037	**.140**	**.202**	.201
	ResNet50V2	.062	**.120**	.057	**.207**	**.241**	.237
	ResNet101V2	.184	**.262**	.213	**.396**	**.430**	.423
	ResNet152V2	.197	**.270**	.223	**.408**	.140	**.377**
	VGG16	.049	**.287**	.056	**.200**	.039	**.231**
	VGG19	.058	**.319**	.069	**.233**	.256	**.285**
Insertion Score with Probability Ratio (↑)	*DenseNet121*	.144	**.415**	.177	**.334**	.091	**.312**
	DenseNet169	.142	**.418**	.167	**.348**	.097	**.315**
	DenseNet201	.168	**.427**	.198	**.368**	.119	**.347**
	InceptionV3	.160	**.483**	.191	**.464**	.122	**.437**
	MobileNetV2	.104	**.364**	.106	**.366**	**.530**	.529
	ResNet50V2	.152	**.285**	.140	**.504**	**.581**	.573
	ResNet101V2	.252	**.355**	.291	**.539**	**.582**	.574
	ResNet152V2	.266	**.363**	.301	**.549**	.187	**.504**
	VGG16	.057	**.317**	.067	**.225**	.045	**.255**
	VGG19	.067	**.352**	.082	**.262**	.291	**.322**

Table 1: Insertion Score for explanation methods using 128 steps. The claim that IDGI improves all methods for all models does not hold true.

4.3 SIC and AIC using Normalized Entropy

Metrics	Models	IG-based Methods					
		IG	+IDGI	GIG	+IDGI	BlurIG	+IDGI
AUC AIC (↑)	*DenseNet121*	.134	**.476**	.080	**.384**	.200	**.349**
	DenseNet169	.141	**.465**	.096	**.398**	.200	**.342**
	DenseNet201	.191	**.484**	.122	**.418**	.267	**.387**
	InceptionV3	.195	**.554**	.128	**.491**	.277	**.478**
	MobileNetV2	.056	**.410**	.043	**.313**	**.570**	.531
	ResNet50V2	.054	**.265**	.048	**.313**	**.617**	.580
	ResNet101V2	.174	**.354**	.154	**.523**	**.693**	.663
	ResNet152V2	**.352**	.345	.151	**.528**	.298	**.464**
	VGG16	.041	**.369**	.029	**.268**	.077	**.311**
	VGG19	.052	**.378**	.033	**.294**	.412	**.421**
AUC SIC (↑)	*DenseNet121*	.010	**.435**	.005	**.311**	.038	**.261**
	DenseNet169	.011	**.438**	.006	**.346**	.042	**.266**
	DenseNet201	.027	**.455**	.009	**.369**	.104	**.320**
	InceptionV3	.016	**.527**	.008	**.465**	.066	**.436**
	MobileNetV2	.005	**.201**	.005	**.121**	**.362**	.348
	ResNet50V2	.005	**.075**	.005	**.132**	**.425**	.408
	ResNet101V2	.025	**.241**	.015	**.470**	**.588**	.570
	ResNet152V2	**.260**	.240	.015	**.486**	.113	**.395**
	VGG16	.005	**.304**	.005	**.160**	.005	**.218**
	VGG19	.005	**.316**	.005	**.197**	.336	**.353**

Table 2: Area under the curve for for AIC and SIC using Normalized Entropy for 128 steps. The claim that IDGI improves all three IG-based methods across all experiment settings does not hold true.

