# Predictive coding results in perceived illusory contours in a recurrent neural network

## Abstract

Feedforward Convolutional Neural Networks (CNNs) have made great strides in solving computer vision tasks. However, these networks only roughly mimic human visual perception. For example, a recent report [1] shows that such neural networks do not perceive illusory contours (e.g., Kanizsa squares) in the way that humans do. Physiological evidence suggests that the perception of illusory contours could involve feedback connections in the visual cortex, which are lacking in feedforward networks. Would recurrent feedback neural networks perceive illusory contours like humans? In this work we address this issue by equipping a deep feedforward convolutional network with brain-inspired recurrent dynamics implementing a "predictive coding" strategy: at each layer of the hierarchical model, generative feedback "predicts" (or reconstructs) the pattern of activity in the previous layer, and the reconstruction errors are used to iteratively update the network's representations across timesteps. The neural network was first pretrained on the CIFAR100 natural image dataset in an unsupervised way with a reconstruction objective. Then, a classification decision layer was added and the model was finetuned on a form discrimination task: squares vs. randomly oriented inducer shapes (no illusory contour). Finally, the model was tested with the unfamiliar "illusory contour" configuration: inducer shapes oriented to form an illusory square. Compared with the feedforward baseline, the iterative "predictive coding" feedback resulted in more illusory contours being classified as physical squares across timesteps. The illusory contour was measurable in the luminance profile of the image reconstructions produced by the model. In other words, the model was not merely confused by the novel configuration, but behaved as if a shape had truly been presented, similar to the human version of the illusion.

## 1 Architecture

We construct a 3-layered hierarchical stacked autoencoder with 3 feedforward encoding layers $e_n$ ($n \in 1, 2, 3$) and 3 corresponding feedback decoding layers $d_{n-1}$. When considering only the encoding layers, the network can be viewed as a standard feedforward convolutional neural network. To guide the implementation of the feedback connections, we follow the principles of "predictive coding" as introduced by Rao and Ballard [2], a popular framework in neuroscience for characterizing cortical function: in the hierarchical network, the higher layers try to predict the activity of the lower layers and the errors made in this prediction are then utilized to correct their activity. For a given input image, we initiate the activations of all encoding layers with a feedforward pass. Then over successive recurrent iterations (referred to as timesteps $t$) we update both the decoding and encoding

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layer representations using the following equations:

$$d_n(t + 1) = \left[W^b_{n+1,n} e_{n+1}(t)\right]_+$$

$$e_n(t + 1) = \beta_n \left[W^f_{n-1,n} e_{n-1}(t+1)\right]_+ + \lambda_n d_n(t+1) + (1 - \beta_n - \lambda_n)e_n(t) - \alpha_n \frac{\partial \epsilon_{n-1}(t)}{\partial e_n(t)},$$
$$\tag{1}$$

where $W^f_{n-1,n}$ denotes the feedforward weights connecting layer $n - 1$ to layer $n$, and $W^b_{n+1,n}$ denotes the feedback weights from layer $n+1$ to $n$. $\beta_n$, $\lambda_n$ and $\alpha_n$ act as balancing coefficients for the feedforward, feedback and error correction terms respectively and they are treated as hyperparameters of the network (for the present experiments these hyperparameter values were fixed to $\beta = 0.2$, $\lambda = 0.1$ and $\alpha = 0.001$). All the weights are fixed during these iterations, and are optimized over successive batches of natural images (see Methods) to minimize the reconstruction errors–an unsupervised objective in accordance with the principles of the predictive coding theory. $\epsilon_n$ denotes the reconstruction error at layer $n$ and is defined as the mean squared error between the representation at a layer and the prediction made for it at that particular timestep.

Each of the four terms in Equation 1 contributes different signals to a layer: (i) the feedforward term (controlled by parameter $\beta$) provides information about the (constant) input and changing representations in the lower layers, (ii) the feedback term (parameter $\lambda$) conveys information about higher-level representations, as proposed in [3], (iii) the memory term helps to retain the current representation over successive timesteps, and (iv) the error correction term (controlled by parameter $\alpha$) fulfills the objective of predictive coding, i.e., it corrects representations in each layer such that their predictions can better match the preceding layer.

We hypothesize that this architecture, due to its training on natural images containing numerous object contours, and its generative properties that iteratively modify lower-level representations to match higher-level descriptions, could be sensitive to "illusory contours", much like human vision. A similar architecture and its application to robust image recognition on the large-scale ImageNet dataset are described in a companion paper (under review).

