Equivalent Linear Mappings of Large Language Models

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Abstract

Despite significant progress in transformer interpretability, an understanding of the computational mechanisms of large language models (LLMs) remains a fundamental challenge. We demonstrate that LLM inference for a given input sequence can be mapped to an equivalent and interpretable linear system that reconstructs the predicted output embedding, where the token probabilities computed from the linear reconstruction achieve relative error below 10^{-14} at double floating-point precision. Extending techniques from image diffusion models that exhibit local or piecewise linearity, we strategically detach components of the gradient computation with respect to an input sequence for a next-token prediction such that this "detached" Jacobian of the model reconstructs the output with one linear operation per input token. We demonstrate this approach across models, including Qwen 3, Gemma 3 and Llama 3, up to Qwen 3 14B. These linear representations of models for particular input token sequences reveal that LLMs operate in extremely low-dimensional subspaces where the singular vectors can be decoded to interpretable semantic concepts. We examine how the linear representations of individual layers as well as their attention and multilayer perceptron modules build predictions, and use these as steering operators to insert semantic concepts into unrelated text. Despite their expressive power and global nonlinearity, modern LLMs can be interpreted through equivalent linear representations that reveal interpretable semantic structures in the next-token prediction process.

1 Introduction

The transformer decoder has become the architecture of choice for large language models (Vaswani et al., 2017) and efforts toward a conceptual understanding of its mechanisms are ongoing. Significant insights include sparse autoencoders for conceptual activations in LLMs (Bricken et al., 2023), "white-box" alternative architectures (Yu et al., 2023), minimally sufficient architectures (He & Hofmann, 2023) and analytic results on generalization (Cowsik et al., 2024). While transformers are complex globally nonlinear functions of their input, we demonstrate how to compute an equivalent linear system that reconstructs the predicted output embedding for a given input sequence up to double floating-point precision.

Our approach builds on two previous results: Elhage et al. (2021) found that attention-only networks with basic language generation abilities transfer semantic information across the network with interpretable circuits, including the "induction head", and Kadkhodaie et al. (2023) showed that powerful image denoising diffusion models with several architectural constraints are piecewise linear functions and interpreted as low-dimensional adaptive linear filters.

We extend these ideas by demonstrating equivalent linear systems for modern LLMs with gated linear activations. For many open-weight LLMs, the gradient operation with respect to the input can be manipulated at inference such that the output prediction is unchanged but has a linear equivalent. This numerical Jacobian computation captures the complete forward operation of the model, including activation functions and attention modules, although it is only valid for that particular input sequence (not piecewise linear but "pointwise" linear).

This approach allows us to analyze entire models, from input embeddings to predicted output embedding, as an equivalent linear system for a particular input sequence. By examining the singular value decomposition

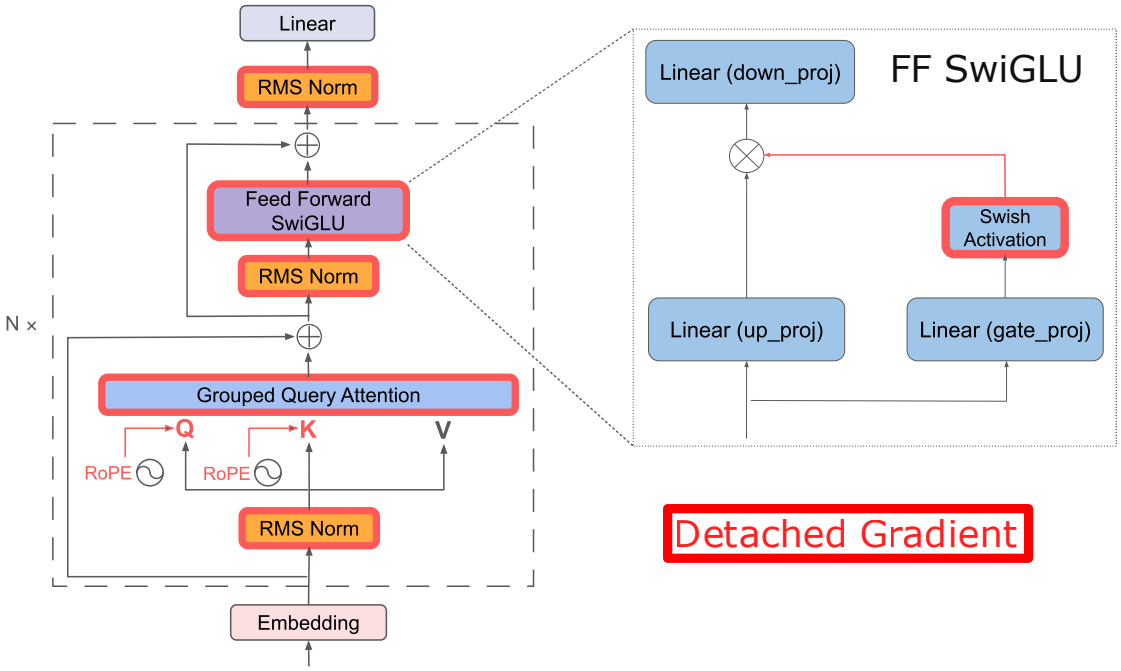

Figure 1: A schematic of the Llama 3 transformer decoder (Grattafiori et al., 2024; Nvidia, 2024). The PyTorch gradient detach operations for components outlined in red effectively freeze the nonlinear activations for a given input sequence, creating a linear path for the gradient with respect to the input embedding vectors, but do not change the output. The output embedding prediction can be mapped to an equivalent linear system by the Jacobian autograd operation. The feedforward module with a SwiGLU activation function is shown in expanded form to demonstrate how the nonlinear Swish term can be detached from the gradient to form a linear path, achieving linearity for a given input. The RMSNorm layers and and softmax attention blocks also must be detached from the gradient.

(SVD) of the equivalent linear system, we can measure the local dimensionality of the learned manifolds involved in next-token prediction and can decode the singular vectors into output tokens. This analysis can also be done layer by layer, or for individual attention and multilayer perceptron (MLP) modules, in order to observe how these models compose next-token predictions.

We demonstrate equivalent linearity in model families including Qwen 3, Gemma 3, Llama 3, at a range of sizes up to Qwen 3 14B. This approach does not require additional model training, offering a new path to interpreting a wide range of open-weight LLMs for specific inputs that could serve as a complement to other powerful interpretability methods.

2 Method

2.1 The Jacobian of a deep ReLU Network

Mohan et al. (2019) observed that deep *ReLU* networks for image denoising which utilize zero-bias linear layers are "adaptive linear" functions due to their homogeneity of order 1 at a given fixed input, which enables interpretation as an exactly equivalent linear system. Given the homogeneity at a fixed input, the network's output can be reproduced by numerically computing the Jacobian matrix of the network at a particular input image $\mathbf{x}^*_{\mathbf{im}}$ and multiplying it by $\mathbf{x}^*_{\mathbf{im}}$.

$$\mathbf{y}^*_{\mathbf{im}} = \mathbf{J}(\mathbf{x}^*_{\mathbf{im}}) \cdot \mathbf{x}^*_{\mathbf{im}} \tag{1}$$

Due to the global nonlinearity of the network, the Jacobian must usually be computed again at every input of interest. The Jacobian may be the same for similar inputs in the same piecewise region of the

response (Balestriero & Baraniuk, 2021) (but this will be demonstrated to not be the case for transformer architectures).

2.2 The Jacobian of a transformer decoder

Many open weight LLMs also use linear layers with zero bias, as required for linearity in the architecture of Mohan et al. (2019). A transformer decoder predicts an output token embedding $\mathbf{y}$ given a sequence of k input tokens $\mathbf{t} = (\mathbf{t_0}, \mathbf{t_1}..., \mathbf{t_k})$ mapped to input embedding vectors $\mathbf{x} = (\mathbf{x_0}, \mathbf{x_1}..., \mathbf{x_k})$, where $\mathbf{t}^*$ and $\mathbf{x}^*$ represent a particular sequence. The output embedding prediction is a nonlinear function of the input embedding vectors $\mathbf{x_0}, \mathbf{x_1}$,...$\mathbf{x_k}$, as LLMs utilize nonlinear gated activation functions for layer outputs (SwiGLU for Llama 3, GELU for Gemma 3 and Swish for Qwen 3) as well as normalization and softmax attention blocks.

Gated activations like $Swish(\mathbf{x}) = \mathbf{x} \cdot sigmoid(\mathbf{x})$, with a linear term and a nonlinear term, are also an "adaptive" linear function or, more generally, an adaptive homogeneous function of order 1 (Mohan et al., 2019). If the $sigmoid(\mathbf{x})$ term that gives rise to the nonlinearity is frozen for a specific numerical input, e.g. an embedding vector $\mathbf{x_0^*}$ (Elhage et al., 2021) (or equivalently detached from the computational graph with respect to the input), then we have a linear function valid only at $\mathbf{x_0^*}$ where (1) holds and we can numerically compute a Jacobian matrix that carries out $Swish(\mathbf{x_0^*})$ as a linear operation.

Below we show that computing the Jacobian after effectively substituting specific values for the nonlinear terms also works for other gated activation functions, normalization layers and softmax attention blocks. We further demonstrate that for a given input sequence we can apply necessary gradient detachments so that the entire transformer decoder is an adaptive homogeneous function of order 1, and numerically compute the equivalent linear system that reproduces the transformer output embedding $\mathbf{y}^*$.

The Jacobian $\mathbf{J}(\mathbf{x})$ of a transformer is the set of matrices generated by taking the partial derivative of the decoder inference function $\mathbf{y}(\mathbf{x}) = f(\mathbf{x_0}, \mathbf{x_1}..., \mathbf{x_k})$, with respect to each element of each $\mathbf{x_i}$ (where $\mathbf{x_i}$ for Llama 3.2 3B has length 3072, for example, and therefore the Jacobian matrix for each embedding vector is a square matrix of this size). If a transformer decoder were naturally a homogeneous function of order 1, this Jacobian would produce an exact reconstruction of the output.

However, this is not the case. In order to numerically compute an equivalent linear representation, we introduce a "detached" Jacobian $\mathbf{J}^+$, which is a set of matrices that captures the full nonlinear forward computation for a particular input sequence $\mathbf{x}^*$ as a linear system. The detached Jacobian is the numerical Jacobian of the LLM forward operation when its gradient includes a specific set of $detach()$ operations for the nonlinear terms in the normalization, activation and attention operations that force the function to be "adaptively" homogeneous of order 1. Fig. A1 shows how each matrix of the detached Jacobian operates on its corresponding input embedding vector to provide a reconstruction of the LLM forward operation (validated by the PyTorch allclose function for absolute and relative tolerances of 10^{-14}), see Fig. 2).

$$\mathbf{y}^* = \sum_{i=0}^{k} \mathbf{J_i^+}(\mathbf{x}^*) \cdot \mathbf{x_i^*} \tag{2}$$

The conventional Jacobian $\mathbf{J}$ for a particular input sequence $\mathbf{x}^*$ (as in Mohan et al. (2019)) does not generate an accurate reconstruction the nonlinear LLM forward operation since the transformer function is not homogeneous of order 1. The detached Jacobian $\mathbf{J}^+$ evaluated at $\mathbf{x}^*$ is the result of an alternative gradient path through the same network which is homogeneous with resepct to the input $\mathbf{x}^*$. The detached Jacobian $\mathbf{J}^+$ only generates an accurate reconstruction at $\mathbf{x}^*$ and not in the local neighborhood due to the strong nonlinearity of the decoder inference function. The detached Jacobian matrices differ for every input sequence and must be computed numerically for every sequence.

2.3 Nonlinear layers as linear operators for a given input

In order to achieve linearity, modifications must be made to the gradient computations of the RMSNorm operation, the activation function (SwiGLU in Llama 3.2) and the softmax term in the attention block output.

2.3.1 Normalization

Normalization layers like LayerNorm (Xu et al., 2019) or RMSNorm (Zhang & Sennrich, 2019) with zero bias are nonlinear with respect to their input because they include division by the square root of the variance of the input.

$$norm(\mathbf{x}) = \frac{\mathbf{x}}{\sqrt{var(\mathbf{x})}} \tag{3}$$

Mohan et al. (2019) devised a novel bias-free batch-norm layer which detaches the variance term from the network's computational graph (see their code implementation). Their batch-norm layer returns the same values as the standard batch-norm layer, but it is linear at inference as the nonlinear operation is removed from the gradient computation. This is also similar to the "freezing" of nonlinear terms in attention-only transformers from Elhage et al. (2021).

