A Unified View of cGANs
with and without Classifiers

Abstract

Conditional Generative Adversarial Networks (cGANs) are implicit generative models which allow us to sample from class-conditional distributions. Existing cGAN works are based on a wide range of different architectures and objectives. One popular architecture in earlier works is to include a classifier during training with the assumption that good classifiers can help eliminate samples generated with wrong classes. Nevertheless, including classifiers in cGANs often comes with a side effect of only generating easy-to-classify samples. Recently, some representative cGANs avoid the side effect and reach state-of-the-art performance without having classifiers. Somehow it is not clear whether the classifiers can be resurrected to design better cGANs. In this work, we demonstrate that classifiers can be properly leveraged to improve cGANs. We start by using the decomposition of the joint probability distribution to connect the goals of the cGAN and classifier as a unified framework. The framework, along with a classic energy model to parameterize the distribution, justifies the use of classifiers for cGANs in a principled manner. In addition, it explains several popular cGAN variants, such as ACGAN, ProjGAN, and ContraGAN, as special cases with different levels of approximations. Experimental results demonstrate that the framework outperforms state-of-the-art cGANs on benchmark datasets, especially on the harder Tiny ImageNet.

1 Introduction

Generative Adversarial Networks [GANs; 10] is a family of generative models that are trained from the duel of a generator and a discriminator. The generator aims to generate data from a target distribution, where the fidelity of the generated data is "screened" by the discriminator. Recent studies on the objectives [2, 29, 25, 26], architectures [38, 46], and regularization techniques [13, 35, 47] for GANs have achieved impressive progress on image generation, making GANs the state-of-the-art approach to generate high fidelity and diverse images [3]. Conditional GANs (cGANs) extend GANs to generate data from class-conditional distributions [33, 36, 34, 16]. The capability of conditional generation extends the application horizon of GANs to conditional image generation based on labels [36] or texts [40], speech enhancement [32], and image style transformation [18, 49].

One representative cGAN is Auxiliary Classifier GAN [ACGAN; 36], which decomposes the conditional discriminator to a classifier and an unconditional discriminator. The generator of ACGAN is expected to generate images that convince the unconditional discriminator while being classified to the right class. The classifier plays a pivotal role in laying down the law of conditional generation for ACGAN, making it the very first cGAN that can learn from ImageNet to generate 1000 classes of images [6]. That is, ACGAN used to be a leading cGAN architecture. While the classifier in ACGAN indeed improves the accuracy of conditional generation, deeper studies revealed that the classifier biases the generator to generate easier-to-classify images [42], which in term decreases the capability to match the target distribution.

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Unlike ACGAN, most state-of-the-art cGANs are designed without a classifier. One representative cGAN without a classifier is Projection GAN [ProjGAN; 34], which learns an embedding for each class to form a projection-based conditional discriminator. ProjGAN not only generates higher-quality images than ACGAN, but also achieves superior accuracy for conditional generation without relying on an explicit classifier. In fact, it was found that ProjGAN usually cannot be further improved by adding a classification loss [34]. The finding, along with the success of ProjGAN and other cGANs without classifiers [15, 4], seem to suggest that including a classifier is not helpful for improving the generation quality or accuracy of cGANs.

In this work, we challenge the belief that classifiers are not helpful for cGANs, with the conjecture that leveraging the classifiers appropriately can benefit conditional generation. We propose a framework that pins down the roles of the classifier and the conditional discriminator by first decomposing the joint target distribution with Bayes rule. We then model the conditional discriminator as an energy function, which is a unnormalized log probability. Under the energy function, we derive the corresponding optimization term for the classifier and the conditional discriminator with the help of Fenchel duality to form the unified framework. The framework reveals that a jointly generative model can be trained via two routes, from the aspect of the classifier and the conditional discriminator, respectively. We name our framework Energy-based Conditional Generative Adversarial Networks (ECGAN), which not only justifies the use of classifiers for cGANs in a principled manner, but also explains several popular cGAN variants, such as ACGAN [36], ProjGAN [34], and ContraGAN [16] as special cases with different approximations. After properly combining the objectives from the two routes of the framework, we empirically find that ECGAN outperforms other cGAN variants across different network architectures on benchmark datasets. Most importantly, ECGAN achieves superior quality and accuracy on Tiny ImageNet, which is notably difficult because of its scarcity of data in each class.

We summarize the contributions of this paper as:

- We justify the principled use of classifiers for cGANs by decomposing the joint distribution.
- We propose a cGAN framework, Energy-based Conditional Generative Adversarial Networks (ECGAN), which explains several popular cGAN variants in a unified view.
- We experimentally demonstrate that ECGAN consistently outperforms other state-of-the-art cGANs across different network architectures on benchmark datasets.

The paper is organized as follows. Section 2 derives the unified framework that establishes the role of the classifiers for cGANs. The framework is used to explain ACGAN [36], ProjGAN [34], and ContraGAN [16] in Section 3. Then, we demonstrate the effectiveness of our framework by experiments in Section 4. We discuss related work in Section 5 before concluding in Section 6.

