Complex-based Ligand-Binding Proteins Redesign by Equivariant Diffusion-based Generative Models

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Abstract

Proteins, serving as the fundamental architects of biological processes, interact with ligands to perform a myriad of functions essential for life. Designing functional ligand-binding proteins is pivotal for advancing drug development and enhancing therapeutic efficacy. In this study, we introduce ProteinReDiff, an efficient computational framework targeting the redesign of ligand-binding proteins. Using equivariant diffusion-based generative models, ProteinReDiff enables the creation of high-affinity ligand-binding proteins without the need for detailed structural information, leveraging instead the potential of initial protein sequences and ligand SMILES strings. Our evaluations across sequence diversity, structural preservation, and ligand binding affinity underscore ProteinReDiff's potential to advance computational drug discovery and protein engineering. We will release our data and source code upon acceptance.

1 Introduction

Proteins, often referred to as the molecular architects of life, play a critical role in virtually all biological processes. A significant portion of these functions involves interactions between proteins and ligands, underpinning the complex network of cellular activities. These interactions are not only pivotal for basic physiological processes, such as signal transduction and enzymatic catalysis, but also have broad implications in the development of therapeutic agents, diagnostic tools, and various biotechnological applications (Du et al., 2016; Wanat, 2020; Skolnick & Zhou, 2022). Despite the paramount importance of protein-ligand interactions, the majority of existing studies have primarily focused on protein-centric designs to optimize specific protein properties, such as stability, expression levels, and specificity (Listov et al., 2024; Lisanza et al., 2023; Dauparas et al., 2022; Yang et al., 2023a; Iqbal et al., 2022). This prevalent approach, despite leading to numerous advancements, does not fully exploit the synergistic potential of optimizing both proteins and ligands for redesigning ligand-binding proteins. By embracing an integrated design approach, it becomes feasible to refine control over binding affinity and specificity, leading to applications such as tailored therapeutics with reduced side effects, highly sensitive diagnostic tools, efficient biocatalysis, targeted drug delivery systems, and sustainable bioremediation solutions (Yang & Lai, 2017; Ebrahimi & Samanta, 2023; Ruscito & DeRosa, 2016), thus illustrating the transformative impact of redesigning ligand-binding proteins across various fields.

Traditional methods for designing ligand-binding proteins have relied heavily on experimental techniques, characterized by systematic but often inefficient trial-and-error processes (Creutznacher et al., 2022; Munk et al., 2016; Tavares & van der Meer, 2021). These methods, while foundational, are time-consuming, resource-intensive, and sometimes fall short in precision and efficiency. The emergence of computational design has marked a transformative shift, offering new pathways to accelerate the design process and gain deeper insights into the molecular basis of protein-ligand interactions. However, even with the advancements in computational approaches, significant challenges remain. Many existing models demand extensive structural information, such as protein crystal structures and specific binding pocket data, limiting their applicability, especially in urgent scenarios like the emergence of novel diseases (Polizzi & DeGrado, 2020; Stärk et al., 2023; Dauparas et al., 2023). For instance, during the outbreak of a new disease like COVID-19, the spike proteins of the virus may not have well-characterized binding sites, delaying the development

of effective drugs (Lv et al., 2020; Schaub et al., 2021). Furthermore, the complexity of binding mechanisms, including allosteric effects and cryptic pockets, adds another layer of difficulty (Agajanian et al., 2023; Oleinikovas et al., 2016). Specifically, many proteins do not exhibit clear binding pockets until ligands are in close vicinity, necessitating extensive simulations to reveal potential binding interfaces (Meller et al., 2023; Oleinikovas et al., 2016). While molecular dynamics simulations offer detailed atomistic insights into binding mechanisms, they often prove inadequate for designing high-throughput sequences due to high computational cost (Barros et al., 2019; Yang & Lai, 2017). This complexity underscores the need for a drug design methodology that is agnostic to predefined binding pockets.

Our study addresses those identified challenges by introducing ProteinReDiff, a computational framework developed to enhance the process of redesigning ligand-binding proteins. Originating from the foundational concepts of the Equivariant Diffusion-Based Generative Model for Protein-Ligand Complexes (DPL) (Nakata et al., 2023), ProteinReDiff incorporates key improvements inspired by the representation learning modules from the AlphaFold2 (AF2) architecture (Jumper et al., 2021). Specifically, we integrate the Outer Product Update (adapted from outer product mean of AF2), Single Representation Attention (adapted from MSA row attention module), and Triangle Multiplicative Update modules into our Residual Feature Update procedure. These modules collectively enhance the framework's ability to capture intricate protein-ligand interactions, improve the fidelity of binding affinity predictions, and enable more precise redesigns of ligand-binding proteins.