We make a similar change for Llama 3.2 3B by altering how the gradient with respect to the input is computed at inference for RMSNorm. This is accomplished by substituting the value for the input vector $\mathbf{x}^*$ for only the variance term as in (4). In PyTorch, this is accomplished by cloning and detaching the $\mathbf{x}$ tensor within the variance operation, so its value will be treated as a constant. The gradient operation is still tracked for $\mathbf{x}$ in the numerator, so that term will be treated as a variable by the PyTorch autograd function for computing the Jacobian. The gradient of the function is then computed at $\mathbf{x}^*$ (we assume for simplicity an input sequence of length 1).

$$norm(\mathbf{x}) = \frac{\mathbf{x}}{\sqrt{var(\mathbf{x}^*)}} \tag{4}$$

We define the detached Jacobian as follows:

$$\mathbf{J}_{\mathbf{n}}^{+} = [\frac{\partial}{\partial \mathbf{x}} norm(\mathbf{x})]|_{\mathbf{x}=\mathbf{x}^*} \tag{5}$$

We can rewrite the pointwise linear RMSNorm as follows:

$$norm(\mathbf{x}^*) = \mathbf{J}_{\mathbf{n}}^{+}(\mathbf{x}^*) \cdot \mathbf{x}^* \tag{6}$$

At inference for a given input, we now have a linear RMSNorm whose output is numerically identical to the one used in training. However, when we take the gradient with respect to the input vector $\mathbf{x}$ in *eval* mode, the numerical output is the detached Jacobian matrix $\mathbf{J}_{\mathbf{n}}^{+}$, which we can use to reconstruct the normalization output as a linear system.

The goal is to apply this same approach for other nonlinear functions in the decoder such that the entire computation from the input embedding vectors to the predicted output is linear for a given input, and we can compute and interpret the set of detached Jacobian matrices.

2.3.2 Activation functions

While Mohan et al. (2019) relied on *ReLU* activation functions, which do not require any changes to achieve linearity, Llama 3.2 3B uses SwiGLU (Shazeer, 2020), Gemma 3 uses approximate GELU (Hendrycks & Gimpel, 2016) and Qwen 3 uses Swish for activation functions. There is a linear $\mathbf{x}$ term in each of these, and the gradients can be cloned and detached from the nonlinear terms. This manipulation produces a pointwise linear Swish layer with respect to the input $\mathbf{x}$.

$$\text{Swish}\,(\mathbf{x}) = \mathbf{x} \cdot \text{sigmoid}(\mathbf{x}) \tag{7}$$

$$\text{Swish}\,(\mathbf{x}^*) = \mathbf{x} \cdot \text{sigmoid}(\mathbf{x})|_{\mathbf{x}=\mathbf{x}^*} \tag{8}$$

$$\text{Swish}\,(\mathbf{x}^*) = ([\frac{\partial}{\partial \mathbf{x}}\text{Swish}(\mathbf{x})]|_{\mathbf{x}=\mathbf{x}^*}) \cdot \mathbf{x}^* \tag{9}$$

$$\text{Swish}\,(\mathbf{x}^*) = \mathbf{J}^+_{\mathbf{Swish}}(\mathbf{x}^*) \cdot \mathbf{x}^* \tag{10}$$

Detaching the gradient from the Swish output thus allows for a pointwise linear form of Swish at inference. A similar procedure may be carried out for SwiGLU with Llama 3 and GELU with Gemma 3 (see supplement, eq. 17).

2.3.3 Attention

The softmax operation at the output of the attention block can also be detached, with the linear relationship preserved through the subsequent multiplication with $\mathbf{V}$, which is a linear function of $\mathbf{x}$. Below, $\mathbf{Q} = \mathbf{W_Q x}$, $\mathbf{K} = \mathbf{W_K x}$ and $\mathbf{V} = \mathbf{W_V x}$.

$$Attn(\mathbf{Q}, \mathbf{K}, \mathbf{V}) = softmax(\frac{\mathbf{Q}\mathbf{K}^T}{\sqrt{d_k}}) \cdot \mathbf{V} \tag{11}$$

$$Attn(\mathbf{x}) = [softmax(\frac{\mathbf{Q}\mathbf{K}^T}{\sqrt{d_k}})|_{\mathbf{Q}=\mathbf{Q}^*,\mathbf{K}=\mathbf{K}^*}] \cdot \mathbf{W_V x} \tag{12}$$

$$Attn(\mathbf{x}^*) = ([\frac{\partial}{\partial \mathbf{x}}Attn(x)]|_{\mathbf{x}=\mathbf{x}^*}) \cdot \mathbf{x}^* \tag{13}$$

$$Attn(\mathbf{x}^*) = \mathbf{J}^+_{\mathbf{Attn}}(\mathbf{x}^*) \cdot \mathbf{x}^* \tag{14}$$

The linear $\mathbf{x}$ term within $\mathbf{V}$ makes it possible for the attention block to be pointwise linear at inference, as the gradient for the softmax output is detached.

2.3.4 The Transformer Decoder

With the the above gradient detachments for the normalization layers, activation functions and attention blocks, the transformer decoder network is linear with respect to $\mathbf{x}^*$ when evaluated at $\mathbf{x}^*$ (shown here for length k).

$$\mathbf{y}^* = \sum_{i=0}^{k} \mathbf{J}^+_{\mathbf{i}}(\mathbf{x}^*) \cdot \mathbf{x}^*_{\mathbf{i}} \tag{15}$$

The output of the network incorporating the above gradient detachments is unchanged from the original architecture but has an equivalent linear representation.

3 Results

3.1 Pointwise linearity of the predicted output

In order to validate whether the detached Jacobian achieves reconstruction with a linear representation, we can compare the predicted output embedding vector for a given input token sequence to the reconstruction of the output. As a baseline, we can also compute the reconstruction using the conventional Jacobian as in Mohan et al. (2019) and examine its accuracy. Given the above argument that the appropriate gradient detachments are necessary to achieve output reconstruction, we expect the detached Jacobian to accomplish reconstruction, but the conventional Jacobian to fail.

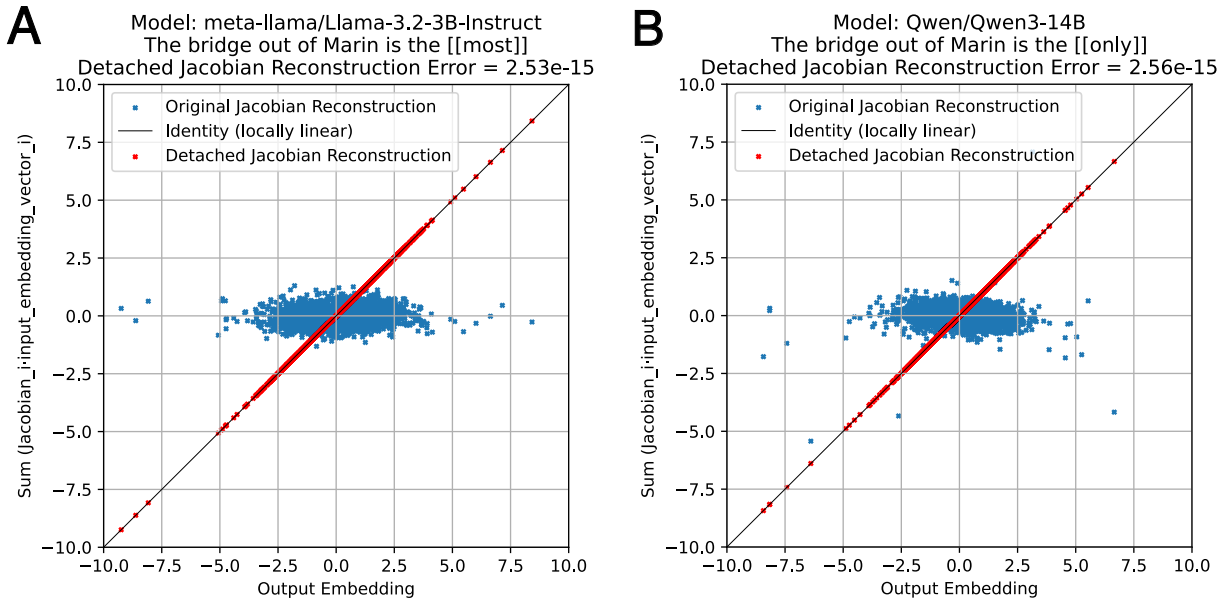

Figure 2: For the input sequence "The bridge out of Marin is the", the elements of the predicted output embedding vector of the model compared to the elements from the Jacobian reconstruction for both the original Jacobian (blue points) and detached Jacobian operations (red points), shown for A) Llama 3.2 3B and B) Qwen 3 14B. Note that the detached Jacobian reconstructions match the predicted embedding, with relative error (the norm of the reconstruction error divided by the norm of the output embedding) on the order 10^{-14} for $float64$ precision.

Fig. 2 compares the network output to both the conventional and detached Jacobian reconstructions for Llama 3.2 3B and Qwen 3 14B. The reconstruction of the output embedding with the detached Jacobian matrices falls on the identity line when compared with the output embedding, showing accurate reconstruction, while the reconstruction with the conventional Jacobian is not at all close to the output. This comparison therefore demonstrates the validity of the reconstruction with the linear system of the detached Jacobian for Qwen 3 14B for a particular input.

In order to examine the fidelity of the detached Jacobian reconstruction, we compared the reconstruction against the network output using PyTorch function allclose with varying tolerance levels. The reconstructions achieved numerical agreement within a relative and absolute tolerance of 10^{-14}. This tolerance is approximately 50 times the machine epsilon of $2.2 \cdot 10^{-16}$ for 64-bit floating-point numbers, indicating high-fidelity reconstruction that is numerically equivalent to the reference implementation for practical purposes. As an additional metric, the norm of the detached Jacobian reconstruction error divided by the norm out of the output is also on the order of 10^{-14}.

The numerical computation of the full detached Jacobian matrix takes on the order of 10 seconds for an input sequence of 8 tokens for Llama 3.2 3B on a GPU with 16 GB VRAM. In contrast, the full Jacobian matrix for the same sequence at float64 precision with Qwen 3 14B on a GPU with 40 GB VRAM takes 20 seconds. A method for computing the top k singular vectors of the detached Jacobian without forming the full matrix utilizing Lanczos iteration has also been implemented in Jax for Gemma 3 4B, allowing for the efficient computation of the top singular vectors of the detached Jacobian for up to 400 input tokens on a GPU with 40 GB VRAM.

3.2 Single-unit feature selectivity and invariance

Since the detached Jacobian applied to the input embedding reproduces the predicted output embedding vector, and the elements of the predicted output embedding vector are the units of the last transformer

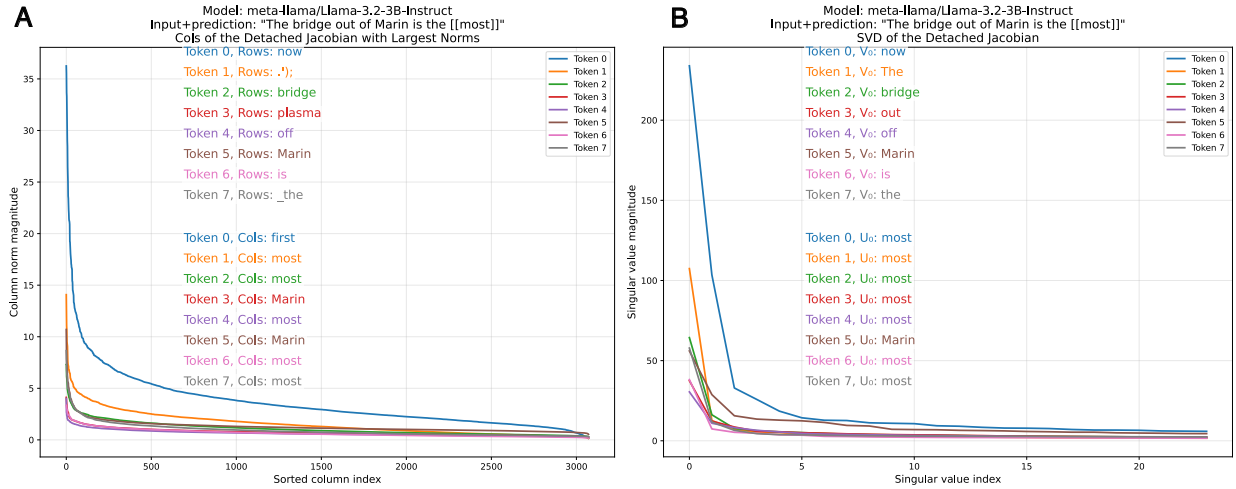

Figure 3: Given the sequence "The bridge out of Marin is the", the most likely prediction is "most" for Llama 3.2 3B. The detached Jacobian matrices for each token represent an equivalent linear system that computes the predicted output embedding. A) We show the features which drive large responses in single units in the last decoder layer, which are the rows of the detached Jacobian with the largest norm values, and decode each of those into the most likely input embedding token. The block of words at the top shows the ordered decoded "feature" input tokens from the largest rows of the detached Jacobian matrix for the input tokens. A similar operation is carried out for columns of the largest norm values, which are decoded to the output token space. Note that the activation distribution of column magnitudes is fairly sparse, with only a few units driving the response. B) We take the singular value decomposition of the detached Jacobian matrix corresponding to each input token, which summarizes the modes driving the response, and decode the right and left singular vectors V and U to input and output embeddings, shown in colors. The singular value spectrum is extremely low rank, and decoding the U singular vectors returns candidate output token, including "most" and "first". Decoding the V singular vectors returns variants of the input tokens like "bridge", "Marin" and "is", as well as others that are not clearly related to the input sequence.

layer, the rows of the detached Jacobian matrices represent the input features to which the last layer units are selective and invariant for that particular input sequence (Kadkhodaie et al., 2023; Mohan et al., 2019).