Metrics	Models	IG-based Methods					
		IG	+IDGI	GIG	+IDGI	BlurIG	+IDGI
AUC AIC (↑)	*DenseNet121*	.164	**.302**	.141	**.283**	.188	**.279**
	DenseNet169	.173	**.300**	.155	**.292**	.192	**.285**
	DenseNet201	.196	**.312**	.169	**.301**	.216	**.302**
	InceptionV3	.212	**.347**	.192	**.345**	.236	**.340**
	MobileNetV2	.124	**.253**	.110	**.243**	.287	**.297**
	ResNet50V2	.135	**.232**	.121	**.252**	.312	**.322**
	ResNet101V2	.206	**.261**	.192	**.325**	.340	**.354**
	ResNet152V2	.262	**.267**	.192	**.330**	.219	**.319**
	VGG16	.092	**.255**	.084	**.218**	.114	**.236**
	VGG19	.103	**.260**	.092	**.229**	.218	**.258**
AUC SIC (↑)	*DenseNet121*	.106	**.260**	.093	**.242**	.149	**.237**
	DenseNet169	.123	**.267**	.109	**.262**	.162	**.253**
	DenseNet201	.135	**.278**	.113	**.268**	.179	**.267**
	InceptionV3	.137	**.308**	.126	**.310**	.186	**.301**
	MobileNetV2	.050	**.141**	.047	**.141**	.173	**.184**
	ResNet50V2	.065	**.136**	.055	**.159**	.207	**.214**
	ResNet101V2	.148	**.209**	.132	**.277**	.269	**.283**
	ResNet152V2	**.221**	**.221**	.140	**.289**	.171	**.276**
	VGG16	.055	**.213**	.051	**.178**	.076	**.195**
	VGG19	.061	**.221**	.056	**.191**	.165	**.213**

Table 3: Area under the curve for for AIC and SIC using MS-SSIM for 128 steps. The claim that IDGI improves all three IG-based methods across all experiment settings does not hold true.

We evaluated the explanation methods using the Softmax information curves (SIC) and the Accuracy information curves (AIC) using Normalized Entropy. We re-wrote the available code according to the modified implementation details introduced in the paper (Yang et al., 2023) and evaluated each of the three baselines. We report the area under the AIC and SIC curves for 128 steps in Table 2.

Based on the results we obtained, we find that our results match the claims made in the original paper (Yang et al., 2023) for the most part, and the better explanation method has a higher area under the AIC and SIC curves. However, we observed that for ResNet152v2, IDGI worsens the area under the AIC and SIC curves for IG; and, for MobileNetv2, ResNet50v2, and ResNet101v2, BlurIG + IDGI also underperforms BlurIG. A common trait observed in the models that exhibit anomalies is that they all implement residual connections in their architecture. While we could not demonstrate how this may cause IDGI to reduce the performance of the underlying method, it is a plausible hypothesis that the residual connections might interact with the IDGI framework in ways that are not fully understood, warranting further investigation into the underlying mechanisms and their impact on explanation methods.

4.4 SIC and AIC with MS-SSIM

We now evaluate the explanation methods using the Softmax information curves (SIC) and the Accuracy information curves (AIC) using MS-SSIM (Kancharla & Channappayya, 2018; Ma et al., 2016; Odena et al., 2017), a well-studied image quality evaluation method that analyzes the structural similarity of two images. We re-wrote the available code according to the modified implementation details introduced in the paper (Yang et al., 2023) and evaluated each of the three baselines (IG, GIG, and BlurIG) across 10 models. We report the area under AIC and SIC for 128 steps in Table 3.

Based on the results we obtained, we find that our results match the claims made in the original paper (Yang et al., 2023) consistently. The better explanation method has a higher area under the AIC and SIC curves. However, for ResNet152V2 the area under SIC for IG is equal to that for IG + IDGI.

4.5 Additional Experiments

4.5.1 Step Size Variation

IG-based methods	Insertion score with probability	Insertion score with probability ratio	AIC with Normalized Entropy	SIC with Normalized Entropy	AIC with MS-SSIM	SIC with MS-SSIM
IG	.024	.026	.033	.004	.010	.002
IG + IDGI	.224	.250	.350	.473	.098	.106
BlurIG	.004	.006	.124	.054	.041	.040
BlurIG+IDGI	.082	.087	.146	.202	.044	.049

Table 4: Difference in score between 8 and 128 steps for InceptionV3 (%)