The framework integrates the generation of diverse protein sequences with blind docking capabilities. Starting with a selected protein-ligand pair, our approach stochastically masks amino acids and equivariantly denoises the diffusion model to capture the joint distribution of ligand and protein complex conformations. Another key feature of our method is blind docking, which predicts how the redesigned protein interacts with its ligand without the need for predefined binding site information, while relying solely on initial protein sequences and ligand SMILES strings (Weininger, 1988). This streamlined approach significantly reduces reliance on detailed structural data, thus expanding the scope for sequence-based exploration of protein-ligand interactions.

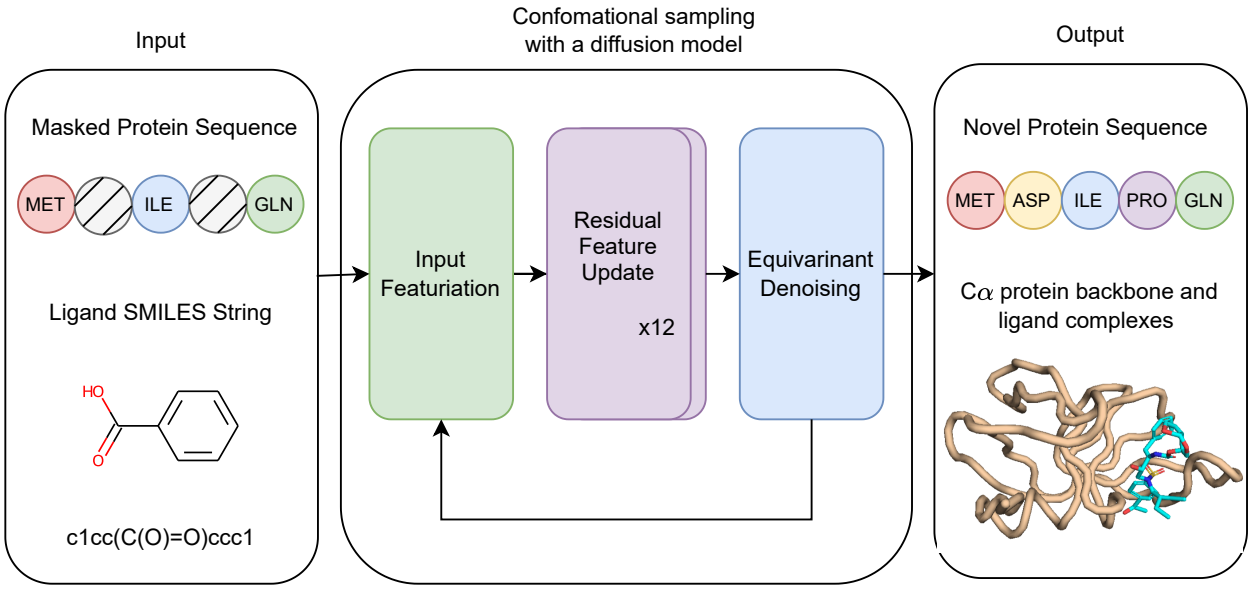

Figure 1: Overview of the proposed framework. The process begins with utilizing a protein amino acid sequence and a ligand SMILES string as inputs. The conformational sampling process includes iteratively applying input featurization, updating residual features, and denoising equivariantly, ultimately yielding novel protein sequences alongside their corresponding $C\alpha$ protein backbone and ligand complexes.

In summary, the contributions of our paper are outlined as follows:

- We introduce ProteinReDiff, an efficient computational framework for ligand-binding protein redesign, rooted in equivariant diffusion-based generative models. Our innovation lies in integrating AF2's representational learning modules to enhance the framework's ability to capture intricate protein-ligand interactions.
- Our framework enables the design of high-affinity ligand-binding proteins without reliance on detailed structural information, relying solely on initial protein sequences and ligand SMILES strings.
- We comprehensively evaluate our model's outcomes across multiple design aspects, including sequence diversity, structure preservation, and ligand binding affinity, ensuring a holistic assessment of its effectiveness and applicability in various contexts.

2 Related work

2.1 Traditional approaches in protein design

Protein design has historically hinged on computational and experimental strategies that paved the way for modern advancements in the field. These foundational methodologies emphasized the intricate balance between understanding protein structure and engineering novel functionalities, albeit with inherent limitations in scalability and precision. Key traditional approaches include:

- **Rational Design** Korendovych (2018); Song et al. (2023); Alley et al. (2019) focused on introducing specific mutations into proteins based on known structural and functional insights. This method required an in-depth understanding of the target protein structures and how changes might impact its function.
- **Directed Evolution** Arnold & Volkov (1999); Wang & Zhao (2016); Guntas et al. (2005); Waltenspühl et al. (2021) mimicked natural selection in the laboratory, evolving proteins towards desired traits through iterative rounds of mutation and selection. Despite its effectiveness in discovering functional proteins, the process was often labor-intensive and time-consuming.