The activation of a particular unit in the last layer is determined by the inner product of a row of the detached Jacobian and the input embedding vector. We can sort by the magnitude of row norms, then map the largest-magnitude rows of the detached Jacobian back to the input embedding space (by finding the nearest-neighbor embedding vectors from the tokenizer) to determine the tokens that cause each unit to be strongly positive or negative. We can see in Fig. 3A that the units respond strongly to the words of the prompt, including "bridge", "Marin" and "is". Decoding of the rows of the detached Jacobian for each token as well as the distribution of activations for this sequence is shown in Fig. 3A.

The columns of the Jacobian can also be decoded to the output token space, and these turn out to be tokens that could be predicted, which include words like "most" or "first", which could be acceptable outputs.

3.3 Singular vectors of the detached Jacobian

An alternative approach is to look at the singular value decomposition of the detached Jacobian $\mathbf{J_i^+} = \mathbf{U\Sigma V^T}$, following Mohan et al. (2019). Since the detached Jacobian represents the forward computation, and there are no higher order terms, the fact that the SVD is very low rank shows the entire forward computation can be approximated with only a few singular vectors operating on the input embeddings.

In Fig. 3B, the singular vectors are decoded for Llama 3.2 3B (and for other models in supplemental Fig. A2). The right singular vectors V are decoded to input tokens in the same way the rows of the detached

Jacobian were above, and we see similar decoding of the top tokens to the features driving the most active single units. The left singular vectors U can be decoded to output embedding tokens, and "most" is the strongest, as it was in the columns of the detached Jacobian matrices.

	Input token 0	Input token 1	Input token 2	
Layer 23_0	salopes CONSTANTS getch Uncomment massage TRY	metaphor bridge largest easiest only first centerpiece	first hardest unc fastest highway bottleneck	
Layer 23_1	metaphor unc Derne makeshift OBJC	bridge Bridge . bridge bridge	scenes WithError opi Timing presets Entering	
Layer 23_2	ros lovers flutter	antics jams	weblog COMPONENT annot metaphor	
Layer 24_0	first third last most largest fourth culmination	metaphor largest centerpiece easiest first hardest bridge gateway	hardest first easiest fastest most ones same	
Layer 24_1	metaphor makeshift .wp REAK	brid bridge bridges bridge Bridge	scenes LocalStorage WithError	
Layer 24_2	flutter ros Lingu	phenomena puzz annot metaphor		
Layer 25_0	largest most first longest latest fastest last third	bridge bridges Bridge gateway	hardest ones exit easiest first most fastest highway	
Layer 25_1	bridge bridges Bridge Bridges brid	bridges bridge Bridge bridge Bridge	(exit exit exits eternity . exit	
Layer 25_2	bridges bridge Bridge bridge parliament	Exit exit jams	INCIDENT symbolism	
Layer 26_0	first most largest last longest latest gateway only	bridge bridges metaphor gateway connecting	highway first exit ones last hardest roads	
Layer 26_1	bridge bridges metaphor Bridges Bridge	bridges bridge structures brid bridge	.charset jams Margins	
Layer 26_2	parliament structures bridges Parliament bridge	Exit exit choke Exit panicked	symbolism metaphor	
Layer 27_0	first last largest bridge longest most oldest latest	bridge bridges Bridge Bridges	last first exit highway bottleneck next road choke	
Layer 27_1	bridge bridges Bridge Bridges	bridges bridge Bridge bridge brid Bridge	EXIT exit exits (exit	
Layer 27_2	bridge bridge bridges Bridge structures	Exit exit Exit	exit . exit incident EXTRA incidents	
Layer 28_0	bridge longest largest first busiest last oldest most	bridge bridges Bridge Bridge	highway exit bottleneck highways Highway last road exits	
Layer 28_1	bridge bridges Bridge Bridge	highway highways coast freeway roads road route	exit exits EXIT exit Exit	
Layer 28_2	bridge bridge bridges Bridge brid	Exit exit Exit exit exit	exit Saddam Mosul Kuwait incident metaphor	
Layer 29_0	bridge only fourth last third longest fifth most	bridge bridges Bridge Bridges	only last first highway third highways exit fourth	
Layer 29_1	bridge bridges Bridge Bridges	coast highway road driveway coastline roads highways freeway	exits exit EXIT	
Layer 29_2	bridge bridges bridge structures brid structure	Exit exit Highway Exit	Saddam Mosul Elvis metaphor incident	
Layer 30_0	bridge most longest fourth third last only fifth	bridge bridges Bridge Bridge	highway only bridge last first Highway road highways	
Layer 30_1	bridge bridges Bridges Bridge	coast freeway highway coastline road roads highways	bridge Bridge bridges bridge brid	
Layer 30_2	bridge structure structures bridges bridge brid	sail seab sailing Bermuda ship	Memphis Kuwait Jordan Saddam Iowa	
Layer 31_0	bridge most only last longest first third largest	bridge bridges Bridge Bridge	only last highway first bridge exit Highway most	
Layer 31_1	coast airlines Interior airline interior Lua Speedway	coast coastline coastal Coast Coastal route	bridge Bridge bridges bridge underwater brid	
Layer 31_2	bridge bridges bridge brid Bridge structure	ship sail sailing dock seab	Jordan Memphis Kuwait Mississippi	
Layer 32_0	bridge most only first last longest third largest	bridge Bridge bridges Bridge bridge	only last first highway most main route exit	
Layer 32_1	interior airline steam airlines Trail breed vacuum	coast coastal coastline route Coast Route beach	bridge span underwater connecting deck public member	
Layer 32_2	bridge bridge bridges Bridge brid Bridge	ship sail dock sailing seab	Kuwait Jordan Memphis Edmonton Mississippi Nile	
Layer 33_0	only first last most third main second subject	bridge Bridge bridges Bridge only	only last first key main same most exit	
Layer 33_1	planet interior cabin floors roots	coast coastline coastal Coast route beach Coastal	span public member library platform floating intervening deck	
Layer 33_2	bridge bridge structure bridges brid Bridge	ship orbit aircraft sail vessel	Kuwait Nile Edmonton Saskatchewan Tulsa	

Table 1: The top-8 token decodings of the largest three singular vectors of the detached Jacobian for the layer outputs from Qwen 3 14B for the sequence "The bridge out of Marin is the" with the prediction [[only]] (note: some tokens do not appear due to unicode display issues). Legend: "Bridge", "only", "highway", "exit", "most". This is a selection of the middle layers, see supplemental Table 5 for the full table that extends to the last layer.

3.4 Analysis of the SVD across models

Applying the SVD to the detached Jacobian matrices across a diverse set of input phrases reveals both shared computational principles and distinct predictive strategies between the Llama 3.2 3B and Qwen 3 4B models. While both models demonstrate consistent low-dimensional semantic representations, they exhibit systematic differences in how they resolve linguistic ambiguity and compose predictions. See Fig A4 in the appendix for details.

3.4.1 Shared structural properties

Both models demonstrate that next-token prediction operates within extremely low-dimensional subspaces. The singular value spectra for each token's detached Jacobian matrix consistently show sharp, rapid decay, with the first few singular values capturing the vast majority of variance across all tested phrases.

Both models demonstrate a shared mechanism of progressive refinement, where later tokens systematically narrow the prediction space. For "The new system," the initial token "The" 'yields general candidates ("is," "of," "has," "will"), while "new" introduces contextually relevant options ("allows," "requires"), and "system" further refines toward specific technical verbs ("includes," "supports").

3.4.2 Divergent predictive strategies

Despite shared computational foundations, the models exhibit systematic differences in prediction strategies that reveal distinct architectural biases.

The models demonstrate contrasting approaches to phrase completion with differing emphasis on grammar and semantics. For "Were singing," Llama predicts the grammatical conjunction "[[and]]" with U_0 candidates dominated by function words ("and," "the," "in," "a," "to"). Qwen instead predicts the specific noun "[[bowls]]," identifying the compound "singing bowls" with U_0 candidates entirely composed of thematically related nouns ("bowls," "bowl," "birds," "lessons," "competitions").

The models show different strategies for handling phrases with multiple interpretations. For "The open door," Llama predicts "[[policy]]," correctly identifying the idiom "open door policy," with "policy" appearing prominently in its U_0 vectors. Qwen provides the literal completion "[[is]]," with its U_0 containing semantically related nouns ("ways," "keeper," "policy," "frame") rather than grammatical continuations.

A subtle difference appears in how final tokens influence predictions. For "To prevent," Qwen exhibits a two-part mechanism where the verb "prevent" primes semantic concepts (U_0 contains "corrosion," "fires," "accidents," "rust") while the syntactic choice ("[[the]]") is governed by earlier grammatical constraints from "To" (U_0 contains "the," "a," "and"). Llama's U_0 for "prevent" directly contains next-word predictions ("the," "a," "and"), suggesting a more integrated prediction strategy.

3.5 Layer output singular vectors

Table 1 shows the top-8 token decodings of the three largest singular vectors of the detached Jacobians of selected layer outputs for Qwen 3 14B. The words "bridge" (and its variants), "highway", "exit", "most" and "only" are highlighted to show their appearances in singular vector decodings. Early layers are excluded as the decodings are unintelligible. The emergence of intelligible tokens in later layers is shown in the tables as something like a phase change in the representation. Qwen 3 generates infrastructure and engineering related concepts before producing "only".

Fig. 4A shows the normalized singular value spectra of the detached Jacobian at the output of every layer. Llama 3.2 3B has 28 layers, and decoding the largest singular vectors shows that the word representation of these intermediate operations is not interpretable until later layers. From the decoding of the top singular vector by layer, "only" emerges in layer 19. From the map of the progression of the projection of the top two singular vectors onto the top two singular vectors of the last layer in Fig. 4B, we first see a shift at layer 11 toward the prediction.

Since the layer-by-layer operations are only linear and have no higher-order terms, the stable rank $R = (\sum_i^L S_i^2)/S_{max}^2$ serves as a measure of the effectively dimensionality of the subspace of the representation at a particular layer.

When looking at $W_{0\_\text{to}\_k}$, the cumulative layer transform up through layer k, the dimensionality of the detached Jacobian steadily decreases. When considering each layer i as its own individual transform W_i (where $W_{0\_\text{to}\_k} = \prod_{i=0}^{k} W_i$ for the simplified scenario of a single input token; there are other cross-token terms not shown here for mid-layer detached Jacobians for longer input sequences), we also see a large peak in dimensionality near the end.

3.6 The detached Jacobian as a conceptual steering operator

Steering vectors are a well-known technique for altering LLM outputs (Liu et al., 2023) where a vector with certain properties is added to a mid-layer representation, and the sum is passed through the rest of the network to generate an output token. Here we utilize the detached Jacobian as an operator instead of an additive vector, and compute it from an intermediate layer for a "steering" phrase like "The Golden Gate" (after the "Golden Gate Claude" demo (Templeton et al., 2024)). The model predicts "Bridge", and this detached Jacobian matrix is used to steer the continuation of a new phrase toward this concept. For a new input phrase, like "Here is a painting of the", the "new" input sqeuence's embedding vectors $\mathbf{x}^*_{\mathbf{new}}$ are