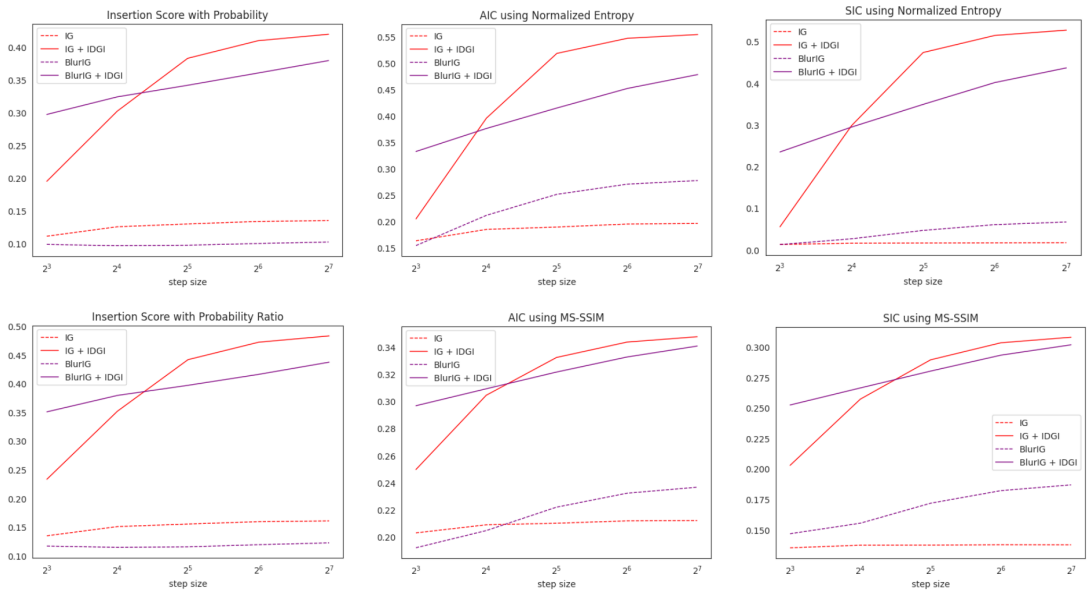

Figure 4: Insertion Score with probability and probability ratio, AIC and SIC using Normalized Entropy and MS-SSIM vs. number of steps, for Inceptionv3.

As mentioned in Section 1 and discussed in Section 3, we now proceed to show our results for step-size variation and evaluate its effect on IDGI compared to the baselines (IG, GIG, and BlurIG). We report our results through Figure 4 where we study the variation of the value of the respective metric versus the number of steps (8, 16, 32 and 64) for InceptionV3. Increasing the number of steps leads to a better score, as a higher number of steps in the Riemann sum leads to a finer approximation of the actual integral. However, due to computational limitations, increasing the number of steps requires more resources and time, necessitating a trade-off. The developer must make a choice based on the sensitivity of the application and resources available. It must be highlighted that the x-axis is in exponential scale, which means that beyond a step-size of ∼32 the return in score improvement per step is marginal. We observe that at a higher step size, the scores of BlurIG+IDGI are lower than those for IG+IDGI. To explain this, we analyse the IDGI algorithm and observe the relationship between d, and I_i^{IDGI}, the attribution value for IDGI. α, x,f,c, and $path$ are as defined in Section 3.

Algorithm 1 Important Direction Gradient Integration

Inputs: x, f, c, $path : [x', \ldots, x_j, \ldots, x]$
$I_i^{IDGI} = 0$
for $x_j \in path$ **do**
  $d = f_c(x_{j+1}) - f_c(x_j)$
  $g = \frac{\partial f_c(x_j)}{\partial x}$
  $I_i^{IDGI} \mathrel{+}= \frac{g_i \times g_i \times d}{g \cdot g}$
end for
return I^{IDGI}

As shown in Figure 5, the variation in the image for BlurIG is minimal for most of the path, with significant sharpening occurring only in the final ∼10% of the steps. This suggests that f is a constant, low value for most of the sampled points. In contrast, the image brightness increases uniformly along the IG path, indicating a more steady change in f. The change between two subsequent steps (d) determines the magnitude of the integrand added to the final saliency. Consequently, for BlurIG+IDGI, most samples contribute minimally to the final saliency. Both IG+IDGI and BlurIG+IDGI benefit from increased steps, improving the approximation of the underlying integral. However, IG+IDGI generally benefits more due to the more uniform change in probability scores along most of the path.