These traditional methods have been instrumental in advancing our understanding and capability in protein design. However, their limitations in terms of efficiency, specificity, and the broad applicability of findings highlighted the need for more versatile and scalable approaches. As the field progressed, the integration of computational power and biological understanding opened new avenues for innovation in protein design, leading to the exploration and adoption of more advanced methodologies.

2.2 Deep generative models in protein design

Since their inception, deep generative models have significantly advanced fields like computer vision (CV) (Raut & Singh, 2024) and natural language processing (NLP) (Iqbal & Qureshi, 2022), sparking interest in their application to protein design. This enthusiasm has led to numerous studies that harness these models for innovating within the protein design area. Among these, certain types of deep generative models have distinguished themselves through their effectiveness and the promising results they have achieved, including:

- **Variational Autoencoders (VAEs)** are harnessed for their ability to learn rich representations of protein sequences, enabling the generation of novel sequences through manipulation in the latent space Lyu et al. (2023); Greener et al. (2018); Brookes et al. (2019).
- **Autoregressive models** predict the probability of each amino acid in a sequential manner, facilitating the generation of coherent and functionally plausible protein sequences Trinquier et al. (2021); Fannjiang et al. (2022).
- **Generative Adversarial Networks (GANs)** employ two networks that work in tandem to produce protein sequences indistinguishable from real ones, enhancing the realism and diversity of generated designs. Kucera et al. (2022); Anand & Huang (2018).

- **Diffusion models** represent a step forward by gradually transforming noise into structured data, simulating the complex process of folding sequences into functional proteins Gruver et al. (2023); Watson et al. (2023); Wu et al. (2022a); Fu et al. (2023).

However, the majority of these studies have focused on protein-centric designs, with a noticeable gap in research that integrates both proteins and ligands for the purpose of redesigning ligand-binding proteins. Such integration is crucial for a holistic understanding of the intricate dynamics between protein structures and their ligands, a domain that remains underexplored.

2.3 Current approaches in ligand-binding protein redesign

Contemporary computational methodologies Polizzi & DeGrado (2020); Stärk et al. (2023); Dauparas et al. (2023) for designing proteins that target specific surfaces predominantly draw upon structural insights from native complexes, emphasizing the critical role of fine-tuning side-chain interactions (Dauparas et al., 2023; Zheng et al., 2023) and optimizing backbone configurations (Polizzi & DeGrado, 2020; Watson et al., 2023; Yang et al., 2022) for optimal binding affinity. Notably, these strategies often begin with the generation of protein backbones, utilizing inverse folding techniques Yang et al. (2023a); Hsu et al. (2022); Dauparas et al. (2022); Yang et al. (2022) thereafter to identify sequences capable of folding into these pre-designed structures. This approach marks a significant paradigm shift by prioritizing structural prediction ahead of sequence identification, aiming to produce proteins that not only fit the desired conformations for potential ligand interactions but also navigate around the challenge of undefined binding sites. Despite the advantages, including the potential of computational docking to create binders via manipulation of antibody scaffolds and varied loop geometries (Lyu et al., 2023; Bennett et al., 2024; Chungyoun & Gray, 2023), a notable challenge persists in validating these binding modes with high-resolution structural evidence. Additionally, the traditional focus on a limited array of hotspot residues for guiding protein scaffold placement often limits the exploration of possible interaction modes, especially in cases where target proteins lack clear pockets or clefts for ligand accommodation (Meller et al., 2023; Gagliardi & Rocchia, 2023). In contrast, our approach breaks away from the heavy reliance on detailed structural information that characterizes conventional methodologies. We introduce a more flexible path for designing ligand-binding proteins by utilizing solely initial protein sequences and ligand SMILES strings. This marks a shift in design perspective in the current protein-design development, facilitating the effective redesign of ligand-binding proteins.

3 Background

3.1 Protein language models (PLMs)

Protein Language Models (PLMs) harness the power of natural language processing (NLP) to unravel the intricate latency embedded within protein sequences. By analogizing amino acid sequences to human language sentences, PLMs unlock profound insights into protein functions, interactions, and evolutionary trajectories (Yang et al., 2023b). These models leverage advanced text processing techniques to predict structural, functional, and interactional properties of proteins based solely on their amino acid sequences (Brandes et al., 2022; Elnaggar et al., 2022; Rives et al., 2021; Lin et al., 2023a; Nguyen & Hy, 2023; Ngo & Hy, 2024). Their adoption in protein design has catalyzed significant progress, with studies leveraging PLMs to translate protein sequence data (Madani et al., 2023; Ruffolo & Madani, 2024; Min et al., 2024; Zheng et al., 2023; Tran & Hy, 2023; Ngo & Hy, 2024) into actionable insights, thus guiding the precise engineering of proteins with targeted functional attributes.