2   Method

Given a K-class dataset $(x, y) \sim p_d$, where $y \in \{1 \ldots K\}$ is the class of x and p_d is the underlying data distribution. Our goal is to train a generator G to generate a sample $G(z, y)$ following $p_d(x|y)$, where z is sampled from a known distribution such as $\mathcal{N}(0, 1)$. To solved the problem, a typical cGAN framework can be formulated by extending an unconditional GAN as:

$$\max_D \min_G \sum_y \mathop{\mathbb{E}}_{p_d(x|y)} D(x, y) - \mathop{\mathbb{E}}_{p(z)} D(G(z, y), y) \tag{1}$$

where G is the generator and D is a discriminator that output higher values for real data. The choice of D leads to different type of GANs [10, 2, 29, 8].

At first glance, there is no classifier in Eq. (1). However, because of the success of leveraging label information via classification, it is hypothesized that a better classifier can improve conditional generation [36]. Motivated by this, in this section, we show how we bridge classifiers to cGANs by Bayes rule and Fenchel duality.

2.1   Bridge Classifiers to Discriminators with Joint Distribution

A classifier, when viewed from a probabilistic perspective, is a function that approximates $p_d(y|x)$, the probability that **x** belongs to class y. On the other hand, a conditional discriminator, telling

whether x is real data in class y, can be viewed as a function approximate $p_d(x|y)$. To connect $p_d(y|x)$ and $p_d(x|y)$, an important observation is through the joint probability:

$$\log p(x, y) = \log p(x|y) + \log p(y) \tag{2}$$
$$= \log p(y|x) + \log p(x). \tag{3}$$

The observation illustrates that we can approximate $\log p(x, y)$ in two directions: one containing $p(x|y)$ for conditional discriminators and one containing $p(y|x)$ for classifiers. The finding reveals that by sharing the parameterization, updating the parameters in one direction may optimize the other implicitly. Therefore, we link the classifier to the conditional discriminator by training both objectives jointly.

2.2 Learning Joint Distribution via Optimization of Conditional Discriminator

Since $p(y)$ is usually known a priori (e.g., uniform) or able to easily estimated (e.g., empirical counting), we focus on learning $p(x|y)$ in Eq.(2). Specifically, since $\log p(x, y) \in \mathbb{R}$, we parameterize it via $f_\theta(x)$, such as a neural network with K real value outputs, where $\exp(f_\theta(x)[y]) \propto p(x, y)$. Similar parameterization is also used in exponential family [44] and energy based model [23]. Therefore, the log-likelihood $\log p(x|y)$ can be modeled as:

$$\log p_\theta(x|y) = \log \left(\frac{\exp\left(f_\theta(x)[y]\right)}{Z_y(\theta)} \right) = f_\theta(x)[y] - \log Z_y(\theta), \tag{4}$$

where $Z_y(\theta) = \int_{x'} \exp\left(f_\theta(x')[y]\right) dx'$.

Optimizing Eq. (4) is challenging because of the intractable partition function $Z_y(\theta)$. Here we introduce the Fenchel duality [44] of the partition function $Z_y(\theta)$:

$$\log Z_y(\theta) = \max_{q_y} \left[\mathop{\mathbb{E}}_{q_y(x)} \left[f_\theta(x)[y] \right] + H(q_y) \right]$$

where q_y is a distribution of x conditioned on y and $H(q_y) = -\mathbb{E}_{x \sim q_y(x)} \left[\log q_y(x) \right]$ is the entropy of q_y. By the Fenchel duality, we can obtain our maximum likelihood estimation in Eq. (4) as:

$$\max_\theta \left[\mathop{\mathbb{E}}_{p_d(x,y)} \left[f_\theta(x)[y] \right] - \max_{q_y} \left[\mathop{\mathbb{E}}_{q_y(x)} \left[f_\theta(x)[y] \right] + H(q_y) \right] \right]. \tag{5}$$

To approximate the solution of q_y, in additional to density models, we can train an auxiliary generator q_ϕ as in cGANs to estimate $\mathbb{E}_{q_y(x)}$ via sampling. That is, we can sample x from q_ϕ by $x = q_\phi(z, y)$, where $z \sim \mathcal{N}(0, 1)$. The objective (5) then becomes:

$$\max_\theta \min_\phi \sum_y \mathop{\mathbb{E}}_{p_d(x|y)} \left[f_\theta(x)[y] \right] - \mathop{\mathbb{E}}_{p(z)} \left[f_\theta(q_\phi(z, y))[y] \right] - H(q_\phi(\cdot, y)), \tag{6}$$

which is almost in the form of Eq (1) except the entropy $H(q_\phi(\cdot, y))$. We leave the discussion about the entropy estimation in Section 2.4. Currently, the loss function to optimize the objective without the entropy can be formulated as:

$$\mathcal{L}_{d_1}(x, z, y; \theta) = f_\theta(x)[y] - f_\theta(q_\phi(z))[y]$$
$$\mathcal{L}_{g_1}(z, y; \phi) = -f_\theta(q_\phi(z, y))[y]$$