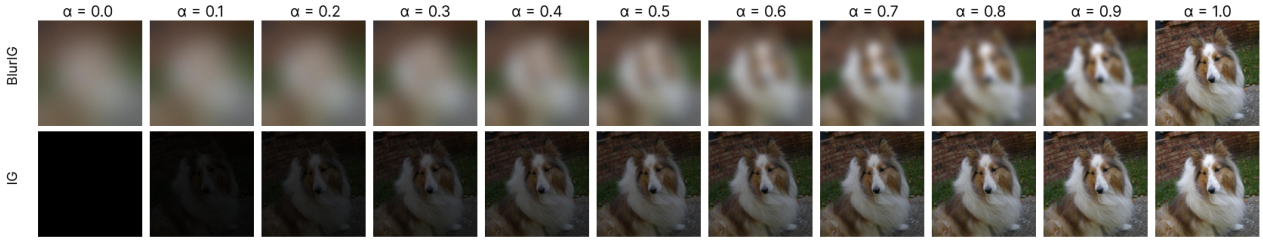

Figure 5: Images observed along the path of BlurIG and IG. For BlurIG, for most values of α, we notice minimal changes in the image with small increments. In contrast, for IG, a uniform change in the image is observed with the same increments in α.

In the Appendix, we report the insertion scores and area under AIC and SIC using Normalized Entropy and MS-SSIM for the remaining models, for 8, 16, 32 and 64 steps. According to our experimental results, our theoretical analysis is verified and stands correct. We observe that IDGI is consistently more variant to the number of steps than its baselines.

4.5.2 Numerical Instability

IG-based Methods	- log MSE
IG	2.619
IG + IDGI	**8.949**
GIG	0.845
GIG + IDGI	**8.029**
BlurIG	3.466
BlurIG + IDGI	**8.778**

Table 5: The negative log values of MSE computed between the saliencies of the compressed images and the non-compressed images for InceptionV3. Higher values indicate better numerical stability

During our early experimental stage, we observed that, visually, the saliency maps obtained for GIG were starkly different when computed on GPU and CPU. This phenomenon is undesirable as it makes the attribu-

tion method unreliable. Hence, we decided to study the numerical instability of different attribution methods. We used JPEG compression using a retention factor of 75% to compress all the images of the dataset. Then, we computed the saliencies using *InceptionV3* for this new dataset and took the mean squared error (MSE) of each saliency with those of the non-compressed images to find the pixel-level variation. The slight compression retains the overall image structure and information; hence, we expect numerically stable methods to have a small MSE. We chose this route of experimentation because computing the saliencies on the CPU would be unfeasibly slow. We perform this experiment for IDGI and each of the underlying methods: IG, BlurIG, and GIG. Based on our experimental results, we observe that baseline method + IDGI achieves significantly better numerical stability (smaller MSE) than the baseline method. Also, GIG shows really poor numerical stability, as we had anticipated from visual observations.

5 Conclusion

We rigorously analyse the theoretical aspects of IDGI, experimentally verify the claims made by Yang et al. (2023), and perform additional experiments to verify our theoretical observations and understand the numerical stability of the framework. While the claim that IDGI always improves upon all baseline methods mostly holds true, for MobileNetV2 and the ResNet family, for some baseline methods our experimental results show otherwise. As per our theoretical and experimental analysis, IDGI is more sensitive to step size variation than the baseline methods. Applying IDGI makes the baseline method more class-sensitive, a desirable property. We also observe that IDGI + baseline method is more numerical stable than the baseline.

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A Appendix

Table 6 to Table 17 show the insertion scores with probability and probability ratio, the area under AIC and SIC using Normalized Entropy and MS-SSIM for 4 methods (baseline methods, IG and BlurIG + IDGI) across the 10 models that we performed the experiments on for 64, 32, 16 and 8 steps (in that order). We could not perform these experiments for GIG due to computational constraints.

We have highlighted the better performing method in each Table.