Mathematically, a PLM can be represented as a function F that maps a sequence of amino acids $S = [s_1, s_2, \ldots, s_n]$, where s_i denotes the i-th amino acid in the sequence, to a high-dimensional feature space that encapsulates the protein's structural and functional properties:

$$X = F(S), \quad X \in R^d, \tag{1}$$

where X represents the continuous representation or embedding derived from the sequence S and d represents the dimensionality of the embedding space, determined by the PLM's architecture. This embedding

captures the complex dependencies and patterns underlying the protein's structural information and biological functionality. Through training on known sequences and structures, PLMs discern the "grammar" governing protein folding and function, facilitating accurate predictions.

We employ the ESM-2 model (Lin et al., 2023a), a state-of-the-art protein language model with 650 million parameters, pre-trained on nearly 65 million unique protein sequences from the UniRef (Suzek et al., 2014) database, to feature initial masked protein sequences. ESM-2 enriches the latent representation of protein sequences, bypassing the need for conventional multiple sequence alignment (MSA) methods. By incorporating structural and evolutionary information from input sequences, ESM-2 enables us to unravel interaction patterns across protein families for effective ligand targeting. This understanding is crucial for designing and optimizing ligand-binding proteins.

3.2 Equivariant diffusion-based generative models

We utilize a generative model driven by equivariant diffusion principles, drawing from the foundations laid by Variational Diffusion Models (Kingma et al., 2023) and E(3) Equivariant Diffusion Models (Hoogeboom et al., 2022).

3.2.1 The diffusion procedure

First, we employ a diffusion procedure that is equivariant with respect to the coordinates of atoms x, alongside a series of progressively more perturbed versions of x, known as latent variables z_t, with t varying from 0 to 1. To maintain translational invariance within the distributions, we opt for distributions on a linear subspace that anchors the centroid of the molecular structure at the origin, and designate N_x as a Gaussian distribution within this specific subspace. The conditional distribution of the latent variable z_t given x, for any given t in the interval [0, 1], is defined as

$$q(z_t|x) = N_x(\alpha_t x, \sigma_t^2 I), \tag{2}$$

where α_t and σ_t^2 represent strictly positive scalar functions of t, dictating the extent of signal preservation versus noise introduction, respectively. We implement a variance-conserving mechanism where $\alpha_t = 1 - \sigma_t^2$ and posit that α_t smoothly and monotonically decreases with t, ensuring $\alpha_0 \approx 1$ and $\alpha_1 \approx 0$. Given the Markov property of this diffusion process, it can be described via transition distributions as

$$q(z_t|z_s) = N_x(\alpha_{t|s} z_s, \sigma_{t|s}^2 I), \tag{3}$$

for any $t > s$, where $\alpha_{t|s} = \alpha_t/\alpha_s$ and $\sigma_{t|s}^2 = \sigma_t^2 - \alpha_t^2\sigma_s^2$. The Gaussian posterior of these transitions, conditional on x, can be derived using Bayes' theorem:

$$q(z_s|z_t, x) = N_x(\mu_{t\to s}(z_t, x), \sigma_{t\to s}^2 I), \tag{4}$$

with

$$\mu_{t\to s} = \frac{\alpha_s \sigma_{t|s}^2}{\alpha_{t|s}\sigma_s^2} z_t + \frac{\sigma_s^2 \sigma_t^2}{\sigma_{t|s}^2} x, \quad \sigma_{t\to s}^2 = \frac{\sigma_t^2 \sigma_s^2}{\sigma_{t|s}^2}. \tag{5}$$

3.2.2 The generative denoising process

The construction of the generative model inversely mirrors the diffusion process, generating a reverse temporal sequence of latent variables z_t from $t = 1$ back to $t = 0$. By dividing time into T equal intervals, the generative framework can be described as:

$$p_\theta(x) = \int_z p(z_1)p(x|z_0) \prod_{i=1}^{T} p_\theta(z_{t_i}|z_{t_{i-1}}), \tag{6}$$

with $s(i) = (i-1)/T$ and $t(i) = i/T$. Leveraging the variance-conserving nature and the premise that $\alpha_1 \approx 0$, we posit $q(z_1) = N_x(0, I)$, hence treating the initial distribution of z_1 as a standard Gaussian:

$$p(z_1) = N_x(0, I). \tag{7}$$

Furthermore, under the variance-conserving framework and considering $\alpha_0 \approx 1$, the distribution $q(z_0|x)$ is modeled as narrowly concentrated, allowing for the approximation of $p_{data}(x)$ as uniform across this concentration. This yields:

$$q(z_0|x) = \frac{q(z_0|x)p_{\text{data}}(x)}{\int_{\tilde{x}} q(z_0|\tilde{x})p_{\text{data}}(\tilde{x})} \approx \frac{q(z_0|x)}{\int_{\tilde{x}} q(z_0|\tilde{x})} = \mathcal{N}_x(x|z_0/\alpha_0, \sigma_0^2/\alpha_0^2 I). \tag{8}$$