2.3 Learning Joint Distribution via Optimization of Unconditional Discriminator and Classifier

Following Eq. (3), we can approximate $\log p(x, y)$ by approximating $\log p(y|x)$ and $\log p(x)$. With our energy function f_θ, $p_\theta(y|x)$ can be formulated as:

$$p_\theta(y|x) = \frac{p_\theta(x, y)}{p_\theta(x)} = \frac{\exp(f_\theta(x)[y])}{\sum_{y'} \exp(f_\theta(x)[y'])},$$

which is equivalent to the y'th output of $\texttt{SOFTMAX}(f_\theta(x))$. Therefore, we can maximize the log-likelihood of $p_\theta(y|x)$ by consider f_θ as a softmax classifier minimizing the cross entropy loss:

$$\mathcal{L}_{\mathrm{clf}}(x, y; \theta) = -\log\left(\texttt{SOFTMAX}\left(f_\theta(x)\right)[y]\right)$$

On the other hand, to maximize the log-likelihood of $p(x)$, we introduce a reparameterization $h_\theta(x) = \log \sum_y \exp(f_\theta(x)[y])$:

$$
\begin{aligned}
\log p_\theta(x) &= \log\left(\sum_y p_\theta(x, y)\right) = \log\left(\sum_y \frac{\exp(f_\theta(x)[y])}{\int_{x'} \sum_{y'} \exp(f_\theta(x')[y'])\,dx'}\right) \\
&= \log\left(\frac{\exp(\log(\sum_y \exp(f_\theta(x)[y])))}{\int_{x'} \exp(\log(\sum_{y'} \exp(f_\theta(x')[y'])))\,dx'}\right) = \log\left(\frac{\exp(h_\theta(x))}{\int_{x'} \exp(h_\theta(x'))\,dx'}\right) \\
&= h_\theta(x) - \log(Z'(\theta)),
\end{aligned}
\tag{7}
$$

where $Z'(\theta) = \int_x \exp(h_\theta(x))\,dx$. Similar to Eq. (5), we can rewrite $\log Z'(\theta)$ by its Fenchel duality:

$$\log Z'(\theta) = \max_q \left[\mathop{\mathbb{E}}_{q(x)}\left[h_\theta(x)\right] + H(q)\right] \tag{8}$$

where q is a distribution of x and $H(q)$ is the entropy of q.

Combining Eq. (7) and Eq. (8) and reusing the generator in Section 2.2, we obtain the optimization problem:

$$\max_\theta \min_\phi \mathop{\mathbb{E}}_{p_d(x,y)}\left[h_\theta(x)\right] - \mathop{\mathbb{E}}_{p(z)}\left[h_\theta(q_\phi(z, y))\right] - H(q_\phi) \tag{9}$$

Similar to Eq. (6), the objective of the unconditional discriminator is equivalent to typical GANs augmented with an entropy term. The loss function without considering the entropy can be formulated as:

$$
\begin{aligned}
\mathcal{L}_{d_2}(x, z, y; \theta) &= h_\theta(x) - h_\theta(q_\phi(z)) \\
\mathcal{L}_{g_2}(z, y; \phi) &= -h_\theta(q_\phi(z, y))
\end{aligned}
$$

2.4 Entropy Approximation in cGANs

In Section 2.2 and Section 2.3, we propose two approaches to train cGANs with and without classification. Unsolved problems in Eq. (6) and Eq. (9) are the entropy terms $H(q_\phi(\cdot, y))$ and $H(q_\phi)$. In previous work, various estimators have been proposed to estimate entropy or its gradient [43, 39, 21, 27]. One can freely choose any approach to estimate the entropy in the proposed framework. In this work, we consider two entropy estimators, and we will show how they connect with existing cGANs.

The first approach is the naive constant approximation. Since entropy is always non-negative, we naturally have the constant zero as a lower bound. Therefore, we can maximize the objective by replacing the entropy term to its lower bound, which is zero in this case. This approach is simple but we will show its effectiveness in Section 4 and how it links our framework to ProjGAN and ContraGAN in Section 3.

The second approach is estimating a variational lower bound. Informally, given a batch of data $\{(x_1, y_1), \ldots, (x_m, y_m)\}$, an encoder function l, and a class embedding function $e(y)$, the negative 2C loss used in ContraGAN [16],

$$\mathcal{L}_C(x_i, y_i; t) = \log\left(\frac{d(l(x_i), e(y_i)) + \sum_{k=1}^m \llbracket y_k = y_i \rrbracket\, d(l(x_i), l(x_k))}{d(l(x_i), e(y_i)) + \sum_{k=1}^m d(l(x_i), (l(x_k))}\right), \tag{10}$$

is an empirical estimate of a proper lower bound of $H(X)$ [37], where $d(a, b) = \exp(a^\top b / t)$ is a distance function with a temperature t. The intuitive behind the 2C loss is pulling the data with the same class closer and pushing the data in difference classes away.

The 2C loss heavily relies on the embeddings $l(x)$ and $e(y)$. Although we only need to estimate the entropy of generated data in Eq. (6) and Eq. (9), we still rely on true data to learn the embeddings in practice. Therefore, the loss function of Eq. (6) can be written as:

$$
\begin{aligned}
\mathcal{L}_{D_1}(x, z, y; \theta) &= \mathcal{L}_{d_1}(x, z, y; \theta) + \lambda_c \mathcal{L}_C^{\mathrm{real}} \\
\mathcal{L}_{G_1}(z, y; \phi) &= \mathcal{L}_{g_1}(x, y; \phi) + \lambda_c \mathcal{L}_C^{\mathrm{fake}},
\end{aligned}
$$

where λ_c is a hyperparameter controlling the weight of the contrastive loss, and $\mathcal{L}_C^{\text{real}}, \mathcal{L}_C^{\text{fake}}$ are the contrastive loss calculated on a batch of real data and generated data respectively.