Metrics	**Models**	**IG-based Methods**			
		IG	+IDGI	BlurIG	+IDGI
Insertion Score with Probability (↑)	*DenseNet121*	.127	**.357**	.080	**.265**
	DenseNet169	.128	**.359**	.088	**.277**
	DenseNet201	.150	**.368**	.106	**.303**
	InceptionV3	.133	**.409**	.100	**.360**
	MobileNetV2	.038	**.122**	**.202**	.198
	ResNet50V2	.059	**.099**	**.241**	.233
	ResNet101V2	.171	**.223**	**.429**	.417
	ResNet152V2	.181	**.222**	.140	**.355**
	VGG16	.048	**.282**	.039	**.215**
	VGG19	.058	**.313**	.255	**.275**
Insertion Score with Probability Ratio (↑)	*DenseNet121*	.143	**.397**	.090	**.295**
	DenseNet169	.141	**.388**	.096	**.300**
	DenseNet201	.167	**.404**	.118	**.332**
	InceptionV3	.159	**.472**	.118	**.416**
	MobileNetV2	.103	**.299**	**.529**	.520
	ResNet50V2	.145	**.237**	**.581**	.564
	ResNet101V2	.235	**.303**	**.581**	.566
	ResNet152V2	.245	**.300**	.186	**.475**
	VGG16	.057	**.313**	.045	**.239**
	VGG19	.067	**.346**	.290	**.311**

Table 6: Insertion score for different models with explanation methods for 64 steps.

Metrics	**Models**	**IG-based Methods**			
		IG	+IDGI	BlurIG	+IDGI
AUC AIC (↑)	*DenseNet121*	.133	**.464**	.193	**.328**
	DenseNet169	.139	**.440**	.193	**.323**
	DenseNet201	.189	**.467**	.260	**.370**
	InceptionV3	.194	**.547**	.270	**.451**
	MobileNetV2	.054	**.337**	**.572**	.520
	ResNet50V2	.052	**.183**	**.618**	.567
	ResNet101V2	.154	**.276**	**.692**	.652
	ResNet152V2	**.322**	.254	.291	**.428**
	VGG16	.041	**.368**	.073	**.288**
	VGG19	.052	**.376**	**.409**	**.409**
AUC SIC (↑)	*DenseNet121*	.010	**.414**	.034	**.232**
	DenseNet169	.011	**.399**	.037	**.239**
	DenseNet201	.026	**.428**	.094	**.293**
	InceptionV3	.016	**.514**	.059	**.401**
	MobileNetV2	.005	**.127**	**.363**	.340
	ResNet50V2	.005	**.028**	**.426**	.404
	ResNet101V2	.020	**.168**	**.588**	.564
	ResNet152V2	**.229**	.150	.103	**.349**
	VGG16	.005	**.301**	.005	**.183**
	VGG19	.005	**.312**	.332	**.337**

Table 7: AUC for AIC and SIC using Normalized Entropy for 64 steps.

Metrics	Models	IG-based Methods			
		IG	+IDGI	BlurIG	+IDGI
AUC AIC (↑)	*DenseNet121*	.164	**.297**	.184	**.272**
	DenseNet169	.173	**.292**	.188	**.279**
	DenseNet201	.196	**.306**	.212	**.297**
	InceptionV3	.211	**.343**	.232	**.332**
	MobileNetV2	.123	**.230**	.287	**.293**
	ResNet50V2	.134	**.205**	.313	**.317**
	ResNet101V2	.201	**.238**	.339	**.352**
	ResNet152V2	**.255**	.240	.215	**.309**
	VGG16	.092	**.253**	.110	**.228**
	VGG19	.103	**.258**	.217	**.254**
AUC SIC (↑)	*DenseNet121*	.106	**.254**	.144	**.230**
	DenseNet169	.123	**.258**	.158	**.247**
	DenseNet201	.135	**.270**	.175	**.261**
	InceptionV3	.137	**.303**	.182	**.293**
	MobileNetV2	.050	**.123**	.172	**.180**
	ResNet50V2	.065	**.112**	.207	**.212**
	ResNet101V2	.144	**.187**	.269	**.281**
	ResNet152V2	**.213**	.193	.166	**.265**
	VGG16	.055	**.212**	.073	**.185**
	VGG19	.061	**.219**	.164	**.209**

Table 8: AUC for SIC and AIC using MS-SSIM for 64 steps.