Accordingly, we approximate $q(x|z_0)$ through:

$$p(x|z_0) = \mathcal{N}_x(x|z_0/\alpha_0, \sigma_0^2/\alpha_0^2 I). \tag{9}$$

The generative model's conditional distributions are then formulated as:

$$p_\theta(z_s|z_t) = q(z_s|z_t, x = \hat{x}_\theta(z_t; t)), \tag{10}$$

which mirrors $q(z_s|z_t, x)$ but substitutes the actual coordinates x with the estimates from a temporal denoising model $\hat{x}_\theta(z_t; t)$, which employs a neural network parameterized by θ to predict x from its noisier version z_t. This denoising model's framework, predicated on noise prediction $\hat{\epsilon}_\theta(z_t; t)$, is articulated as:

$$\hat{x}_\theta(z_t; t) = \frac{(z_t - \sigma_t \hat{\epsilon}_\theta(z_t; t))}{\alpha_t}. \tag{11}$$

Consequently, the transition mean $\mu_{t\to s}(z_t, \hat{x}_\theta(z_t; t))$ is determined by:

$$\mu_{t\to s}(z_t, \hat{x}_\theta(z_t; t)) = \frac{\alpha_s \sigma_{t|s}^2}{\alpha_{t|s}\sigma_s^2} z_t + \frac{\alpha_s \sigma_t^2}{\sigma_{t|s}^2} x = \frac{1}{\alpha_{t|s}} z_t - \frac{\sigma_{t|s}^2}{\alpha_{t|s}\sigma_t} \hat{\epsilon}_\theta(z_t; t). \tag{12}$$

4 Method

In this section, we detail the methodology employed in our noise prediction model, which is depicted in Figure 1 and consists of three main procedures: (1) input featurization, (2) residual feature update, and (3) equivariant denoising. Through these steps, we transform raw protein and ligand data into structured representations, iteratively refine their features, and leverage denoising techniques inherent in the diffusion model to improve sampling quality.

4.1 Input featurization

We develop both single and pair representations from protein sequences and ligand SMILES string (Figure 2). For proteins, we initially applied stochastic masking to segments of the amino acid sequences. The protein representation is attained through the normalization and linear mapping of the output from the final layer of the ESM-2 model, which is subsequently combined with the amino acid and masked token embeddings. Additionally, for pair representations of proteins, we leveraged pairwise relative positional encoding techniques, drawing from established methodologies (Jumper et al., 2021). For ligand representations, we employed a comprehensive feature embedding approach, capturing atomic and bond properties such as atomic number, chirality, connectivity, formal charge, hydrogen attachment count, radical electron count, hybridization status, aromaticity, and ring presence for atoms; and bond type, stereochemistry, and conjugation status for bonds. These representations are subsequently merged, incorporating radial basis function embeddings of atomic distances and sinusoidal embeddings of diffusion times. Together, these steps culminate in the formation of preliminary complex representations, laying the foundation for our computational analyses.

4.2 Residual feature update procedure

Our approach deviates significantly from the residual feature update procedure employed in the original DPL model (Nakata et al., 2023). While the DPL model relied on Alphafold2's Triangular Multiplicative Update for updating single and pair representations, where these representations mutually influence each other, our

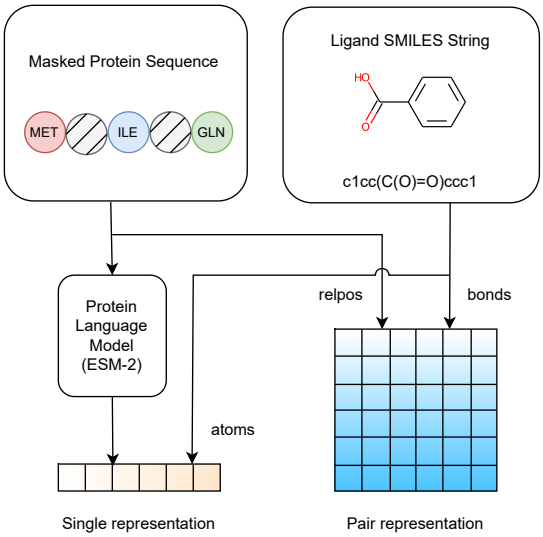

Figure 2: Overview of the input featurization procedure of the model.

objective is to optimize this procedure for greater efficiency. Specifically, we incorporate enhancements such as the Outer Product Update and Single Representation Attention to formulate sequence representational hypotheses of protein structures and to model suitable motifs for binding target ligands specifically. These modules, integral to Evoformer, the sequence-based module of AF2, play a crucial role in extracting essential connections among internal motifs that serve structural functions (i.e., ligand binding) when structural information is not explicitly provided during training. Importantly, we adapt and tailor these modules to fit within our model architecture, ensuring their effectiveness in capturing the intricate interplay between proteins and ligands.