Similarly, the loss function of Eq. (9) becomes:

$$\mathcal{L}_{D_2}(x, z, y; \theta) = \mathcal{L}_{d_2}(x, z, y; \theta) + \lambda_c \mathcal{L}_C^{\text{real}}$$
$$\mathcal{L}_{G_2}(z, y; \phi) = \mathcal{L}_{g_2}(x, y; \phi) + \lambda_c \mathcal{L}_C^{\text{fake}},$$

The introduction of 2C loss allows us to accommodate ContraGAN into our framework.

2.5 Energy-based Conditional Generative Adversarial Network

Previous work has shown that multitask training benefits representation learning [30] and training discriminative and generative models jointly outperforms their purely generative or purely discriminative counterparts [12, 28]. Therefore, we propose a framework named Energy-based Conditional Generative Adversarial Network (ECGAN) which combining the two approaches in Section 2.2 and Section 2.3 to learn the joint distribution better. The loss function can be summarized as:

$$\mathcal{L}_D(x, z, y; \theta) = \mathcal{L}_{d_1}(x, z, y; \theta) + \alpha \mathcal{L}_{d_2}(x, z, y; \theta) + \lambda_c \mathcal{L}_C^{\text{real}} + \lambda_{\text{clf}} \mathcal{L}_{\text{clf}}(x, y; \theta) \qquad (11)$$
$$\mathcal{L}_G(z, y; \phi) = \mathcal{L}_{g_1}(z, y; \phi) + \alpha \mathcal{L}_{g_2}(z, y; \phi) + \lambda_c \mathcal{L}_C^{\text{fake}} \qquad (12)$$

where α is a weight parameter for the unconditional GAN loss.

Here we discuss the intuition of the mechanisms behind each components in Eq. (11). $\mathcal{L}_{d_1}$ is a loss function for conditional discriminator. It updates the y-th output when given a data pair (x, y). $\mathcal{L}_{d_2}$ guides to an unconditional discriminator. It updates all outputs according to whether x is real. $\mathcal{L}_{\text{clf}}$ learns a classifier. It increase the y-th output and decrease the other outputs for data belong to class y. Finally, $\mathcal{L}_C^{real}$ and $\mathcal{L}_C^{fake}$ play the roles to improve the latent embeddings by pulling the embeddings of data with the same class closer.

Previously, we derive the loss functions $\mathcal{L}_{d_1}$ and $\mathcal{L}_{d_2}$ as the loss in Wasserstein GAN [2]. In practice, we use the hinge loss as proposed in Geometric GAN [26] for better stability and convergence. We use the following combination of $\mathcal{L}_{d_1}$ and $\mathcal{L}_{d_2}$:

$$\text{Hinge}(f_\theta(x_{\text{real}}, y) + \alpha \cdot h_\theta(x_{\text{real}}), f_\theta(x_{\text{fake}}, y) + \alpha \cdot h_\theta(x_{\text{fake}})). \qquad (13)$$

For more discussion of the implementation of hinge loss, please check Appendix A. The overall training procedure of ECGAN is presented in Appendix C.

3 Accommodation to Existing cGANs

In this section, we show that our framework covers several representative cGAN algorithms, including ACGAN [36], ProjGAN [35], and ContraGAN [16]. Through the ECGAN framework, we obtain a unified view of cGANs, which allowing us to fairly compare and understand the pros and cons of existing cGANs. We name the ECGAN counterparts ECGAN-0, ECGAN-C and ECGAN-E, corresponding to ProjGAN, ACGAN, and ContraGAN, respectively. A summary can be found in Table 1.

Table 1: A summary of cGANs and their closest ECGAN counterpart.

Existing cGAN	ECGAN Counterpart	α	λ_{clf}	λ_c
ProjGAN	ECGAN-0	0	0	0
ACGAN	ECGAN-C	0	> 0	0
ContraGAN	ECGAN-E	0	0	> 0

3.1 ProjGAN

ProjGAN [34] is the most representative cGAN architecture that is commonly used in state-of-the-art research [3, 46]. Let the output of the penultimate layer in the discriminator be $g(x)$. The output of ProjGAN's discriminator is:

$$D(x, y) = w_u^T g(x) + b_u + w_y^T h(x) = (w_u + w_y)^T g(x) + b_u \qquad (14)$$

where w_u, b_u are the parameters for the unconditional linear layer, and w_y is the class embedding of y. On the other hand, the output of a discriminator in ECGAN is:

$$D(x, y) = f(x)[y] = (\mathbf{W}^T g(x) + \mathbf{b})[y] = w_y^T g(x) + b_y \tag{15}$$

where $\mathbf{W}, \mathbf{b}$ are the parameters of the linear output layer in f_θ. As shown in Eq. (14) and Eq. (15), the architectures of ProjGAN and ECGAN are almost equivalent. In addition, the loss function of ProjGAN can be formulated as:

$$\mathcal{L}_G = -D(G(z), y)$$
$$\mathcal{L}_D = D(x, y) - D(G(z), y),$$

which is a special case of ECGAN while $\alpha = \lambda_c = \lambda_{\text{clf}} = 0$. We name this case **ECGAN-0**, which is the simplest version of ECGAN. Compared with ProjGAN, ECGAN-0 has additional bias terms for the output of each class.