## 2  Prior work

Several studies have investigated the perception of illusory contours in deep artificial neural networks. Baker et al [1] tested whether a feedforward deep convolutional network -AlexNet [4]- could interpolate illusory contours between inducing elements in the same way as humans. They employed a so-called classification image technique [5] to give insight into which regions in a given image are important to an observers' perceptual decisions. Applying this technique to human subjects found that the region between inducers is influential in humans' perceptual decisions [5]. However, applying the same technique to a feedforward network showed that it did not appear to represent illusory contours – instead, it relied only on the orientation of inducing elements to make its decisions [1], illustrating a fundamental difference between the visual representations formed by deep networks and humans.

The above-described classification image technique used an external noise probe to infer the network's representation for illusory contours. Kim et al [6] on the other hand directly examined the activations of intermediate layers in feedforward neural networks. They computed the cosine similarity between layers' activations for illusory contours and for physical shapes. Their results suggest illusory contours are closer or more similar to physical contours in the network's representational space than control non-illusory shapes. However, this effect was more pronounced in the network's higher layers, which may be inconsistent with physiological evidence suggesting that the perception of illusory contours originates in early visual cortex [7]. Moreover, the similarity in the layers' activations only indirectly suggests that the network is truly *perceiving* illusory contours.

In addition to feedforward neural networks, Lotter et al [8] investigated a type of recurrent neural network, PredNet [9], which is similar but not identical to the current network. They compared the response properties of single units in PredNet to neuronal recordings in the primate visual cortex and showed similar dynamic responses in the presence of illusory contours. Nevertheless, their research only focused on the neuronal/layer level, and could not directly conclude that the model 'perceived' illusory shapes. Also, it should be noted that Lotter et al trained their network on dynamic stimuli to predict future from past video frames, and consequently tested illusory contours in a dynamic situation—different from the human version of the illusion which can be experienced on static images.

Figure 1: **Finetuning dataset and results.** A. Sample training and testing images for 7 different levels of Gaussian noise: Square, Random, All-out, and All-in. All stimuli varied in luminance (both background luminance and inducer luminance), size (square sidelength or distance between inducers), and position. B. Training results. Left: Average training loss and accuracy results over all noise levels. Right: Same, split by noise level.

## 3  Methods and Results

### 3.1  Training procedure

The network's training included two stages: pretraining and finetuning. The pretraining was conducted in an unsupervised way with a reconstruction objective, wherein both feedforward and feedback weights were optimized over the CIFAR100 natural images dataset. This was done to learn a hierarchy of relevant features to describe each natural image, as well as the corresponding generative pathway to reconstruct images from their features. The finetuning stage was done in a supervised way, with a classification decision layer added to the network to perform a binary form-discrimination task. Specifically, we generated 4 classes of stimuli: Square (physical squares), Random (randomly oriented inducers), All-in (illusory contours, in which the inducers faced each other), and All-out (a control condition, in which all inducers were facing away from each other). These stimuli varied in luminance, size, and position (Figure 1A). In addition, 7 levels of Gaussian noise were added, to render the task non-trivial and avoid overfitting. Notably, during finetuning, the network was only presented with the Square class and the Random class, and trained to discriminate between them. In other words, no illusory contour (All-in) or control (All-out) images were presented in this phase. The weights of the whole network were finetuned for 20 epochs (where for each image, 10 predictive coding timesteps were used), after which it was tested with a distinct validation set. The accuracy on the validation set was around 0.975, with higher values for lower Gaussian noise level (Figure 1B).

### 3.2  Illusory contour perception

After pre-training on natural images and fine-tuning on simple shapes, the network could discriminate between physical squares and randomly oriented inducers in any configuration (except the two critical configurations, All-in and All-out, which had not been seen during training). During testing, all four classes were presented to the network, with All-out (control class) and All-in (illusory contours) as novel stimulus configurations formed by familiar inducers. Our hypothesis was that the All-in configuration would be classified as a square in a number of trials (illusory contour perception), whereas the All-out configuration would be more likely to be classified as random inducers.

Figure 2: Classification results. A. Feedforward network classification output (timestep 0) for different noise levels ($\sigma$) B. Change in the probability of "square" report as a function of the number of recurrent predictive coding iterations (timesteps) compared to timestep 0. Each panel corresponds to a different noise level. Feedback iterations increase the likelihood of a "square" report, especially for the All-in condition (and especially at higher noise levels).