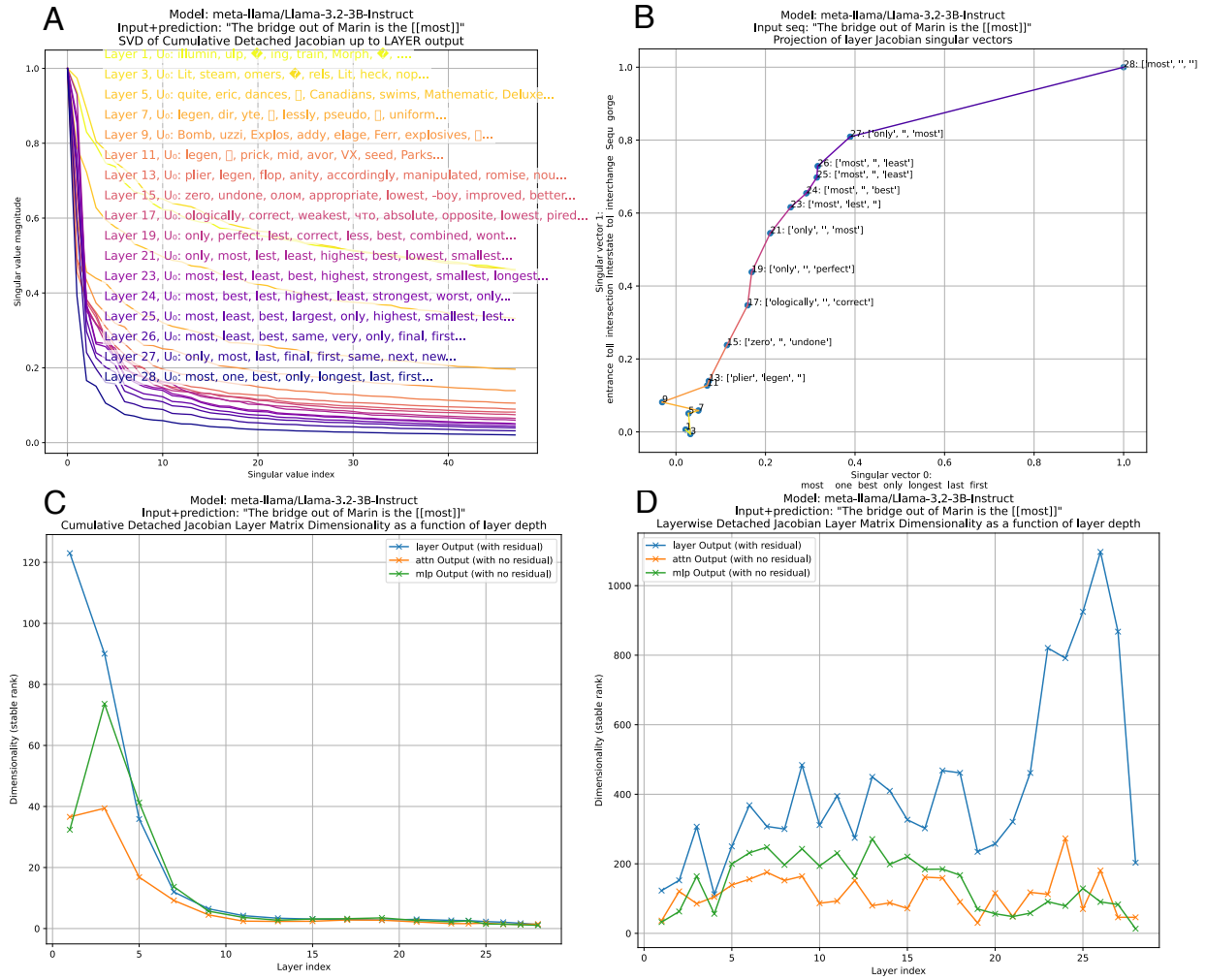

Figure 4: Since the transform representing the model forward operation is linear after detachment, we can also decompose each transformer layer as a linear operation as well. A) The singular value spectrum for the cumulative transform up to layer i. Note that later layers are lower rank than earlier layers. The top singular vectors of the later layers show a clear relation to the prediction of "most". B) The projection of the top two singular vectors onto the top two singular vectors of the final layer. The singular vectors of the first 10 layers are very different than those of the last layer, so the projections remain close to the origin. At layer 11, they begin to approach those of the output layer. C) A measurement of the dimensionality of the cumulative transform up to the output of each layer as the stable rank. Within each layer, the outputs of the attention and MLP modules (prior to adding the residual terms) can also be decomposed as linear mappings. The dimensionality decreases deeper into the network at each of these points, except for a slight increase for the attention and MLP module outputs in layer 3. D) The dimensionality of the detached Jacobian for the layer-wise transform at layer i for the layer output, as well as the attention module output and MLP module output.

multiplied by the detached Jacobian previously computed from the steering concept $\mathbf{J}_{\mathbf{L}}^{+}(\mathbf{x}^{*}_{\mathbf{steer}})$, scaled by λ and added to the layer activation $\mathbf{f}_{\mathbf{Li}}$ from the "new" input.

$$\mathbf{f}_{\mathbf{Li}}(\mathbf{x}) = \lambda \cdot \mathbf{f}_{\mathbf{Li}}(\mathbf{x}^{*}_{\mathbf{new}}) + (1-\lambda) \cdot \mathbf{J}_{\mathbf{Li}}^{+}(\mathbf{x}^{*}_{\mathbf{steer}}) \cdot \mathbf{x}^{*}_{\mathbf{new}} \tag{16}$$

Model	Layer intervention	Input sequence	Normal response	Steered response
Llama 3.1 8B	24 / 36	'I'm going to arizona to see the'	'I'm going to arizona to see the Grand Canyon. I've heard it's a must see. I've also heard it's a bit of a trek to'	'I'm going to arizona to see the Grand Canyon, and I'm planning to hike the Bright Golden Gate Bridge (I think that's the name of the trail) in the Grand Canyon.'
Qwen 3 8B	24 / 36	'Here is a painting of the'	'Here is a painting of the same scene as in the previous question, but now the two people are standing on the same side of the building. '	'Here is a painting of the Golden Gate Bridge in San Francisco. The Golden Gate Bridge is one of the most famous bridges in the world. '
Gemma 3 12B	33 / 48	'I went to new york to see the'	'I went to new york to see the memorial and museum. It was a very moving and emotional experience.'	'I went to new york to see the 10th anniversary of the Broadway show, "The Golden Gate Bridge Bridge." It was a great show.'

Table 2: Detached Jacobian matrices as steering operators, pilot results with Llama 3.1 8B, Qwen 3 8B and Gemma 3 12B.

This steered intermediate representation is then put through the remaining layers of the network and the next token is decoded. The detached Jacobian must only be computed once for the steering concept, and therefore this method is rather efficient. Table 2 shows how the detached Jacobian from an intermediate layer imposes the Golden Gate Bridge as the semantic output coherent with the rest of the input sentence, even when it is difficult to make a logical connection. Beyond demonstrating practical utility, the success of the steering operator provides validation that the detached Jacobian captures actual semantic representations.

4 Discussion

The detached Jacobian approach allows for linear representations of the transformer decoder to be found for each input sequence, without changing the output. The intermediate outputs of each layer and the attention and MLP modules are also accurately reproduced by the detached Jacobian function.

The detached Jacobian operation is accurate only at the specific operating point at which the matrices were computed by the PyTorch autograd function. A short distance away in the input embedding neighborhood, the detached Jacbian will be extremely different because the manifold is highly curved. (Although local neighborhood validity is less applicable to LLMs which map tokens to embedding vectors, as inputs will only ever discretely sample the embedding space, and there is not an obvious need for exploring the local neighborhood to embedding vectors that do not represent words from the input vocabulary). The manifold is not piecewise linear, but only has a linear equivalent at the operating point, which can be found numerically for every input sequence.

5 Conclusion

We have demonstrated that a number of open-weight LLMs have equivalent linear representations for a given input, where a set of detached Jacobian matrices completely describes the forward computation, and that the predicted token probabilities of the reconstruction have a relative error on the order 10^{-14}. Although

this method requires intensive computation for decomposing single-token predictions, the Lanczos method that does not compute the full Jacobian matrix greatly improves the memory efficiency, and it should be possible to run an experiment scaling this to well-known LLM datasets.

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A Appendix

A.1 Pointwise linear approximate GELU

Gemma 3 uses the approximate GELU activation function. Below $\gamma = 0.44715$. Here is the derivation of the pointwise linear version of GELU used for Gemma 3 in the preceding analysis.

$$\mathrm{GELU}\left(\mathbf{x}\right) = \frac{1}{2}\mathbf{x}\left(1 + \tanh\left[\sqrt{2/\pi}\left(x + \gamma\mathbf{x}^3\right)\right]\right) \tag{17}$$

$$\mathrm{GELU}\left(\mathbf{x}\right) = \frac{1}{2}\mathbf{x}\left(1 + \tanh\left[\sqrt{2/\pi}\left(x + \gamma\mathbf{x}^3\right)\right]\right)|_{\mathbf{x}=\mathbf{x}^*} \tag{18}$$

$$\mathrm{GELU}\left(\mathbf{x}^*\right) = ([\frac{\partial}{\partial\mathbf{x}}\mathrm{GELU}(x)]|_{\mathbf{x}=\mathbf{x}^*}) \cdot \mathbf{x}^* \tag{19}$$

A.2 Code availability

Code is provided as a zip file (and will be made available on github).

A.3 Singular vectors across model families

Fig A2 shows this same analysis for Llama 3, Qwen 3 and Gemma 3 across two different sizes of each. Note the low-rank structure of each of the detached Jacobians, as well as the differing decoding of the top singular vectors from each input embedding vector. The first or "beginning of sequence" token has the highest magnitude in each spectrum reflecting how the positional encoding is entangled with semantic information in the detach Jacobian representation.

A.4 Additional models

Pointwise linearity for Deepseek R1 0528 Qwen 3 8B Distill, Phi 4, Mistral Ministral and OLMo 2 are shown on the following page. See Fig. A3.

A.5 Semantic Emergence in Transformer Layers

The first singular vectors of the detached Jacobians for the layer outputs from Llama 3.1 8B, Gemma 3 4B and Qwen 3 8B for the sequence "The bridge out of Marin is the" are shown below on the following page. These are expanded versions of Table 1 from the main text.

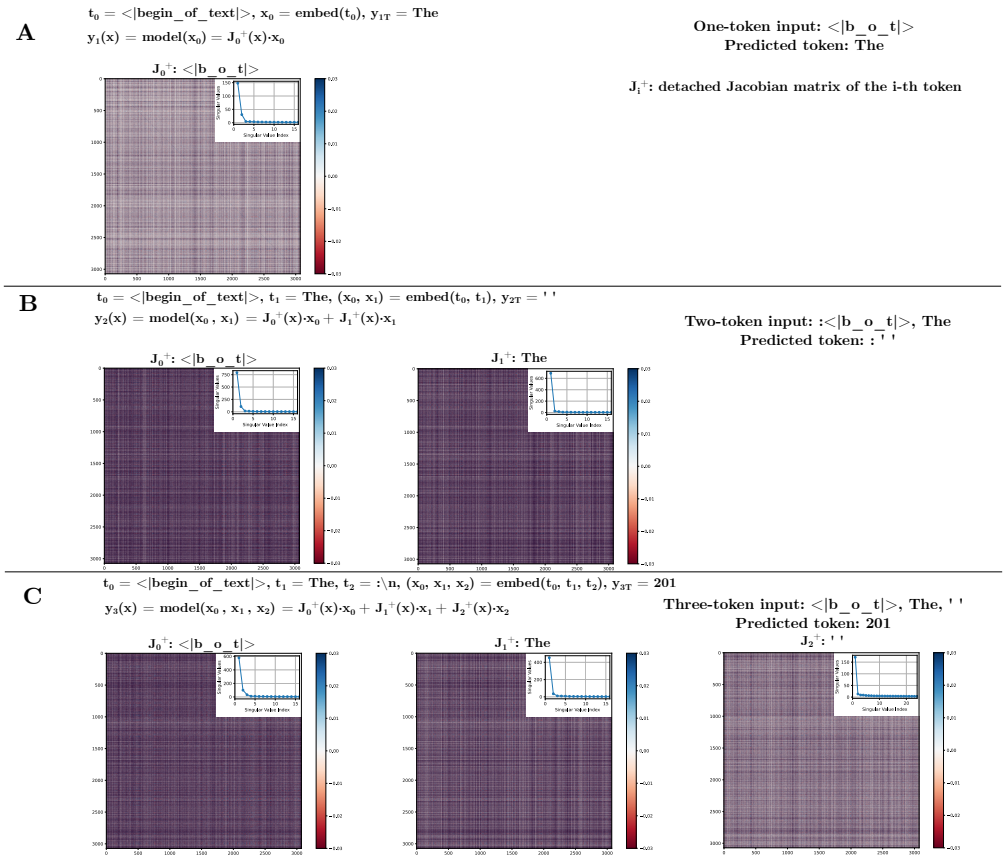

Figure A1: An overview of next-token prediction in the Llama 3.2 3B transformer decoder and decomposition of the predicted embedding vector computation using the detached Jacobian. Generating three tokens with only $< |BoT| >$ as input produces "The 201". For each prediction, each input token $\mathbf{t_i}$ is mapped to an embedding vector $\mathbf{x_i}$, and the network generates the embedding of a next token. The phrase turns out to be "The 2019-2020 season". The detached Jacobian $\mathbf{J}^+(\mathbf{x})$ of the predicted output embedding with respect to the input embeddings is composed of a matrix corresponding to each input vector. Each detached Jacobian matrix $\mathbf{J}_\mathbf{i}^+(\mathbf{x})$ is a function of the entire input sequence but operates only on its corresponding input embedding vector. The matrices tend to be extremely low rank, shown in the inset figures, and the matrix $\mathbf{J}_\mathbf{0}^+$ varies across A), B) and C) above because the input sequences differ. Since the detached Jacobian captures the entirety of the model operation in a linear system (numerically, for a given input sequence), tools like the SVD can be used to interpret the model and its sub-components.