3.2 ACGAN

ACGAN [36] is the most well-known cGAN algorithm that leverage a classifier to achieve conditional generation. Given a K-class dataset, the discriminator of ACGAN is parameterized by a network with $K + 1$ outputs. The first output, denoted as $D(x)$, is an unconditional discriminator distinguishing between real and fake images. The remaining K outputs, denoted as $C(x)$, is a classifier that predicts logits for every classes. The loss function of ACGAN can be formulated as:

$$\mathcal{L}_G = -D(G(z)) + \lambda_g \mathcal{L}_{\text{clf}}(G(z), y; C)$$
$$\mathcal{L}_D = D(x) - D(G(z)) + \lambda_d (\mathcal{L}_{\text{clf}}(x, y; C) + \mathcal{L}_{\text{clf}}(G(z), y; C))$$

where G is the generator, λ_g and λ_d are hyperparameters to control the weight of cross entropy loss.

The formulation of ACGAN is similar to our ECGAN when $\alpha = \lambda_c = 0$ and $\lambda_{\text{clf}} > 0$. We call the special case as **ECGAN-C**, with a siffix 'C' for classification loss. The main difference between ACGAN and ECGAN-C is that ECGAN-C uses a conditional discriminator which plays the role of a classifier at the same time. Hence the generator in ECGAN-C learns from the conditional discriminator rather than the cross entropy loss which is biased for generative objective.

3.3 ContraGAN

ContraGAN [16] proposed 2C loss, which we mentioned in Eq. (10), to improve ProjGAN by capturing the data-to-data relationship and data-to-label relationship. The 2C loss is applied in both discriminator and generator to achieve conditional generation. That is:

$$\mathcal{L}_G = -D(G(z), y) + \lambda_c \mathcal{L}_C^{\text{fake}}$$
$$\mathcal{L}_D = D(x, y) - D(G(z), y) + \lambda_c \mathcal{L}_C^{\text{real}}$$

The loss functions are the same as ECGAN with $\alpha = \lambda_{\text{clf}} = 0$ and $\lambda_c > 0$. We call it **ECGAN-E**, where 'E' means entropy estimation. The main discrepancy between ContraGAN and ECGAN-E is the output layer of their discriminators. While ContraGAN uses a single-output network, ECGAN uses a K-output network f_θ which has higher capacity.

4 Experiment

4.1 Dataset and Evaluation Metric

We conduct our conditional generation experiments with two dataset: CIFAR-10 [20] as a common benchmark and Tiny ImageNet [22] as a higher resolution and more challenging condition generation task. Both datasets are distributed under the MIT license and do not contain any human-related class hence no personally identifiable information or offensive content in them.

CIFAR-10 [20] is a popular benchmark dataset in image tasks. It contains 50,000 images for training and 10,000 images for testing. Each image contains 32×32 pixels with 3 color channels. The dataset is categorized into 10 different classes.

Table 2: Ablation study of ECGAN on CIFAR-10 and Tiny ImageNet. The label cGAN means the vanilla version of ECGAN where $\alpha = \lambda_{\text{clf}} = \lambda_c = 0$. The label U stands for unconditional gan loss ($\alpha > 0$). C means classification loss ($\lambda_{\text{clf}} > 0$). E means entropy estimation loss via contrastive learning ($\lambda_c > 0$).

Dataset	ECGAN Variant	FID ($\downarrow$)	IS ($\uparrow$)	Intra-FID ($\downarrow$)
CIFAR-10	ECGAN-0	8.049 ± 0.092	9.759 ± 0.061	41.708 ± 0.278
	ECGAN-U	$\mathbf{7.915} \pm 0.095$	9.967 ± 0.078	41.430 ± 0.326
	ECGAN-C	7.996 ± 0.120	9.870 ± 0.157	41.715 ± 0.307
	ECGAN-UC	7.942 ± 0.041	$\mathbf{10.002} \pm 0.120$	41.425 ± 0.221
	ECGAN-UCE	8.039 ± 0.161	9.898 ± 0.064	$\mathbf{41.371} \pm 0.278$
Tiny ImageNet	ECGAN-0	24.077 ± 1.660	16.173 ± 0.671	214.811 ± 3.627
	ECGAN-U	20.876 ± 1.651	15.318 ± 1.148	215.117 ± 7.034
	ECGAN-C	24.853 ± 3.902	16.554 ± 1.500	212.661 ± 8.135
	ECGAN-UC	$\mathbf{18.919} \pm 0.774$	$\mathbf{18.442} \pm 1.036$	$\mathbf{203.373} \pm 5.101$
	ECGAN-UCE	24.728 ± 0.974	17.935 ± 0.619	209.547 ± 1.968

Tiny ImageNet [22] provides 120,000 color images with 200 classes. Each image contains 64×64 pixels. Each class contains 500, 50, 50 images for training, validation, testing, respectively. We use this dataset to demonstrate the effectiveness of ECGAN in a much more challenging conditional generation task with higher resolution images and the scarcity of training data in each class.