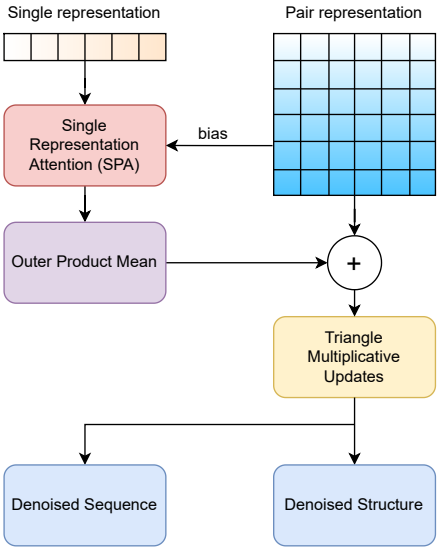

Figure 3: Overview of the residual feature update procedure of the model.

4.2.1 Single representation attention module

The Single Representation Attention (SPA) module, derived from the Alphafold2 model's MSA row attention with pair bias, accounts for long-range interactions among residues and ligand atoms within a single protein-ligand embedding vector. In essence, the attention mechanism assigns importance to those involved

in complex-based folding to denoise the equivariant loss (4.3) in a self-supervised manner. While the original Alphafold2 MSA row attention mechanism processes input for a single sequence, the SPA module is designed to incorporate representations from multiple protein-ligand complexes concurrently. Specifically, the pair bias component of the SPA attention module captures dependencies between proteins and ligands, which was shown to fit the attention score better than the regular self-attention model without bias terms (Xu et al., 2023). By considering both the single representation vector (which encodes the protein/ligand sequential representation) and the pairwise representation vector (which encodes protein-protein and protein-ligand interactions), this cross-attention mechanism exchanges information between pairwise and single representation to effectively preserves internal motifs, as evidenced by contact overlap metrics (Rao et al., 2021; Yang et al., 2023b). As transformer architecture is widely used for predicting protein functions (Buton et al., 2023), we observed similar efficacy to our binding affinity prediction in section Results 5.2.6 and Appendix A. For a detailed description of the computational steps implemented in this module, refer to Algorithm 1.

Algorithm 1 Single Representation Attention pseudocode

Input: Single representation vector m_{si}, pair representation vector z_{sij} of the i-th sequence in the set of sequences s, C = 65, $N_{head} = 4$.

Output: Updated single representation vector $\tilde{m}_{si}$ with the dimension of C_m.

1: $m_{si} \leftarrow \text{LayerNorm}(m_{si})$
2: $q^h_{si}, k^h_{si}, v^h_{si} \leftarrow \text{LinearNoBias}(m_{si}) \quad q^h_{si}, k^h_{si}, v^h_{si} \in \mathbb{R}^C, h \in \{1, \ldots, N_{\text{head}}\}$
3: $b^h_{sij} \leftarrow \text{LinearNoBias}(\text{LayerNorm}(z_{sij}))$
4: $g^h_{si} \leftarrow \text{sigmoid}(\text{Linear}(m_{si})) \quad g^h_{si} \in \mathbb{R}^C$
5: $a^h_{sij} \leftarrow \text{softmax}_j\left(\frac{1}{\sqrt{C}} q^h_{si} {k^h_{sj}}^T + b^h_{sij}\right)$
6: $o^h_{si} \leftarrow g^h_{si} \odot \sum_j a^h_{sij} v^h_{sj}$
7: $\tilde{m}_{si} \leftarrow \text{Linear}(\text{concat}_h(o^h_{si})) \quad \tilde{m}_{si} \in \mathbb{R}^{C_m}$
8: return$\{\tilde{m}_{si}\}$

4.2.2 Outer product update

Since the SPA encodings have a shape (s, r, c_m) and the pair representation has a shape (s, r, r, c_z), the outer product layer merges insights by reshaping SPA encodings into pair representations. This module leverages evolutionary cues to generate plausible structural hypotheses for pair representations (Ju et al., 2021). It first calculates the outer product of the SPA embeddings of protein-ligand pairs, then aggregates the outer products to yield a measure of co-evolution between every residue pair (Yang et al., 2023b). Analogous to Tensor Product Representations (TPR) in NLP, the outer product is akin to the filler-and-role binding relationship, where each entity (i.e. amino acid residue) on a sequence is attached to a rich functional embedding based on its relationship to one another (Huang et al., 2018; Smolensky, 1990; Huang et al., 2019).