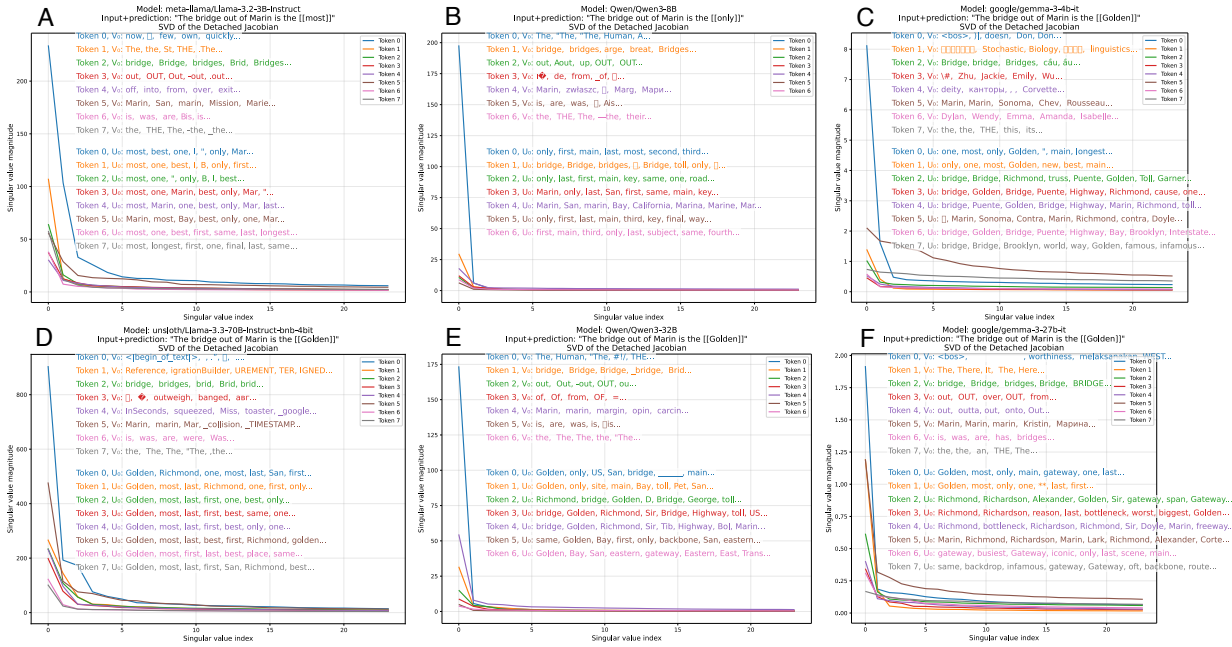

Figure A2: Singular value decomposition of the detached Jacobian for different families and sizes of language models (from 3B to 70B parameters) evaluating the input sequence "The bridge out of Marin is the", followed by a predicted token. The left singular vectors decode to tokens related to bridges and local geography, particularly the Golden Gate Bridge, while singular value spectra all have extremely low rank (see below for quantification). Each row shows top tokens associated with different singular vectors, demonstrating how models encode semantic knowledge about the input sequence and the prediction. See Fig. A3 for Deepseek R1 0528 Qwen 3 8B Distill, Phi 4, Mistral Ministral and OLMo 2.

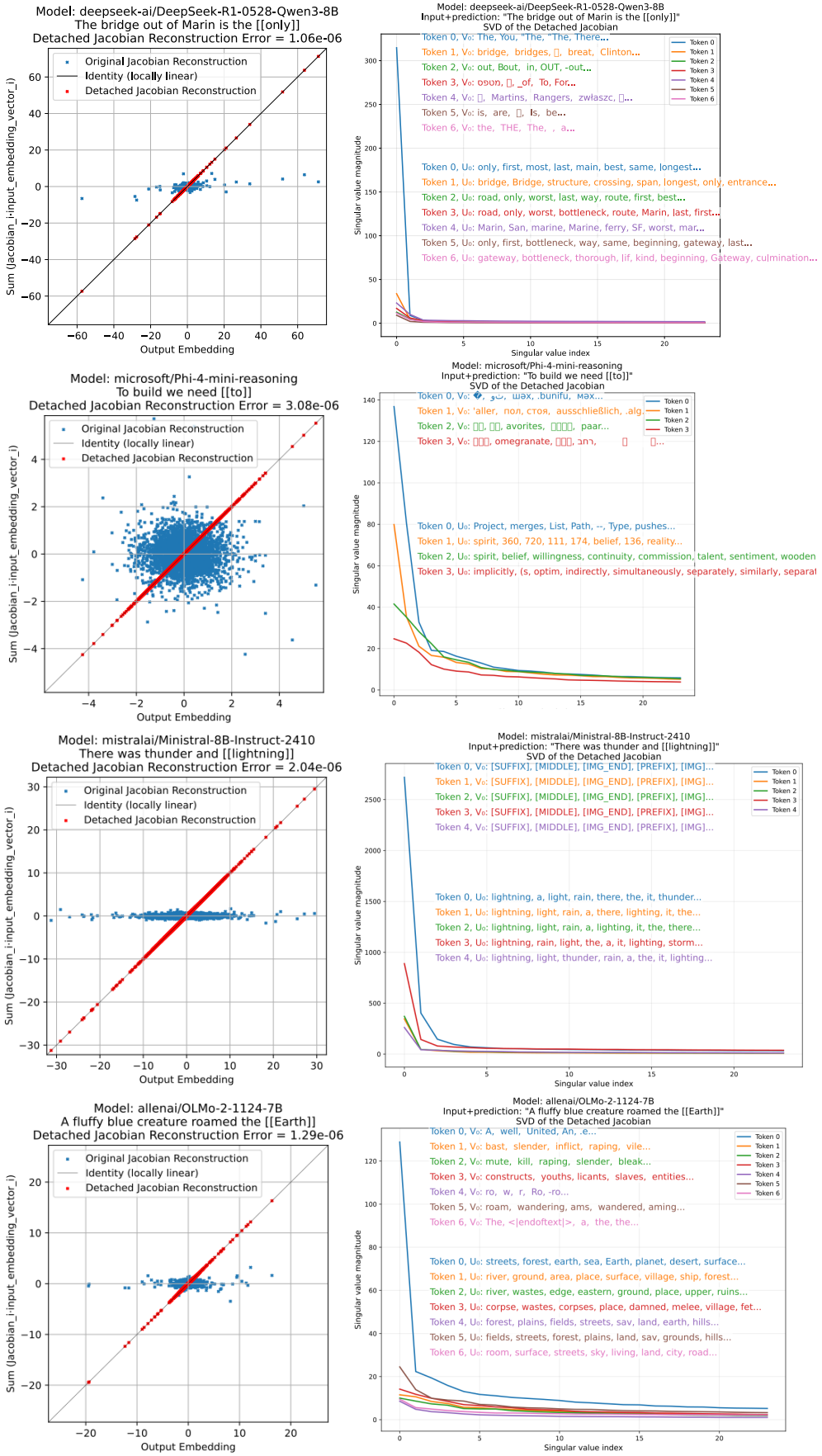

Figure A3: The detached Jacobian reconstruction error and SVD for Deepseek R1 0528 Qwen 3 8B, Phi 4 Mini 4B, Mistral Ministral 8B and OLMo2 7B.

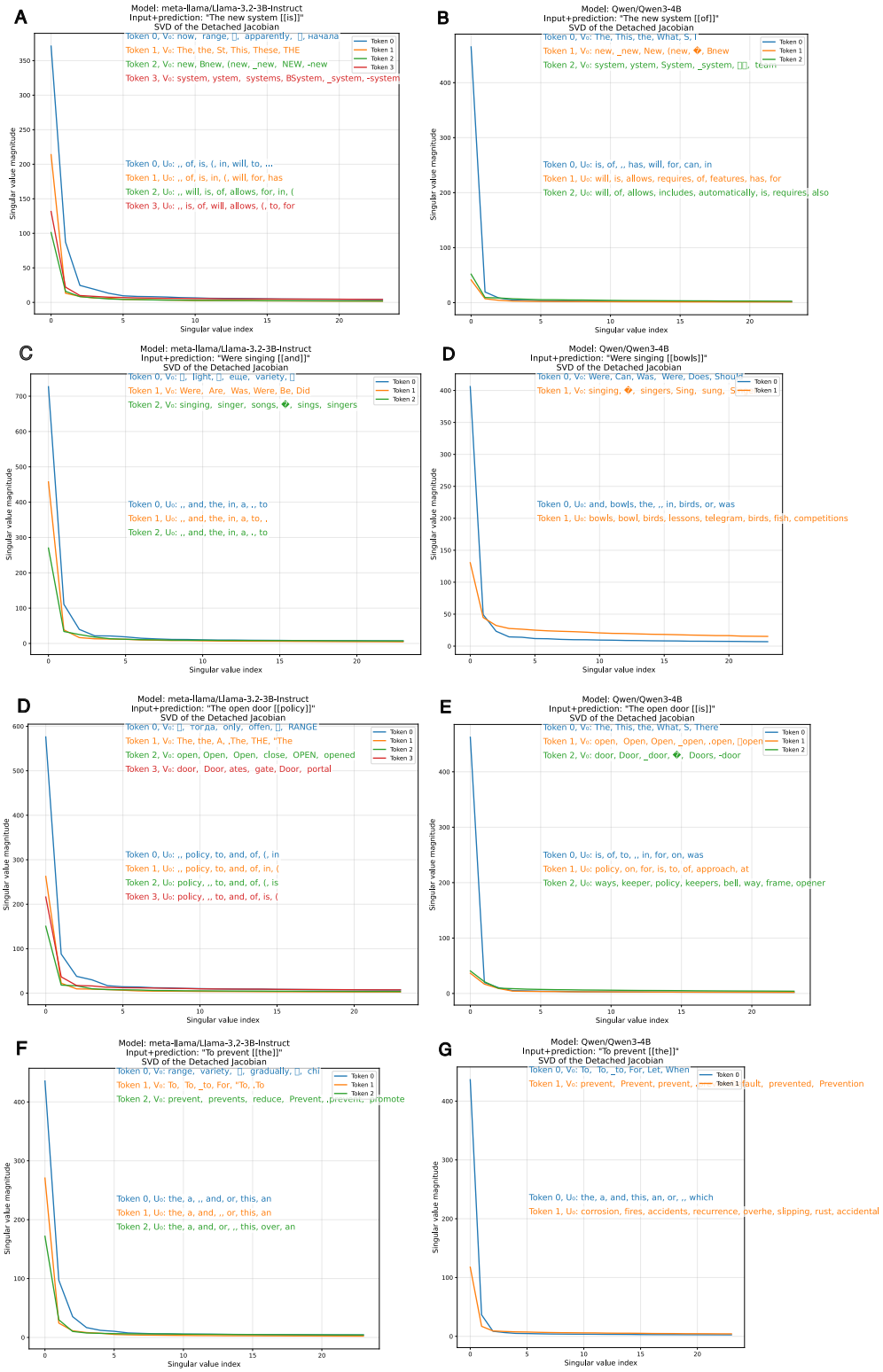

Figure A4: Comparison of detached Jacobians for the same phrase across models.

Legend: "Bridge", "only", "highway", "exit", "Golden", "most".