In our experiment, we use two common metrics, **Frechet Inception Distance** [FID; 14] and **Inception Score** [IS; 41], to evaluate our generation quality and diversity. Besides, we use **Intra-FID**, which is the average of FID for each class, to evaluate the performance of conditional generation.

4.2 Experimental Setup

We use StudioGAN[1] [16] to conduct our experiments. StudioGAN is a PyTorch-based project distributed under the MIT license that provides implementation and benchmark of several popular GAN architecture and techniques. To provide reliable evaluation, we conduct all experiments with 4 different random seeds and report the means and standard deviations for each metric. We evaluate the model with the lowest FID for each trial. The default architecture is BigGAN [3]. We fix the learning rate for generators and discriminators to 0.0001 and 0.0004, respectively, and tune λ_{clf} in $\{1, 0.1, 0.05, 0.01\}$. We follow the setting $\lambda_c = 1$ in [16] when using 2C loss, and set $\alpha = 1$ when applying unconditional GAN loss. All experiments are run on single GPU (Nvidia Tesla V100) machines. Each process takes about 36 GPU hours. The total amount of computation takes about 14,400 GPU hours. For more detail of the experimental setting, please check Appendix B.

4.3 Ablation Study

We start our empirical studies from investigating the effectiveness of each component in ECGAN. We use symbols 'U' to represent unconditional GAN loss, 'C' to represent classification loss and 'E' to represent entropy estimation loss, which is 2C loss in our implementation. The concatenation of the symbols indicates the combination of losses. For example, ECGAN-UC means ECGAN with both unconditional GAN loss and classification loss ($\alpha > 0$ and $\lambda_{\text{clf}} > 0$). Table 2 shows the results of ECGAN from the simplest ECGAN-0 to the most complicated ECGAN-UCE. On CIFAR-10, ECGAN-0 already achieves decent results. Adding unconditional loss, classification loss or contrastive loss provides slightly better or on-par performance. On the harder Tiny Imagenet, the benefit of unconditional loss and classification loss become more significant. While ECGAN-U already shows advantages to ECGAN-0, adding classification loss to ECGAN-U further improves all metrics considerably. We can also observe that directly adding classification loss is not sufficient to improve cGAN, just the same to the results mentioned in [34]. The fact reveals that the unconditional GAN loss is a crucial component to bridge classifiers and discriminators in cGANs. We also observe that adding contrastive loss doesn't improve ECGAN-UC. An explanation is that the entropy estimation lower bound provided by the contrastive loss is too loose to benefit the training. Furthermore, the additional parameters introduced by 2C loss make the optimization problem more complicated. As

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[1]https://github.com/POSTECH-CVLab/PyTorch-StudioGAN

Table 3: Comparison between cGAN variants with different architectures on CIFAR-10 and Tiny ImageNet

Dataset	Backbone	method	FID ($\downarrow$)	IS ($\uparrow$)	Intra-FID ($\downarrow$)
CIFAR-10	DCGAN	ACGAN	32.507 ± 2.174	7.621 ± 0.088	129.603 ± 1.212
		ProjGAN	21.918 ± 1.580	8.095 ± 0.185	68.164 ± 2.055
		ContraGAN	28.310 ± 1.761	7.637 ± 0.125	153.730 ± 9.965
		ECGAN-UC	**18.035** ± 0.788	**8.487** ± 0.131	**59.343** ± 1.557
	ResGAN	ACGAN	10.073 ± 0.274	9.512 ± 0.050	48.464 ± 0.716
		ProjGAN	10.195 ± 0.203	9.268 ± 0.139	46.598 ± 0.070
		ContraGAN	10.551 ± 0.976	9.087 ± 0.228	138.944 ± 12.582
		ECGAN-UC	**9.244** ± 0.062	**9.651** ± 0.098	**43.876** ± 0.384
	BigGAN	ACGAN	8.615 ± 0.146	9.742 ± 0.041	45.243 ± 0.129
		ProjGAN	8.145 ± 0.156	9.840 ± 0.080	42.110 ± 0.405
		ContraGAN	8.617 ± 0.671	9.679 ± 0.210	114.602 ± 13.261
		ECGAN-UC	**7.942** ± 0.041	**10.002** ± 0.120	**41.425** ± 0.221
Tiny ImageNet	BigGAN	ACGAN	29.528 ± 4.612	12.964 ± 0.770	315.408 ± 1.171
		ProjGAN	28.451 ± 2.242	12.213 ± 0.624	242.332 ± 11.447
		ContraGAN	24.915 ± 1.222	13.445 ± 0.371	257.657 ± 3.246
		ECGAN-UC	**18.780** ± 1.291	**17.475** ± 1.052	**204.830** ± 5.648

a result, we use the combination ECGAN-UC as the default option of ECGAN in the following experiments.