This process integrates correlated information of residues i and j of a sequence s, resulting in the intermediate Kronecker product tensors (.i.e. role embeddings in NLP) (Xu et al., 2023; Schlag & Schmidhuber, 2018; Chen et al., 2021). Subsequently, an affine transformation projects those representations to hypotheses concerning the relative positions of residues i and j under biophysical constraints. Our implementation adapts the outer product without computing the mean to maintain the pair representations of multiple protein-ligand complexes. For a detailed description of the computational steps implemented in this module, refer to Algorithm 2.

Algorithm 2 Outer product update pseudocode

Input: Single representation vector m_{si} of the i-th sequence in the set of sequences s, $C = 32$.
Output: Pair representation vector z_{sij} with the dimension of $s \times C_z$.

1: $m_{si} \leftarrow \text{LayerNorm}(m_{si})$
2: $a_{si}, b_{si} \leftarrow \text{Linear}(m_{si}) \quad a_{si}, b_{si} \in \mathbb{R}^C$
3: $o_{sij} \leftarrow \text{flatten}(a_{si} \otimes b_{si}) \quad o_{sij} \in \mathbb{R}^{C \times C}$
4: $z_{sij} \leftarrow \text{Linear}(o_{sij}) \quad z_{sij} \in \mathbb{R}^{s \times C_z}$
5: return$\{z_{sij}\}$

4.2.3 Triangle multiplicative updates

After refining the pair representation, our model interprets the primary protein-ligand structure using principles from graph theory, treating each residue as a distinct entity interconnected through the pairwise matrix. These connections are then refined through triangular multiplicative updates to account for physical and geometric constraints, such as triangular inequality. While the SPA weights the importance of residues, the triangular multiplicative update acts as other transformer-based layers where any two edges affect the third one to enforce triangle equivariance (Lin & AlQuraishi, 2023; Yang et al., 2023b). The starting and ending nodes propagate information in and out of neighbors in similar fashion as the message-passing framework (Xu et al., 2023). These mechanisms enable the model to generate more accurate representations of protein-ligand complexes, leading to improved predictive performance in predicting binding affinities and structural characteristics.

4.3 Equivariant denoising

During the equivariant denoising process, the final pair representation undergoes symmetrization and is then transformed using a multi-layer perceptron (MLP) into a weight matrix W. This matrix is utilized to compute the weighted sum of all relative differences in 3D space for each atom, as shown in the equation (Nakata et al., 2023):

$$\hat{\epsilon}_i(z) = \sum_j W_{ij}(z) \cdot \frac{(z_i - z_j)}{\|z_i - z_j\|}. \tag{13}$$

Afterward, the centroid is subtracted from this computation, resulting in the output of our noise prediction model $\hat{\epsilon}$. Additionally, it's important to note that the described model maintains SE(3)-equivariance, meaning that:

$$\hat{\epsilon}_i(\mathbf{R}z + \mathbf{t}) = \sum_j \frac{W_{ij}(\mathbf{R}z + \mathbf{t})}{\|(\mathbf{R}z_i + \mathbf{t}) - (\mathbf{R}z_j + \mathbf{t})\|} \cdot ((\mathbf{R}z_i + \mathbf{t}) - (\mathbf{R}z_j + \mathbf{t})) \tag{14}$$

$$= \mathbf{R} \sum_j \frac{W_{ij}(\mathbf{R}z + \mathbf{t})}{\|z_i - z_j\|} \cdot (z_i - z_j) \tag{15}$$

$$= \mathbf{R} \sum_j \frac{W_{ij}(z)}{\|z_i - z_j\|} \cdot (z_i - z_j) \tag{16}$$

$$= \mathbf{R}\hat{\epsilon}_i(z) \tag{17}$$

for any rotation $\mathbf{R}$ and translation $\mathbf{t}$. This property is derived from the fact that the final representation, and hence the weight matrix W, depends solely on atom distances that are invariant to rotation and translation.