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Layer 24_2	uluk fabs dealloc anlk Brig Roose simd Bud	Marin dea ?type zc chez Berkeley app aidu	Marin SF .sf sf Oakland San SF Salesforce	San San Bay SAN bay igne bay Silicon	Bay bay San bay slee SF Bay Yer	Santa Santa Monterey santa 831 Son Laguna	bridge urovision suspension Suspension chez idget .uf ombat	urses uckle acier ahren ederland NONNULL
Layer 25_0	toll bridge vi subject connecting exit Bay only	toll bridge Golden vi tol Toll Bridge Golden	toll span bridge tol vi latest bridges Toll	toll exit Exit Marin tol Golden Highway cause	Marin Golden toll Richmond Golden tol exit Highway	Marin Richmond sf 415 SF Golden SF Skywalker	toll only Golden tol Bay KeyType San vi	toll tol KeyType Golden dealloc Bay vi connecting
Layer 25_1	Marin aidu Skywalker arm sf	riz iny jev thing 415 contra	Pacific POSIT Via c Santa tracks rough Backbone	kip between chant only ogo deterior gir oke	uluk acic Maul Ava Jal Los Los uda	Bay Oakland Stanford arten San SJ Silicon Yer	elic usp asco older bridge span apas	otope part bridge abcdefghijklmnop Bridge passer tej own
Layer 25_2	uluk anlk fabs dealloc Brig GetEnumerator vka Roose	Marin chez dea ?type zc aidu ptr reib	Marin SF sf SF .sf San Richmond SF	San San SAN Bay SAN bay bay igne	Bay bay San bay SF slee Yer ogo	Santa Santa Monterey santa 831 Cupertino Son Laguna	bridge urovision .uf suspension Suspension uality piler eniable	urses acier ahren engo uncture uckle
Layer 26_0	toll subject cause San Golden ge bridge only	Golden toll bridge tol span cause Golden crossing	span toll tol bridge spans Golden crossing vital	Marin toll Golden tol exit cause Exit vital	Marin Golden Richmond toll Golden SF sf tol	Marin Richmond sf 415 SF Golden Rafael ausal	Golden only toll San KeyType tol cause Bay	KeyType Golden toll tol San connecting cause Bay
Layer 26_1	Marin aidu .Generated mainwindow .scalablytyped	415 arching iny n s contra riz	Pacific Via Santa rough rou annel Santa route	ogo chant only ge LastError rael deterior owi	uluk Ava Bailey Los uta Norm Los Brig	Bay Oakland arten Stanford SJ Silicon San SJ	elic usp asco chwitz GG SF ederland	part otope bridge Bridge abcdefghijklmnop ictured of passer
Layer 26_2	uluk Brig anlk spans .Atomic fabs Bailey plied	Marin ptr dea ensis aidu chez lands inas	Marin sf SF .sf SF Richmond San 415	San San SAN Bay igne Golden Santa bay	Bay bay ogo Yer San SF bay slee	Santa Santa Monterey santa Son Cupertino Span los	.uf bridge urovision Suspension eniable idget etrain suspension	urses engo ahren n ederland eteria
Layer 27_0	subject only cause SF ge exit connecting toll	span toll Golden cause tol San Toll only	span toll tol spans vital Span symbol latest	toll tol cause Golden exit span vital Vital	Golden Richmond Marin SF toll tol Vital span	Marin Richmond sf SF Tib 415 Golden ausal	only San Golden KeyType tol toll cause Bay	KeyType San Golden tol toll only connecting Bay
Layer 27_1	Marin mainwindow /effects .Generated	arching n pone s yar	Pacific Santa .Atomic Santa annel route rou POSIT	chant slee only linking deterior ogo ge LastError	.Atomic Ava uluk Bailey Norm strand lico TMPro	Bay San SJ Oakland SJ Stanford sj Frem	elic chwitz n usp amp GG antic span	otope part abcdefghijklmnop ictured own hereby urd lijk
Layer 27_2	.Atomic uluk Bailey eview elig stdout ffset	Marin ensis zc dea chez lands agna	Richmond Marin SF sf .sf SF San SF	San San Bay SAN bay Santa bay igne	Bay San slee bay SF ogo connecting SAN	Santa Santa Monterey santa span Highway Span	.uf bridge idget etrain uddy urovision .lv eniable	n ahren engo acier eteria urses ederland
Layer 28_0	Richmond only subject one last symbol toll I	Golden toll Richmond tol span San Toll only	span toll symbol tol latest Richmond only final	Richmond toll tol Golden final only Richardson Vital	Richmond Golden toll Richardson tol Marin Vital Toll	Richmond Marin SF Golden SF Rafael sf Mu	only Golden San Bay most tol toll Richmond	Golden San tol KeyType Bay toll only Richmond
Layer 28_1	P .Generated /effects	yar pone arching n s	Pacific .Atomic Santa Via Samuel twisting route	linking chant slee unn only link ogo deterior	Ava Desert Thomas Henry uluk Bailey strand .Atomic	Bay Bay bay SJ SJ bay sj bile	n chwitz elic antic acier GG YT bridge	otope part own integral abcdefghijklmnop lijk ta
Layer 28_2	uluk Bailey Ava ffset .Atomic jak Whip Santa	Marin odian dea ensis agna agnar zc olin	Richmond SF Marin SF sf .sf SF San	Bay San bay San Bay bay SAN Golden	Bay bay bay slee ogo SF San SAN	Santa Santa Gu Jal Monterey Son santa	.uf urovision piler idget eniable frozen unta	ahren n urses acier ogie eteria
Layer 29_0	only Richmond final last most one subject symbol	Golden most tol toll final Richmond Bay Golden	tol last final Golden symbol latest toll most	Golden final most tol last Richmond toll only	Golden Richmond most tol Golden toll final GG	Marin Richmond Golden GG Rafael Mu SF SF	Golden most only tol Bay Golden same golden	Golden tol most Bay Pacific Golden San Richmond
Layer 29_1	Golden .Iter .Generated tslint	pone n arching beiter Ped yar jev	Via Santa Pacific Samuel Rim Corner winding coast	slee KeyId i chant solution ogo linking Mercer	Ava Thomas Sul lico Crawford strand Av Henry	Bay Bay bay bay SJ SJ bile	chwitz n antic elic toll oleon	own otope *backslash*grid part orda unique STRUCTURE /import
Layer 29_2	Marin abra riad seite theless ordion sonian	Marin olin marin nov ensis aser agnar nov	Marin SF SF .sf Richmond sf San SF	Bay bay San San Bay bay SAN building	Bay slee bay ogo bay nisi Yer	Santa Gu Santa Jal Wilson Arnold	.scalablytyped ge idget Duffy aeda fillType izr zimmer	.scalablytyped ahren urovision fillType ungeons

Table 3: The top three singular vectors of the detached Jacobian for the layer outputs from Llama 3.1 8B for the sequence "The bridge out of Marin is the" with the prediction [[Golden]].