4.4 Comparison with Existing cGANs

We compare ECGAN to several representative cGANs including ACGAN [36], ProjGAN [34], and ContraGAN [16], with three representative network architectures: DCGAN [38], ResNet [13], and BigGAN [3]. Table 3 compares the results of each combinations of cGAN algorithms and network architectures. The results show that ECGAN-UC outperforms other cGANs significantly with all architectures on both CIFAR-10 and Tiny ImageNet. We also noticed that ContraGAN, though achieves decent image quality and diversity, learns a conditional generator which interchanges some classes while generating, hence has low Intra-FID. Overall, the experiment indicates that ECGAN-UC can be a preferred choice for cGAN in general situation.

4.5 Compare Existing cGANs to their ECGAN Counterpart

Table 4 compares ProjGAN, ContraGAN, ACGAN to their ECGAN counterpart. As we described in Section 3, each of these representative cGANs can be viewed as special cases under our ECGAN framework. As mentioned in Section 3, ECGAN-0 has additional bias terms in the output layer compared to ProjGAN. The results in Table 4 shows that the subtle difference still bring significant improvement to the generation quality, especially on the harder Tiny ImageNet.

Compared to ContraGAN, ECGAN-E has the same loss design but different architecture in the discriminator's output layer. While the discriminator of ContraGAN has only single output, ECGAN-E has multiple output for every classes. The difference makes ECGAN-E solve the label mismatching problem of ContraGAN mentioned in Section 4.4 and benefits generation on CIFAR-10, but does not work well on Tiny ImageNet. It is probably because of the scarcity of training data in each class in Tiny ImageNet. Only 50 data are available for updating the parameters corresponding to each class.

Last, we compare ECGAN-C to ACGAN. Both of them optimize a GAN loss and a classification loss. However, ECGAN-C combines the discriminator and the classifier, so the generator can directly optimize cGAN loss rather than the classification loss. As a result, ECGAN-C demonstrates better performance on both CIFAR-10 and Tiny ImageNet. In sum, the comparisons show that through the unified view provided by ECGAN, we can improve the existing methods with minimal modifications.

5 Related Work

The development of cGANs started from feeding label embeddings to the inputs of GANs or the feature vector at some middle layer [33, 7]. To improve the generation quality, ACGAN [36] proposes

Table 4: Compare between representative cGANs and their ECGAN counterparts.

Dataset	method	FID ($\downarrow$)	IS ($\uparrow$)	Intra-FID ($\downarrow$)
CIFAR-10	ProjGAN	8.145 ± 0.156	$\mathbf{9.840} \pm 0.080$	42.110 ± 0.405
	ECGAN-0	$\mathbf{8.049} \pm 0.092$	9.759 ± 0.061	$\mathbf{41.708} \pm 0.278$
	ContraGAN	8.617 ± 0.671	9.679 ± 0.210	114.602 ± 13.261
	ECGAN-E	$\mathbf{8.038} \pm 0.102$	$\mathbf{9.876} \pm 0.036$	$\mathbf{41.155} \pm 0.277$
	ACGAN	8.615 ± 0.146	9.742 ± 0.041	45.243 ± 0.129
	ECGAN-C	$\mathbf{8.102} \pm 0.039$	$\mathbf{9.980} \pm 0.093$	$\mathbf{41.109} \pm 0.273$
Tiny ImageNet	ProjGAN	28.451 ± 2.242	12.213 ± 0.624	242.332 ± 11.447
	ECGAN-0	24.077 ± 1.660	16.173 ± 0.671	214.811 ± 3.627
	ContraGAN	$\mathbf{24.915} \pm 1.222$	$\mathbf{13.445} \pm 0.371$	257.657 ± 3.246
	ECGAN-E	38.270 ± 1.174	12.576 ± 0.405	239.184 ± 2.628
	ACGAN	29.528 ± 4.612	12.964 ± 0.770	315.408 ± 1.171
	ECGAN-C	$\mathbf{24.853} \pm 3.902$	$\mathbf{16.554} \pm 1.500$	$\mathbf{212.661} \pm 8.135$

to leverage classifiers and successfully generates high resolution images. The use of classifiers in GANs can also be found in Triple GAN [24] for semi-supervised learning and Triangle GAN [9] for cross-domain distribution matching. However, Shu [42] and Miyato and Koyama [34] pointed out that the auxiliary classifier in ACGAN misleads the generator to generate images that are easier to be classified. Thus, whether classifiers can help conditional generation still remains questionable.

In this work, we connect cGANs with and without classifiers via an energy model parameterization from the joint probability perspective. [11] use similar ideas but focus on sampling from the trained classifier via Markov Chain Monte Carlo [MCMC; 1]. Our work is also similar to a concurrent work [12], which improve [11] by introducing Fenchel duality to replace computationally-intensive MCMC. They use a variational approach [19] to formulate the objective for tractable entropy estimation. In contrast, we study the GAN perspective and the entropy estimation via contrastive learning. Therefore, the proposed ECGAN can be treated a complements works compared with Grathwohl et al. [11, 12] by studying a GAN perspective. We note that, the studied cGAN approaches also results in better generation quality than its variational alternative [12].