Metrics	Models	IG-based Methods			
		IG	+IDGI	BlurIG	+IDGI
Insertion Score with Probability (↑)	*DenseNet121*	.124	**.290**	.078	**.246**
	DenseNet169	.125	**.268**	.087	**.259**
	DenseNet201	.147	**.292**	.105	**.284**
	InceptionV3	.129	**.382**	.097	**.341**
	MobileNetV2	.037	**.099**	**.202**	.193
	ResNet50V2	.058	**.094**	**.240**	.229
	ResNet101V2	.166	**.195**	**.427**	.409
	ResNet152V2	.176	**.201**	.140	**.329**
	VGG16	.048	**.265**	.040	**.196**
	VGG19	.057	**.288**	.251	**.260**
Insertion Score with Probability Ratio (↑)	*DenseNet121*	.140	**.324**	.088	**.275**
	DenseNet169	.137	**.292**	.095	**.281**
	DenseNet201	.163	**.323**	.116	**.313**
	InceptionV3	.154	**.441**	.115	**.396**
	MobileNetV2	.101	**.247**	**.528**	.510
	ResNet50V2	.142	**.225**	**.579**	.553
	ResNet101V2	.228	**.266**	**.578**	.554
	ResNet152V2	.238	**.272**	.187	**.442**
	VGG16	.056	**.294**	.046	**.219**
	VGG19	.067	**.319**	.285	**.295**

Table 9: Insertion score for different models with explanation methods for 32 steps.

Metrics	Models	IG-based Methods			
		IG	+IDGI	BlurIG	+IDGI
AUC AIC (↑)	*DenseNet121*	.132	**.396**	.173	**.296**
	DenseNet169	.135	**.342**	.175	**.295**
	DenseNet201	.186	**.385**	.238	**.342**
	InceptionV3	.188	**.518**	.250	**.414**
	MobileNetV2	.050	**.261**	**.573**	.508
	ResNet50V2	.047	**.147**	**.617**	.554
	ResNet101V2	.144	**.230**	**.690**	.638
	ResNet152V2	**.305**	.217	.278	**.378**
	VGG16	.041	**.351**	.066	**.256**
	VGG19	.052	**.353**	**.405**	.392
AUC SIC (↑)	*DenseNet121*	.010	**.314**	.024	**.186**
	DenseNet169	.010	**.253**	.026	**.197**
	DenseNet201	.025	**.305**	.070	**.252**
	InceptionV3	.015	**.473**	.046	**.348**
	MobileNetV2	.005	**.065**	**.362**	.333
	ResNet50V2	.005	**.015**	**.424**	.398
	ResNet101V2	.016	**.119**	**.586**	.555
	ResNet152V2	**.209**	.116	.087	**.284**
	VGG16	.005	**.275**	.005	**.134**
	VGG19	.005	**.278**	**.326**	.313

Table 10: AUC for AIC and SIC using Normalized Entropy for 32 steps.

Metrics	Models	IG-based Methods			
		IG	+IDGI	BlurIG	+IDGI
AUC AIC (↑)	*DenseNet121*	.163	**.286**	.172	**.261**
	DenseNet169	.172	**.273**	.178	**.270**
	DenseNet201	.195	**.293**	.201	**.287**
	InceptionV3	.210	**.332**	.221	**.321**
	MobileNetV2	.120	**.205**	.283	**.286**
	ResNet50V2	.132	**.189**	.309	**.311**
	ResNet101V2	.198	**.220**	.337	**.347**
	ResNet152V2	**.250**	.225	.209	**.294**
	VGG16	.093	**.249**	.104	**.215**
	VGG19	.103	**.253**	.212	**.248**
AUC SIC (↑)	*DenseNet121*	.106	**.242**	.132	**.217**
	DenseNet169	.123	**.236**	.148	**.236**
	DenseNet201	.135	**.254**	.163	**.251**
	InceptionV3	.137	**.289**	.171	**.280**
	MobileNetV2	.049	**.103**	.168	**.175**
	ResNet50V2	.065	**.099**	.204	**.207**
	ResNet101V2	.142	**.168**	.267	**.277**
	ResNet152V2	**.209**	.179	.159	**.249**
	VGG16	.055	**.207**	.066	**.172**
	VGG19	.061	**.213**	.158	**.202**

Table 11: AUC for SIC and AIC using MS-SSIM for 32 steps.