	Input token 0	Input token 1	Input token 2	Input token 3	Input token 4	Input token 5	Input token 6	Input token 7
Layer 13_0	nt only the alors that ... and ..	the that only nt and most called either	probablement Guad alcanz Lans Yellow yaitu	the nt called that only one	NavBar hug headwinds rollercoaster brutal carnage angry toll	NavBar Marathon tzv Flower Bruce Broad Central Pam	... us nt : and of if	y er a e an
Layer 13_1	sh handful Shaq fame mselves pity mga	Sur GONE). Ret Genau Ret	the and that the ... and if nt	Empty Called Taj Input Fore Aqui Cc Fool	the and that or ... or as	.. only one or nt (/ ((?	<bos> meisten socit ionato lma	
Layer 13_2	ively ional]]);	0 5 1 2 4 mete 3	Called March Bon Entity Clock Patricia Bin	Halloween gonna roller kiddos creepy necesitas Gonna gotta	Awesome = called Called =	virtues delights (bimodule quaint triumphs naturalist medieval	ro furl l el	zelfde el as
Layer 14_0	only that the nt ... one .. either	only the that one nt either only those	vecchio Bridge Guad probablement iconic menambah Night	one only not nt racist terrorist suicide	Airports Cable HDMI cable Rodeo HDMI NavBar	mountain Mountain Hiking alpine Watershed Highland Hiking Mountain	us if ... nt ert called	y er a e an
Layer 14_1	the 1 robot uvre	Sur GONE MaxLength Toto heus Seg Novo	the racist extremist that those terrorist scenic anarch	Blank Manual Pair Quick Early Initial Alternatively Bon	the that and ... those at perennial not	NASCAR Mega TikTok Walmart khususnya Bekasi Urban City	meisten <bos> lma ionato ilerden tl	zelfde as el
Layer 14_2	Tyl	0 1 5 2 4 3 verwenden 6	and already after sure Z AL only development	gonna boho marchandises foodie trek necesitas chopper	tiktok Tiktok veldig incroyable skincare TikTok you Beyonce	Baltimore Philadelphia Philadelphia skyscraper Baltimore skyscrapers Londres ICAGO	ro l ainder kz	
Layer 15_0	only called one probably either the very	only the one either that called probably transportation	iconic Bridge bridge IQR Nope puente bridges Bridges	one only probably called airport transportation highway contender	Airports airport Airport westerly Airport freeway eastbound	Watershed Maple Recreational Mountain Glen Route Pine Glen	called ... only : ert	
Layer 15_1	feminism 1 robot imperialism ems polticas	tzw Seg tzv North Sur Secondo aman atraves	one extremist racist the camping terrorist supposed military	Blank Flight Gas Quick Clock Oxygen Cyclone Called	the that one called those only not ...	Walmart ASEAN airport Etihad NASCAR Nigerian Airport airports	<bos> meisten lma ionato tl	
Layer 15_2	)).	0 1 5 2 verwenden 3 4 6	called Sept (Grand	Anime Ecommerce boho foodie Ayurveda Genre Etsy Girlfriend	Hydro Introduction Bibli Water Handbook History Kirk Guide	only timeless lesbian (algae bike minimalist where	Empty partidas tion varchar grnt	i as el
Layer 16_0	only one very first the route	only the one first three two very	iconic Bridge bridge Centennial Greater Golden bridges Iconic	only route Route transportation one most scenic very	Route airport westerly route detour Airport freeway eastbound	Route Watershed watercolor Valley Pine hiking Recreational Hiking	only called on mile ... at	
Layer 16_1	tzw North bernama Nec tangent Bitter Seg getAvg	North North tzw tzv largest lagoon sogenannten shortcut	coastal scenic not military one likely very location	Flight Quick Aer Funk Blank Oxygen Air Ginger	the not located that one three only in	Texas airport Miami Walmart cities NASCAR Nigerian city	<bos> ophylline	zelfde as el
Layer 16_2	Arc Approx	0 5 1 2 3 Provides 6 4	turbo Hydro Turbo Geo Mapa northward blasted north	Anime Ecommerce Headphones Millennials emocional Genre Beatles	Hydro Northern Revised Introduction Route Nelson Percy Berkeley	only aesthetic timeless true cottage hippie wooden antique	HPC entropic uncharted disruption almighty	
Layer 17_0	only first most one very two the	only one first the two most very	iconic legendary famed famous Greater namesake infamous Centennial	only most one very iconic route probably not	airport blue Route cable route westerly tunnel scenic	Route iconic most north gateway scenic recreational Valley	only on first North ones at	
Layer 17_1	hacerlo tangent tzw bernama north loophole	North north North tzv tzw sogenannte sogenannten behem	only very not scenic one likely military extremely	Flight adrenalin Funk Oxygen Aer Oxygen Turbo Magenta	in the not only three that located buildings	Texas cities UAE Kuwait airport Nigerian military Saudi	<bos>	zelfde as el
Layer 17_2	). Paths Tub .).) Endpoints Heap	0 1 5 2 3 Provides 4 verwenden	Turbo TOC Pipeline Aviation City Route Water	Ecommerce Acne Anime msicas Attractive Decorative eCommerce	Hydro Traffic Crossing John Water Highway Network Northern	alpine antiques antique naturalist only mountain never timeless	uncharted brave almighty HPC entropic veritable	
Layer 18_0	only first most one very two the	only first one most two the that	bridge Bridge bridges iconic crossing Bridges	only most one iconic first very three	only iconic blue most scenic airport route gateway	iconic most only Route gateway scenic coastal watercolor	only first ones way infrastructure	
Layer 18_1	loophole Nec Locator FBSDKAccessToken peanut sebaik	behem giant loophole lagoon swamp MaxLength Nec Locator	military only coastal area likely location beaches areas	Flight Funk Gina Magenta Acceler Going ToGo	in the located other ed of only state	Kuwait cities UAE Nigerian Philippines Saudi Texas Singapore	Luego gleiche ophylline same	zelfde oretically ophylline t mselves
Layer 18_2	). .). Paths	0 Design 1 Style 3 Styling Provides	Water Pipeline Watercolor Pipelines Fountain Beacon Marathon Balloon	Acne Ecommerce msicas Ayurveda halloween Geschwindigkeit Anime	Nelson Hydro Traffic Kirk John Water Branch Margaret	alpine mountain Alpine skiers naturalist alpine antique conservation	uncharted entropic almighty brave disruption brutally	
Layer 19_0	only first one most two highway the	only one first two that most second	Bridge bridge bridges Bridges Crossing Bridge Golden crossing	only most one highway coastal North first	highway only North freeway Highway coastal blue Route	subway Route coastal North East iconic most Highway	only first ones bridge one way highway	same splitLength
Layer 19_1	Ring Coc Road reverse Rd Beacon	Bridge Ring Coc Road notorious iconic behem Reverse	coastal military area location areas most beach beaches	Funk Flight ToGo Honestly Thro Gina Launching	other in the emperor government located buildings of	Kuwait Saudi Nigerian UAE Singapore Oklahoma Florida Nigeria	gleiche Questo	zelfde oretically t
Layer 19_2	vreau rupani nggak inclusin advogado comprens emphas	Crossing Compre Laufe Steel Indem Cht Bridge	Aviation Outreach Pipelines Turbo Wastewater Pipeline Brewing Beacon	Epilepsy Watercolor Bathroom Ayurveda Genre Biblioteca Ecommerce Mindfulness	Bridge Traffic Berkeley Branch Gene Brid Md Nelson	alpine mountain wilderness Alpine mineral naturalist mountaine archaeological	noon the whack	
Layer 20_0	one only most first second very	one only most first second best	Bridge bridge bridges Crossing Bridges crossing bridging iconic	one only most ones highway first	one only most highway ones Highway coastal best	most Highway Highland suburban waterfront Gateway Route gateway	one only ones most largest first	same detriment
Layer 20_1	Mun Mun Har Tak Coc Trinity Beacon	Har Har Est Tak Mega Rainbow Coc	area one areas most location only coastal military	ToGo Honestly Benzo thru Launching Ahh Flight	other ancient government constituent Indian dynasty highest oldest	Belarusian Cleveland Minsk Essex Belarus Noida	substantiate Pflanzen	zelfde t e y er
Layer 20_2	Zap Typical Ric Tub +)$ Ridge	Bridge Crossing Bridges Crossing Bridge Guad	teapot minus Vectors Spiral spiral turbo spirals	Biblioteca Bridge Campground Bibliothque Canva Brighton ocuk BufOffset	Traffic Kirk Transit Bridge Linking Brid Md Lincoln	Jamaican Kenyan Karachi Jamaica Southampton Nassau	noon coming via	
Layer 21_0	bridge only one most highway first best	bridge only one most first highway best	Bridge bridge bridges Bridge Bridges Crossing crossing bridging	bridge Bridge highway bridges only one most Highway	bridge highway Bridge Highway only bridges most road	bridge Bridge bridges ferry Highway highway Ferry crossing	bridge only Bridge highway most Highway bridges road	same most simplest largest easiest best greatest strictest
Layer 21_1	Bridge Bridge bridge bridges zungen Tol Tak	Bridge bridges Bridge bridge Bridges bridging Tol	most coastal area areas maritime one closest fastest	Ahh stints stint salir Says	university highest University largest ancient museum emperor British	Singapore Tianjin Chicago Houston Dallas Etihad Shreveport	nhiu caza Pflanzen Luego	y er a e zelfde t
Layer 21_2	vreau gobierno totalit comprens nggak lackluster ejrcito	Bridge Crossing Bridges Ponte Crossing Bridge	mansion Architectural Sculpture Basilica monumento Monument Museum edifice	Bridge Canva ocuk Orchard Biblioteca Thng Counseling Shopify	Bridge Bridge Crossing Brid BRIDGE bridging	Crimean coral Worthing Maas Argentina	Bridge Brid Highway Quiz	
Layer 22_0	only bridge one most first highway new	only bridge one most first new highway	Bridge bridge bridges Bridges Bridge bridging Ponte	bridge only Bridge highway bridges one most ferry	bridge only highway Bridge Highway bridges most route	bridge Bridge bridges ferry Highway only Route ferries	only bridge Bridge highway bridges most Highway famous	same most only bridge simplest easiest beginning best
Layer 22_1	Namara Puente chercher zungen McCullough klnb Wheeler	Bridge Puente puente bridges Tol Bridge	highway road route roads fastest most coastal coast	Ahh <unused2104> Whats stints <unused1771>	university University ancient British dynasty Buddhist emperor medieval	Cape Cape	Catering Luego nhiu Tato caza	y er e a t zelfde
Layer 22_2	ERISA vreau lackluster gacche pabbaj ceremonia prosa i	Bridge Bridges Bridge Geral Design	routes highways roads routes route ferries freeway expressway	Canva Pinterest Shopify WooCommerce Artisan Anime Reiki eCommerce	variously Berkeley broadly comprehensively inasmuch Trait	Houston Guangzhou Dubai Karachi Chicago CHICAGO docked	obviously JJ St compare	
Layer 23_0	only bridge California most one highway freeway Bridge	only bridge California one most highway first new	bridge Bridge bridges Bridges Bridge bridging	California bridge freeway Bridge only bridges Pacific Californian	California freeway bridge California Californian california Pacific Monterey	Fairfield Surrey Brentwood Ogun Westchester	bridge only highway Bridge Highway bridges freeway most	most same bridge ones easiest only simplest quickest
Layer 23_1	zungen Langer <unused58> qualiter loadNpmTasks menghilangkan	Bridge Bridges bridges <unused58> puente Bridge Langer	California freeway coastal Pacific trailhead fastest Californian route	Ohio Alabama Nebraska Kansas Iowa Manitoba Missouri Mississippi	Chicago University Mississippi university American Iowa Nebraska Illinois	California California Sonoma Californian San redwood Californians UCS	Luego Catering caza malls opportune pundits	y er a e zelfde
Layer 23_2	Sonoma Marin Napa Marin Esprito Medford California	Bridge Bridge Bridges bridge bridges	Sonoma Californians California Californian Valle Monterey Yosemite	Sarasota Michigan Michigan Akron MICHIGAN	Minecraft Jungkook Cancun minecraft Oklahoma Miami OKC Walmart	Dart Sussex Dartmouth Dart Wiesbaden Maui	Bridge quick toned Quick JJ Bridge	
Layer 24_0	California only bridge freeway highway Highway Pacific Bridge	California only bridge freeway highway Highway Bridge one	bridge Bridge bridges Bridge Bridges bridge bridging puente	California bridge Bridge freeway bridges Highway highway only	California bridge freeway Highway Bridge highway bridges California	Fairfield Surrey Brentwood Ogun Woodbridge	bridge California Bridge Highway freeway only highway bridges	bridge Bridge bridges only freeway same ones one
Layer 24_1	<unused58> pored ! Bridges Langer	Bridges bridges Bridge Bridge puente <unused58> bridging	freeway highway route trailhead fastest roads highways pathway	Cebu Edmonton Winnipeg Alberta Manitoba Calgary Merseyside Queensland	University university Arabidopsis Mughal phylogenetic Nile skyscraper Tokugawa	Sonoma Dartmouth Swiss Swiss swiss CHF	bestselling caza pundits transpired Catering Luego	er y a e o
Layer 24_2	Sonoma Swiss Essex Marin Esprito Marin Medford	Bridges Bridge Bridges bridge bridges	routes Routes Route routes Route route route Routing	Provo Irvine Boise Malaga Anaheim Warwickshire Seattle	Minecraft PUBG Fortnite pokemon skincare nightlife Binance Pokemon	Oaxaca Hessen Barbados Tucson Dord Maui Swansea	<unused2139> Bridge Puente <unused1867> Quick Stanford Bridge	
Layer 25_0	bridge Bridge bridges California only bridge Highway highway	bridge Bridge bridges California only bridge ferry Highway	bridge Bridge bridges Bridge Bridges bridge bridging bridges	bridge bridges Bridge Bridge bridge Bridges bridging puente	bridge bridges Bridge Bridge California bridge Bridges bridging	SF Marin Contra Marin SF Burmese Bay Oakland	bridge Bridge bridges Bridge bridge puente bridging Highway	bridge bridges Bridge puente Bridge Bridges bridging bridge
Layer 25_1	Bridge Bridges Bridge bridges bridge bridging puente	bridges Bridge Bridges Bridge bridge bridging puente	highway route trailhead freeway roads road Highway trail	Cebu Utah BYU Calgary Birmingham Winnipeg Alberta Edmonton	University Noida Arabidopsis university Mughal Cambridge Universit Louvre	Ogun Ventura Fairfield Wiesbaden Windsor Arnhem	Bridges Bridge Bridge bridges bridge BRIDGE bridged	er y a e an
Layer 25_2	Marin Marin Burmese SF SF Sonoma Genova	Bridges Bridge Bridge bridges bridges	Omaha Wichita Milwaukee Houston Memphis Chicago Nebraska Detroit	Syrian Guwahati Assam Syria Arkansas Arkansas	desert Cebu Malaga Calgary Marrakech Miami Cusco LA	Maui Dartmouth Maui Kerry Kerry Dart Davao	bestselling triathlon sneaker cutest cupcake playoffs streetwear gameplay	
Layer 26_0	bridge Bridge bridges California only San Highway most	bridge Bridge bridges California only San Highway most	bridge Bridge bridges Bridge Bridges bridge bridging bridges	bridge bridges Bridge Bridge bridge Bridges puente bridging	bridge bridges Bridge Bridge puente California Bridges bridge	Marin Marin Sonoma SF sf SF Contra Burmese	bridge bridges Bridge Bridge bridge puente Highway freeway	bridge bridges Bridge puente Bridge Bridges bridge BRIDGE
Layer 26_1	Bridges bridges Bridge puente bridge bridging	bridges Bridges Bridge puente bridge Bridge bridging	route highway trailhead freeway pathway Highway fastest road	Cebu Boise Utah Birmingham BYU Warwickshire Calgary Alabama	Cambridge Noida University Merseyside Nile Universit Recife Haryana	Ventura Wiesbaden Coachella Cannes Newbury Ogun Oaxaca	Bridge Bridges Bridge bridges bridge BRIDGE	y er a e o
Layer 26_2	Marin Marin sf SF Burmese SF Sonoma	Bridge Bridge Bridges	Utah Angkor Boise Nebraska Alabama Omaha Mormon	Assam Guwahati Syrian Pyongyang Yukon Arkansas Tripura Belarusian	sf Marin Sovi postgresql Sonoma Marin SF	Woodbridge Noida Brookhaven Oakland	coolest cutest funniest bestselling most sweetest smartest	
Layer 27_0	bridge bridges Bridge California only most Highway highway	bridge bridges Bridge California only most bridge Highway	bridge Bridge bridges Bridge Bridges bridge bridging puente	bridge bridges Bridge bridge Bridge bridging puente Bridges	bridge bridges Bridge puente bridge Bridge Bridges bridging	Marin Sonoma Marin Contra sf Burmese Sovi	bridge bridges Bridge Bridge bridge puente bridging freeway	bridge bridges Bridge puente Bridges Bridge bridging bridge
Layer 27_1	Bridges puente bridges <unused25> Bridge	Bridges bridges puente bridging Bridge bridge Bridge	route highway trailhead pathway freeway most trail path	Sonoma silvest Marin Sebast Waldo Garo	University Cambridge Universit Louvre Noida university campus Recife	Ventura Wiesbaden Coachella Cannes Newbury Hessen Provence	Bridge Bridge Bridges BRIDGE bridge	y er a e o
Layer 27_2	Marin Marin Sonoma Burmese sf	Struct Structural Structural Struct	Utah Mormon Boise Angkor Alabama Cebu Birmingham Nebraska	Assam Guwahati Yukon Belarusian Arkansas Cambridge Tripura Tyne	Sovi Marin Sonoma contra postgresql Marin	Woodbridge Oakland Noida Delta	coolest healthiest best cutest most beste newest	s
Layer 28_0	bridge Bridge bridges only most California San Highway	bridge Bridge bridges only most California San Pacific	bridge Bridge bridges Bridge bridge Bridges bridging puente	bridge bridges Bridge bridge puente bridging Bridge Bridges	bridge bridges Bridge puente bridge bridging Highway Marin	Marin Sonoma Marin Sovi marin Contra Richmond	bridge bridges Bridge bridge Bridge puente Highway bridging	bridge bridges Bridge puente most Bridge Bridges bridging
Layer 28_1	wachung oksatta athermy puente	puente Bridges bridges bridging <unused58> athermy	highway route pathway freeway Highway most path gateway	Sonoma silvest Waldo Marin Sebast	University Cambridge Louvre Noida Universit Nile Lucknow parquet	Ventura Hessen Oaxaca Wiesbaden Sussex Maui Malibu	Bridge Bridge Bridges BRIDGE bridge	er y a e
Layer 28_2	Marin Marin Sonoma marin marin kafka	Struct Struct	Sonoma ruari yaml	Assam Yukon Guwahati Belarusian Tyne Sak Georgian	Sonoma Sovi postgresql Marin	Woodbridge Delta Egypt Oakley	coolest most newest cutest sweetest best healthiest	s
Layer 29_0	only most bridge one Golden California longest largest	only most bridge one Golden longest California largest	bridge Bridge bridges Bridge bridge puente bridging	bridge bridges Bridge Golden Highway most toll freeway	bridge bridges Bridge Highway Golden toll freeway Marin	Marin Marin Sonoma Lark Russian Contra Richmond	bridge bridges Bridge Golden Highway freeway only highway	bridge bridges Bridge most puente ones freeway Golden
Layer 29_1	wachung azitt patx athermy orragie	puente bridging bridges Bridges Bridge	route highway trail path gateway pathway trailhead most	Sonoma silvest Marin Waldo Kent Garo	University Noida Universit Assam Lucknow Nile university Louvre	Ventura Hessen Sussex Wiesbaden Oaxaca Westchester	Bridge Bridge BRIDGE Bridges bridge	s y er a e
Layer 29_2	Marin Marin Sonoma kafka Ukraj	<unused2146> struct Structure Struct Structural Structure	Snapshot nt Sonoma	Assam Yukon Belarusian Guwahati Georgian Tripura ra Sak	Sonoma Sovi UKI Marin nutty	Woodbridge Egypt Oakley	coolest healthiest best most cutest najleps sweetest funniest	s
Layer 30_0	most one only bridge California new Golden	most only one California new bridge Golden longest	bridge Bridge bridges Bridge puente bridge toll	bridge Bridge bridges Highway California Golden most puente	bridge bridges Bridge Highway Marin freeway toll Puente	Marin Marin Sonoma Contra Richmond Richmond Doyle	bridge Bridge Highway bridges Golden freeway highway California	bridge Bridge bridges most puente Brooklyn famous one
Layer 30_1	wachung arakatuh Choibalsan athermy	bridging puente bridges getTransforms	route highway trail trailhead path pathway trails gateway	Garo Sonoma silvest Waldo	University Recife Universit university Nile University Assam edifice	Ventura Hessen Ax Wiesbaden Sussex MX	most most sweetest newest healthiest	s y a e r e
Layer 30_2	Marin Marin marin Sonoma	struct Struct Structure	prescribe Snapshot nt	Assam Yukon tzt Guwahati Georgian ruzione Belarusian Sak	Sovi uniary UKI Sonoma	Woodbridge Suffolk Ipswich	Bridge Bridge Bridges BRIDGE bridges	s s
Layer 31_0	most only one bridge new main Golden	only most one new main Golden bridge	bridge Bridge bridges Bridge bridge toll puente Toll	bridge Bridge Highway bridges Golden one toll Puente	bridge Highway Bridge bridges Golden Puente toll freeway	Marin Sonoma Contra Marin Doyle contra Richmond	bridge Bridge Highway Golden bridges only freeway Puente	bridge Bridge bridges famous most same iconic Brooklyn
Layer 31_1	bottlene Comunic azitt lytres qttr	puente bridges lytres	route trail highway path pathway trails trailhead Highway	objc coc Marin	University edifice predecessor Universit Recife university machine diet	Ventura Ax MX fx mx Hessen	coolest epitome healthiest perfect ideal sneaker best sweetest	s a y er t
Layer 31_2	Marin Marin kuk	structures	Alabama Idaho Kansas Angkor Oklahoma Nebraska dunes fuselage	Assam Yukon Urs Monsieur Rivire Euh tzt	uniary contra quantify	Woodbridge Anambra	Bridge Bridge absValue measured	i

Table 4: The top three singular vectors of the detached Jacobian for the layer outputs from Gemma 3 4B for the sequence "The bridge out of Marin is the" with the prediction [[Golden]].