Last, [5] study the connection between exponential family and unconditional GANs. Different from [5], we study the conditional GANs with the focus to provide a unified view of common cGANs and an insight to the role of classifiers in cGANs.

6 Conclusion

In this work, we present a general framework Energy-based Conditional Generative Networks (ECGAN) to train cGANs with classifiers. With the framework, we can explain representative cGANs including ACGAN, ProjGAN, and ContraGAN in a unified view. The experiments demonstrate that ECGAN-UC outperforms state-of-the-art cGANs with different network architectures on CIFAR-10 and Tiny ImageNet. Further investigation can be conduct to find a better entropy approximation or improve cGANs by advanced techniques for classifiers. We hope this work can pave the way to more advanced cGAN algorithms in the future.

7 Limitations and Potential Negative Impacts

There are two main limitations in the current study. One is the scale of the experiments. Ideally experimenting with a larger dataset such as the full ImageNet can further strengthen the contribution. But training with such a large dataset is not affordable for our computational resource, and we can only resort to the conclusive findings in the current benchmark datasets. The other limitation is whether the metrics such as FID truly reflect generation quality, but this limitation is considered an open problem to the community anyway.

As with any work on generative models, there is a potential risk of the proposed model being misused to create malicious contents, much like how misused technology can be used to forge bills. In this sense, more anti-forgery methods will be needed to mitigate the misuse in the future.

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A Implementation Issue of Hinge Loss

In Section 2.2 and Section 2.3, we derive the loss functions $\mathcal{L}_{d_1}$ and $\mathcal{L}_{d_2}$ as the loss in Wasserstein GAN [2]. In practice, we use the hinge loss as proposed in Geometric GAN [26] for better convergence. An intuitive combination of $\mathcal{L}_{d_1}$ and $\mathcal{L}_{d_2}$ can be as following:

$$\text{Hinge}(f_\theta(x_{\text{real}}, y), f_\theta(x_{\text{fake}}, y)) + \alpha \cdot \text{Hinge}(h_\theta(x_{\text{real}}), h_\theta(x_{\text{fake}})), \tag{16}$$

where $\text{Hinge}(\cdot)$ is the hinge loss function proposed in [26].

The property of the hinge loss encourages the output value of $f_\theta(x_{\text{real}}, y), h_\theta(x_{\text{real}})$ to 1, and $f_\theta(x_{\text{fake}}, y), h_\theta(x_{\text{fake}})$ to -1, which leads to better stability in optimization generally. However, since $h_\theta(x) = \log \sum_y \exp(f_\theta(x)[y])$ by definition, we notice that encouraging the output of both functions into the same scale harms the optimization. Therefore, we use the following combination instead:

$$\text{Hinge}(f_\theta(x_{\text{real}}, y) + \alpha \cdot h_\theta(x_{\text{real}}), f_\theta(x_{\text{fake}}, y) + \alpha \cdot h_\theta(x_{\text{fake}})). \tag{17}$$

The new formulation leads to more stable optimization and is less sensitive to the parameter α empirically.

B Experimental Setup Details

We use hinge loss [26] and apply spectral norm [35] on all models to stabilize the training. We adopt self-attention technique [46] and horizontal random flipping [48] to provide better generation quality. We apply moving average update [17, 31, 45] for generators after 1,000 generator updates for CIFAR-10 and 20,000 generator updates for Tiny ImageNet with decay rate 0.9999. We follow the setting of 2C-loss in [16], using $\lambda_c = 1$ and 512-dimension linear projection layer for CIFAR-10 and 768-dimension linear projection layer for Tiny ImageNet. We use Adam [19] optimizer with batch size 64 for CIFAR-10 and batch size 256 for Tiny ImageNet. The training takes 150,000 steps for CIFAR-10 and 100,000 steps for Tiny ImageNet.

C Training Algorithm

Input: Unconditional GAN loss weight: α. 2C loss weight: λ_c. Classification loss weight: λ_{clf}. Parameters of the discriminator and the generator: (θ, ϕ).
Output: (θ, ϕ)

Initialize (θ, ϕ)
for $\{1, \ldots, n_{iter}\}$ **do**
    for $\{1, \ldots, n_{dis}\}$ **do**
        Sample $\{(x_i, y_i)\}_{i=1}^m \sim p_d(x, y)$
        Sample $\{z_i\}_{i=1}^m \sim p(z)$
        Calculate $\mathcal{L}_D$ by Eq. (11)
        $\theta \longleftarrow \text{Adam}(\mathcal{L}_D, lr_d, \beta_1, \beta_2)$
    end for
    Sample $\{(y_i)\}_{i=1}^m \sim p_d(y)$ and $\{z_i\}_{i=1}^m \sim p(z)$
    Calculate $\mathcal{L}_G$ by Eq. (12)
    $\phi \longleftarrow \text{Adam}(\mathcal{L}_G, lr_g, \beta_1, \beta_2)$
end for

D Images Generated by ECGAN-UC

Figure 1: CIFAR-10 images generated by ECGAN (FID: 7.89, Inception Score: 10.06, Intra-FID: 41.42)

Figure 2: Tiny ImageNet images generated by ECGAN (FID: 17.16, Inception Score: 17.77, Intra-FID: 201.66)