Metrics	Models	IG-based Methods			
		IG	+IDGI	BlurIG	+IDGI
Insertion Score with Probability (↑)	*DenseNet121*	.115	**.189**	.079	**.226**
	DenseNet169	.117	**.169**	.088	**.237**
	DenseNet201	.138	**.191**	.106	**.264**
	InceptionV3	.125	**.302**	.096	**.323**
	MobileNetV2	.037	**.086**	**.199**	**.189**
	ResNet50V2	.058	**.092**	**.235**	**.223**
	ResNet101V2	.165	**.181**	**.421**	.398
	ResNet152V2	.173	**.189**	.142	**.297**
	VGG16	.048	**.212**	.042	**.171**
	VGG19	.056	**.226**	.239	**.245**
Insertion Score with Probability Ratio (↑)	*DenseNet121*	.131	**.214**	.089	**.254**
	DenseNet169	.129	**.187**	.096	**.259**
	DenseNet201	.154	**.215**	.117	**.292**
	InceptionV3	.150	**.351**	.114	**.379**
	MobileNetV2	.100	**.216**	**.521**	**.498**
	ResNet50V2	.141	**.221**	**.566**	**.539**
	ResNet101V2	.226	**.247**	**.570**	**.540**
	ResNet152V2	.234	**.255**	.189	**.402**
	VGG16	.056	**.238**	.049	**.192**
	VGG19	.065	**.253**	.272	**.277**

Table 12: Insertion score for different models with explanation methods for 16 steps.

Metrics	Models	IG-based Methods			
		IG	+IDGI	BlurIG	+IDGI
AUC AIC (↑)	*DenseNet121*	.118	**.269**	.137	**.267**
	DenseNet169	.121	**.218**	.147	**.269**
	DenseNet201	.167	**.257**	.198	**.312**
	InceptionV3	.184	**.395**	.211	**.375**
	MobileNetV2	.045	**.215**	**.564**	**.501**
	ResNet50V2	.044	**.130**	**.610**	**.545**
	ResNet101V2	.137	**.212**	**.686**	**.622**
	ResNet152V2	**.292**	.199	.253	**.324**
	VGG16	.039	**.283**	.054	**.224**
	VGG19	.051	**.281**	**.397**	.375
AUC SIC (↑)	*DenseNet121*	.009	**.158**	.013	**.146**
	DenseNet169	.009	**.111**	.015	**.161**
	DenseNet201	.020	**.145**	.038	**.212**
	InceptionV3	.015	**.297**	.025	**.294**
	MobileNetV2	.005	**.038**	**.355**	**.331**
	ResNet50V2	.005	**.013**	**.416**	**.394**
	ResNet101V2	.015	**.101**	**.582**	**.546**
	ResNet152V2	**.196**	.097	.062	**.215**
	VGG16	.005	**.168**	.005	**.088**
	VGG19	.005	**.170**	**.314**	.287

Table 13: AUC for AIC and SIC using Normalized Entropy for 16 steps.

Metrics	Models	IG-based Methods			
		IG	+IDGI	BlurIG	+IDGI
AUC AIC (↑)	*DenseNet121*	.160	**.268**	.156	**.248**
	DenseNet169	.169	**.239**	.164	**.259**
	DenseNet201	.191	**.265**	.183	**.275**
	InceptionV3	.208	**.304**	.204	**.309**
	MobileNetV2	.116	**.187**	.275	**.281**
	ResNet50V2	.131	**.178**	.302	**.303**
	ResNet101V2	.197	**.210**	.334	**.341**
	ResNet152V2	**.246**	.216	.200	**.276**
	VGG16	.092	**.237**	.100	**.201**
	VGG19	.103	**.238**	.200	**.239**
AUC SIC (↑)	*DenseNet121*	.106	**.219**	.117	**.204**
	DenseNet169	.121	**.202**	.135	**.224**
	DenseNet201	.132	**.220**	.145	**.238**
	InceptionV3	.137	**.257**	.155	**.266**
	MobileNetV2	.048	**.090**	.161	**.171**
	ResNet50V2	.065	**.090**	.197	**.202**
	ResNet101V2	.142	**.158**	.265	**.272**
	ResNet152V2	**.205**	.171	.149	**.230**
	VGG16	.055	**.193**	.068	**.158**
	VGG19	.061	**.195**	.143	**.192**

Table 14: AUC for SIC and AIC using MS-SSIM for 16 steps.