	Input token 0	Input token 1	Input token 2	Input token 3	Input token 4	Input token 5	Input token 6
Layer 20_0	TRY NORMAL	massage	akedown eway slow congest nodeId	eway akedown slow bottleneck .avi congest	ijk compat normal whatsoever Reflect regards	chatter	largest easiest smallest fastest first weakest closest most
Layer 20_1	AUSE nrw bbw metaphor .listFiles stret tgt	overlay extracts Liter	villa fashion getattr depress bias	whatsoever FORMAT QUESTION scenes	monster coil thm bers pee	corresponding iguiente usual pecified specified imap	h H spNet F
Layer 20_2	ade flutter Fil mon imm and ren	lyr bounding while	Entities campaign EventBus .FILL	fullest .INSTANCE hlen keyst Fortress KING RESPONS	NVIC Locations keyst titular literal overse	artisanlib H	
Layer 21_0	TRY REGARD dT	REGARD massage	eway slow exiting outbound fastest tight	eway slow fastest hardest tight exiting slow draining	Hierarchy ijk whatsoever Suit Firstly Role	chatter	first weakest largest fastest most longest easiest smallest
Layer 21_1	@end IGHL ocos UAGE crt	overlay substr tag adorn bestowed	Managed meds Choices TORT Madness machine Spare	scenes meds whatsoever hurry	bers NYSE nation dollar	.Guna iguiente corresponding ProductId esub =BitConverter pecified Frameworks	H h artisanlib
Layer 21_2	Terr tag iers imm Fil ues Mal	itol Tomorrow goodbye stash calar lyr syrup	HTTPS reinterpret UTF REFER JSON Netflix	.INSTANCE ECB keyst ESIS fullest HBO CORPOR	Proxy Preconditions contractual height Encode /exec Alamofire	H	
Layer 22_0	tweaking CONSTANTS	vacc getch Period	first hardest fastest exiting ramp	hardest fastest first exiting easiest Interstate	function whatsoever whilst Misc Hierarchy	.flash thm	thm repeat
Layer 22_1	metaphor unc DERP OBJC stret .wp ISP	substr MBOL bridge	hurry HIP opi Rockets TORT	scenes	bers nation gim pick	eec esub =BitConverter ITIVE .Guna equivalent	TRGL spNet
Layer 22_2	alk ole ool ros angan icon vn	antics iker rocking	backstory weblog SVG JSON INCIDENT	ESA keyst .INSTANCE ECB	Theme Proxy height Entities Encode ultipart /System D		
Layer 23_0	salopes CONSTANTS getch Uncomment massage TRY	metaphor bridge largest easiest only first centerpiece	first hardest unc fastest highway bottleneck	hardest first fastest easiest toughest weakest unc quickest	Whilst whilst role CONTRACT Whilst	.flash thm	thm redit dates still
Layer 23_1	metaphor unc Derne makeshift OBJC	bridge Bridge . bridge bridge	scenes WithError opi Timing presets Entering	scenes WithError	California California bers nation lover	ly ut ett ath of tra ty	TRGL
Layer 23_2	ros lovers flutter	antics jams	weblog COMPONENT annot metaphor	fullest PGA ESA keyst JVM classic focus	specialised bespoke connexion macOS UNESCO SSH EU initialise		ity ation age ury oretical ie ance acock
Layer 24_0	first third last most largest fourth culmination	metaphor largest centerpiece easiest first hardest bridge gateway	hardest first easiest fastest most ones same	hardest first fastest easiest most longest same least	Whilst whilst Firstly Whilst crate	culmination first fourth largest highest third same seventh	first fourth third last largest highest fifth most
Layer 24_1	metaphor makeshift .wp REAK	brid bridge bridges bridge Bridge	scenes LocalStorage WithError	scenes	entirety Malta main third favoured Yemen	ut ly ath ett of ality hereby	it ities
Layer 24_2	flutter ros Lingu		phenomena puzz annot metaphor	ESA fullest PGA machine focus ECB	bespoke macOS connexion specialised mount initialise UNESCO Patreon	or	
Layer 25_0	largest most first longest latest fastest last third	bridge bridges Bridge gateway	hardest ones exit easiest first most fastest highway	hardest fastest easiest most ones weakest first exit	Whilst Firstly .dimensions Mahmoud	note abortions edd	first fourth third last largest highest most weakest
Layer 25_1	bridge bridges Bridge Bridges brid	bridges bridge Bridge bridge Bridge	(exit exit exits eternity . exit	exit	Malta main entirety Jordan third Klopp Nicar	eec fax streets hotline @student tats	ities it
Layer 25_2	bridges bridge Bridge bridge parliament	Exit exit jams	INCIDENT symbolism	JVM migrations CAB largest upcoming machine	specialised initialise UNESCO bespoke connexion mount arist macOS		e cion ted
Layer 26_0	first most largest last longest latest gateway only	bridge bridges metaphor gateway connecting	highway first exit ones last hardest roads	highway hardest first weakest last road roads easiest	highway California highways road freeway most Highway Interstate	only first last fourth culmination longest highest same	first last only fourth third fifth ninth same
Layer 26_1	bridge bridges metaphor Bridges Bridge	bridges bridge structures brid bridge	.charset jams Margins	jams wipes	Malta main Jordan Egyptian Romanian central	eec @student Begin streets hotline fax	ities TRGL
Layer 26_2	parliament structures bridges Parliament bridge	Exit exit choke Exit panicked	symbolism metaphor	California California interstate Californ Maven Butter	UNESCO Brexit initialise bespoke arist	Cumhurbakan	ly ted e
Layer 27_0	first last largest bridge longest most oldest latest	bridge bridges Bridge Bridges	last first exit highway bottleneck next road choke	last first weakest highway hardest bottleneck next road	bridge highway first California next largest last latest	first last only fourth culmination weakest highest same	first last fourth third bridge fifth second seventh
Layer 27_1	bridge bridges Bridge Bridges	bridges bridge Bridge bridge brid Bridge	EXIT exit exits (exit	exit EXIT exit exits	central Malta main Egyptian key Yemen Jordan	streets hotline ieres bridge cherry reason rise	TRGL ities
Layer 27_2	bridge bridge bridges Bridge structures	Exit exit Exit exit . exit	incident EXTRA incidents	California California Seattle Butter Seattle Californ	Tibetan Swiss Tibet arist Himal	Cumhurbakan	ly ted e cion lah
Layer 28_0	bridge longest largest first busiest last oldest most	bridge bridges Bridge Bridge	highway exit bottleneck highways Highway last road exits	highway bottleneck Highway last highways exit road busiest	California bridge Marin ferry highway Oakland freeway	only first bridge last fourth culmination weakest same	first bridge last fourth third gateway highway fifth
Layer 28_1	bridge bridges Bridge Bridge	highway highways coast freeway roads road route	exit exits EXIT exit Exit	exit exits EXIT exit Exit exit	Jordan Memphis Nile Mississippi main Nicar	streets hotline ieres sang	TRGL h ities
Layer 28_2	bridge bridge bridges Bridge brid	Exit exit Exit exit exit exit	Saddam Mosul Kuwait incident metaphor	Nile Kuwait Jordan Memphis	Slovenia Sloven Croatia Manit Estonia Gael	Sy the	ly ted ments
Layer 29_0	bridge only fourth last third longest fifth most	bridge bridges Bridge Bridges	only last first highway third highways exit fourth	only last highway first busiest bottleneck third hardest	California only bridge first highway latest Oakland last	only fourth last fifth third first seventh bridge	fourth third only fifth bridge first last seventh
Layer 29_1	bridge bridges Bridge Bridges	coast highway road driveway coastline roads highways freeway	exits exit EXIT	exits exit EXIT exit	Jordan Memphis Nile Frankfurt Mississippi desert	only Only wich which ai cent only	TRGL h
Layer 29_2	bridge bridges bridge structures brid structure	Exit exit Highway Exit	Saddam Mosul Elvis metaphor incident	Nile Frankfurt Kuwait desert	Slovenia Gael villagers Tibet Tibetan	checkpoint tunnel chances nicknamed crossing dubbed tunnels	ly fully ments ted rer lah e
Layer 30_0	bridge most longest fourth third last only fifth	bridge bridges Bridge Bridge	highway only bridge last first Highway road highways	bridge only highway last Highway freeway first busiest	California Marin bridge Oakland San California Bay	only bridge fourth last fifth third first seventh	bridge fourth third fifth only first seventh last
Layer 30_1	bridge bridges Bridges Bridge	coast freeway highway coastline road roads highways	bridge Bridge bridges bridge brid	bridge Marin underwater Bridge bridge public	Jordan Memphis Mississippi Nile Missouri Nashville	sang ieres streets @student bridge	TRGL h ities
Layer 30_2	bridge structure structures bridges bridge brid	sail seab sailing Bermuda ship	Memphis Kuwait Jordan Saddam Iowa	Nile Memphis Jordan Edmonton Kuwait	Gael Tibetan Tibet Nepal Kashmir Tanzania	bridges bridge crossing	ly rer e sign fully ted liness
Layer 31_0	bridge most only last longest first third largest	bridge bridges Bridge Bridge	only last highway first bridge exit Highway most	only Marin last highway bridge first California Highway	Marin California San Bay marine seaw bay coastal	only last first bridge third fourth fifth key	bridge third only fourth first last main fifth
Layer 31_1	coast airlines Interior airline interior Lua Speedway	coast coastline coastal Coast Coastal route	bridge Bridge bridges bridge underwater brid	Marin marine underwater bridge aquatic span	Jordan Mississippi Memphis Nile Missouri Tennessee Jordan	bridge Bridge sang streets bridges ieres	TRGL h ities
Layer 31_2	bridge bridges bridge brid Bridge structure	ship sail sailing dock seab	Jordan Memphis Kuwait Mississippi	Jordan Edmonton Nile Memphis Cairo Kuwait	Mara Finnish Finn Kashmir Gael	bridge bridges crossing	e ly rer fully ted liness ned sign
Layer 32_0	bridge most only first last longest third largest	bridge Bridge bridges Bridge bridge	only last first highway most main route exit	Marin only last highway route first most San	Marin San marin Mar California marine Bay mar	only last first main key most third subject	only main last first third key bridge subject
Layer 32_1	interior airline steam airlines Trail breed vacuum	coast coastal coastline route Coast Route beach	bridge span underwater connecting deck public member	Marin underwater marine span aquatic member Meer	Jordan Mississippi Nile Missouri Memphis only main Cairo	only Only Vader only somehow ly	ities TRGL Others
Layer 32_2	bridge bridge bridges Bridge brid Bridge	ship sail dock sailing seab	Kuwait Jordan Memphis Edmonton Mississippi Nile	Jordan Nile Edmonton Cairo Missouri	Houston Houston Birmingham Pittsburgh Astros Chevrolet Harvey	bridge bridges crossing	e eer ele y een c er ein
Layer 33_0	only first last most third main second subject	bridge Bridge bridges Bridge only	only last first key main same most exit	Marin only last San first key same most	Marin marin San Mar Marina mar California marine	only last first key subject third main final	only subject third main first last key fourth
Layer 33_1	planet interior cabin floors roots	coast coastline coastal Coast route beach Coastal	span public member library platform floating intervening deck	Marin member span underwater marine aquatic public	Jordan Nile Mississippi Memphis Cairo Missouri	own ly about Vader about somehow	TRGL ities
Layer 33_2	bridge bridge structure bridges brid Bridge	ship orbit aircraft sail vessel	Kuwait Nile Edmonton Saskatchewan Tulsa	Jordan Nile Edmonton Cairo Kuwait	Houston Birmingham Houston Chevrolet Carnegie Pittsburgh McMahon	wheels bridge miles snow sky busy icon	est e y er fully the . d

Table 5: The top three singular vectors of the detached Jacobian for the layer outputs from Qwen 3 14B for the sequence "The bridge out of Marin is the" with the prediction [[only]].