For each class, we thus measured the probability of the image being classified as a square. Figure 2A shows the classification results at timestep 0, corresponding to the output of a standard feedforward convolutional network. Since the Square class reached nearly 100% of correct classification, here we only compare the results for the remaining three classes. Surprisingly, immediately after the feedforward pass the network was more likely to classify the All-out control condition as a square than the All-in or random inducer conditions. This bias, which was present independent of noise level (Figure 3A), may be explained by low-level similarity between the All-out and Square classes, at the pixel level. However, taking into account this initial bias, the probability assigned to the All-in illusory contour condition grew much more rapidly over successive timesteps; this effect became even more pronounced as the noise level increased (Figure 2B). After 50 timesteps for the highest levels of noise ($\sigma > 0.15$), the likelihood of reporting a square (an "illusory contour perception") had increased by more than 10% for the All-in condition, but less than 3-4% for the All-out control condition.

Although the network classified more illusory contours as squares, it remains hard to draw the conclusion that the network could really "see" illusory contours. An advantage of the predictive coding framework is that we can inspect the reconstructions at each layer. Thus, we examined the image reconstructions produced by the model. Figure 3B displays two examples of reconstructed images at timestep 100. Compared with the original images (top row) whose noise standard deviation is 0.2, the reconstructed images are denoised by the network, and the illusory contour shapes are even clearer. To quantify the illusion "perceived" by the network, we inspected the luminance profile of the reconstructions: for each image we computed a "Figure-ground luminance difference" (FG). Given the expected position of the illusory contour (the position that the square would have occupied if it had been real instead of illusory), along each of the four cardinal axes we took two pixels inside (red in Figure 3A) and two pixels outside the square (green in Figure 3A). We computed the average difference between the pixel luminance values inside and outside. A polarity factor

Figure 3: Quantification of illusory countour perception in the neural network. A. Computation of the "FG" value measuring the figure-ground luminance difference. B. Two examples of illusory contour (All-in) stimuli, and their corresponding reconstructions from the network at timestep 100. C. The FG-luminance difference for classes Random, All-out, and All-in over 100 timesteps (zero is absence of illusion, larger values mean more illusion is perceived).

(-1 or 1) multiplied this measure, to take into account the different configurations: dark inducers (polarity=1) are expected to produce lighter illusory shapes, light inducers (polarity=-1) to produce darker ones. The constructed FG measure is zero in the original All-in images (since it is measured in the background between the inducers), but should be positive in the image reconstructions whenever an illusory contour is perceived. Figure 3C shows how this FG value changes over predictive coding iterations, for illusory contours (All-in class) and the other two non-illusory shapes (All-out and Random classes). For the All-in class, after 10 time steps the value is consistently higher than zero, and 5 to 10 times higher than the FG value measured for the control (All-out) or the random inducer classes. For comparison, the FG value for the physical square would range from 0.3 to 0.6 (not shown here). Remarkably, these results are consistent with physiological evidence showing that neural responses for illusory contours in monkey V1 are higher than similar non-illusory images, but lower than physical squares [7].

## 4 Discussion

The purpose of this study was to test whether a recurrent feedback neural network could perceive illusory contours (Kanizsa squares) in a similar manner to humans. We augmented a feedforward CNN with predictive coding recurrent dynamics so that, unlike other related work [8, 1, 6], we were able to (i) analyse explicit classification decisions (square vs. inducers) and (ii) visualize reconstructed inputs from the model's viewpoint. We found that, compared to a feedforward baseline, the recurrent dynamics led the network to perceive more and more illusory contours. Further, by inspecting the network's reconstructions, we found evidence of modulations of the perceived luminance profiles in the expected direction for illusory shapes, suggesting that the network was truly "perceiving" the contours. In summary, we provide evidence that brain-inspired recurrent dynamics can lead networks to perceive illusory contours like humans.

## Broader Impact

This work is at the intersection of machine learning and computational neuroscience, and we leverage each field to better understand the other. Fostering further integration and collaboration between the two has the potential to advance both significantly. In this work we primarily contribute to the ongoing goal of better understanding biological neural systems, which has wide-ranging potential societal benefits including potential improvements in medical care. The risk of this aspect of the work having harmful consequences seems relatively low.

We also demonstrate that taking inspiration from the brain can help develop artificial intelligence systems which share similarities with human perception, potentially contributing to the development of systems which better mirror human behavior. Given the rapidly progressing integration of machine learning systems into many everyday tools and the ongoing discussions surrounding transparency, accountability, and explainability, the possible positive outcomes include helping us better understand the tools being deployed. On the other hand, although this work is demonstrating a relatively low-level effect (the perception of visual illusion), in general this approach may carry risks that include enabling malicious groups to impersonate humans with AI.

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