Metrics	Models	IG-based Methods			
		IG	+IDGI	BlurIG	+IDGI
Insertion Score with Probability (↑)	*DenseNet121*	.107	**.139**	.087	**.206**
	DenseNet169	.113	**.121**	.102	**.213**
	DenseNet201	.129	**.139**	.114	**.241**
	InceptionV3	.111	**.195**	.098	**.297**
	MobileNetV2	.036	**.080**	**.193**	.185
	ResNet50V2	.057	**.090**	**.229**	.217
	ResNet101V2	.164	**.176**	**.410**	.386
	ResNet152V2	.172	**.182**	.150	**.255**
	VGG16	.046	**.141**	.046	**.151**
	VGG19	.054	**.148**	.228	**.232**
Insertion Score with Probability Ratio (↑)	*DenseNet121*	.122	**.159**	.099	**.232**
	DenseNet169	.124	**.135**	.111	**.233**
	DenseNet201	.144	**.158**	.126	**.267**
	InceptionV3	.134	**.233**	.116	**.350**
	MobileNetV2	.099	**.206**	**.504**	.488
	ResNet50V2	.140	**.219**	**.552**	.525
	ResNet101V2	.224	**.240**	**.554**	.524
	ResNet152V2	.232	**.246**	.199	**.348**
	VGG16	.054	**.161**	.054	**.170**
	VGG19	.063	**.171**	.259	**.264**

Table 15: Insertion score for different models with explanation methods for 8 steps.

Metrics	Models	IG-based Methods			
		IG	+IDGI	BlurIG	+IDGI
AUC AIC (↑)	*DenseNet121*	.102	**.204**	.098	**.247**
	DenseNet169	.110	**.153**	.121	**.250**
	DenseNet201	.146	**.187**	.145	**.291**
	InceptionV3	.162	**.204**	.153	**.332**
	MobileNetV2	.041	**.196**	**.524**	.497
	ResNet50V2	.040	**.127**	**.573**	.539
	ResNet101V2	.132	**.206**	**.661**	.605
	ResNet152V2	**.283**	.192	.212	**.265**
	VGG16	.036	**.175**	.049	**.206**
	VGG19	.047	**.174**	**.369**	.364
AUC SIC (↑)	*DenseNet121*	.007	**.091**	.007	**.118**
	DenseNet169	.007	**.060**	.010	**.134**
	DenseNet201	.015	**.082**	.017	**.181**
	InceptionV3	.012	**.054**	.012	**.234**
	MobileNetV2	.005	**.029**	**.333**	.329
	ResNet50V2	.005	**.012**	**.400**	.392
	ResNet101V2	.013	**.094**	**.567**	.536
	ResNet152V2	**.187**	.090	.032	**.144**
	VGG16	.005	**.039**	.005	**.062**
	VGG19	.005	**.045**	**.274**	.271

Table 16: AUC for AIC and SIC using Normalized Entropy for 8 steps.

Metrics	Models	IG-based Methods			
		IG	+IDGI	BlurIG	+IDGI
AUC AIC (↑)	*DenseNet121*	.155	**.250**	.147	**.240**
	DenseNet169	.166	**.211**	.162	**.251**
	DenseNet201	.185	**.238**	.172	**.267**
	InceptionV3	.202	**.249**	.195	**.296**
	MobileNetV2	.112	**.177**	.269	**.278**
	ResNet50V2	.129	**.176**	.293	**.298**
	ResNet101V2	.196	**.206**	.328	**.333**
	ResNet152V2	**.244**	.211	.192	**.251**
	VGG16	.090	**.210**	.104	**.194**
	VGG19	.101	**.204**	.198	**.235**
AUC SIC (↑)	*DenseNet121*	.103	**.195**	.113	**.195**
	DenseNet169	.119	**.177**	.132	**.215**
	DenseNet201	.127	**.191**	.136	**.229**
	InceptionV3	.135	**.202**	.146	**.252**
	MobileNetV2	.046	**.083**	.157	**.169**
	ResNet50V2	.064	**.087**	.192	**.200**
	ResNet101V2	.141	**.154**	.260	**.265**
	ResNet152V2	**.203**	.166	.140	**.204**
	VGG16	.054	**.161**	.077	**.150**
	VGG19	.060	**.159**	.141	**.187**

Table 17: AUC for SIC and AIC using MS-SSIM for 8 steps.