5 Experiments

5.1 Training process

5.1.1 Materials

Our training strategy harnesses a meticulously curated dataset encompassing a broad range of protein structures, including both ligand-bound (holo) and ligand-free (apo) forms, sourced from two key repositories: PDBBind v2020 (Wang et al., 2004) and CATH 4.2 (Sillitoe et al., 2018). PDBBind v2020 offers a diverse collection of protein-ligand complexes, while CATH 4.2 provides a substantial repository of protein structures. Each dataset was selected for its unique contributions to our understanding of protein-ligand interactions and structural diversity. This strategic selection of datasets ensures our model is exposed to a wide and varied spectrum of protein-ligand interactions and structural configurations, enabling a comprehensive evaluation against diverse inverse folding benchmarks. By training on both holo and apo structures, our approach not only aims to imbue the model with a robust understanding of protein-ligand dynamics but also equips it to adeptly navigate the complexities of unseen protein-ligand interaction scenarios. To ensure robust model training and evaluation, we employ careful data partitioning techniques. The dataset is divided into distinct subsets, including training, validation, and test sets. Table 1 provides an overview of the partitioning details, facilitating a clear understanding of the distribution of samples across different subsets of the dataset.

- **PDBBind v2020**: For consistency and comparability with previous studies, we adhered closely to the test/training/validation split settings outlined in established literature, specifically following the configurations defined in the respective sources for the PDBBind v2020 datasets (Koh et al., 2023).

- **CATH 4.2**: In our approach, we deliberately focused on proteins with fewer than 400 amino acids from the CATH 4.2 database. This selective criterion was chosen to prioritize smaller proteins, which often represent more druggable targets of interest in drug discovery and development endeavors. During both the training and validation phases, SMILES strings of CATH 4.2 proteins were represented as asterisks (masked tokens) to denote missing ligands. Notably, CATH 4.2 was excluded from the test set due to the absence of corresponding ligands required for evaluating protein-ligand interactions.

Table 1: Data Partitioning Overview (Unit: number of samples)

Dataset	**Training**	**Validation**	**Test**
PDBBind v2020	9430	552	207
CATH 4.2	15261	939	-

5.1.2 Loss functions

Previous models typically denoise in only one domain, such as ProteinMPNN, LigandMPNN, and MIF in sequence space, and DPL in structural space. This limitation restricts their ability to fully capture the intricate interactions between proteins and ligands. To address this, we have introduced significant modifications to the loss function to better suit the task of ligand-binding protein redesign. By tailoring the loss function to integrate both sequence and structural spaces, our approach effectively addresses the unique challenges of protein-ligand interactions. This dual-domain denoising strategy sets our work apart from standard diffusion models and enhances the model's ability to generate high-affinity ligand-binding proteins while maintaining structural fidelity. Specifically, the optimization of our model for ligand-binding protein redesign is governed by a composite loss function L, formulated as follows:

$$L = L_{\mathrm{WS}} + L_{\mathrm{KL}} + L_{\mathrm{CE}}, \tag{18}$$

Weighted sum of relative differences ($L_{\mathbf{WS}}$) This component ensures the model's sensitivity to the directional influence between atoms, supporting the accurate prediction of the denoised structure while maintaining physical symmetries. It is crucial for the equivariant denoising step, enabling accurate noise prediction for atoms in the protein-ligand complex. The loss is defined as:

$$L_{\text{WS}} = \sum_{t=1}^{T} \|\epsilon - \hat{\epsilon}_\theta(z;t)\| \,, \tag{19}$$

where T is the total number of time steps in the diffusion process, ϵ is the Gaussian noise vector $\mathcal{N}(\mathbf{0}, \mathbf{I})$ and $\hat{\epsilon}_\theta(z;t)$ is the loss prediction at time step t parameterized by an MLP in Section 4.3.

Kullback-Leibler divergence ($L_{\mathbf{KL}}$) (Joyce, 2011) This component quantifies the divergence between the model's predictions and actual sequence data at timestep $t-1$, playing a pivotal role in the denoising process. Defined as $KL(x_{\text{pred_t-1}}, seq_{\text{t-1}})$, it contrasts the predicted distribution, $x_{\text{pred_t-1}}$, against the true sequence distribution, $seq_{\text{t-1}}$, leveraging the diffusion process's γ parameter for temporal adjustment. This loss is also applied in the Protein Generator (Lisanza et al., 2023) model to ensure the model's predictions progressively align with actual data distributions, enhancing the accuracy of sequence and structure generation by minimizing the expected divergence.

Cross-entropy loss ($L_{\mathbf{CE}}$) This loss function is crucial for the accurate prediction of protein sequences, aligning them with the ground truth through effective classification. It denoises each amino acid from masked latent embedding to a specific class, leveraging categorical cross-entropy to rigorously penalize discrepancies between the model's predicted probability distributions and the actual distributions for each amino acid type.

5.1.3 Training performance

Throughout the training phase, we meticulously observed the model's performance, paying close attention to the dynamics between training and validation losses, as demonstrated in Figure 4. While the training loss consistently diminished, indicating effective learning, the validation loss exhibited more variability. Despite these fluctuations, the validation loss showed an overall downward trend, suggesting that the model is improving its generalization capabilities over time. The general alignment between the downward trends of training and validation losses indicates that the model is learning effectively without significant overfitting.

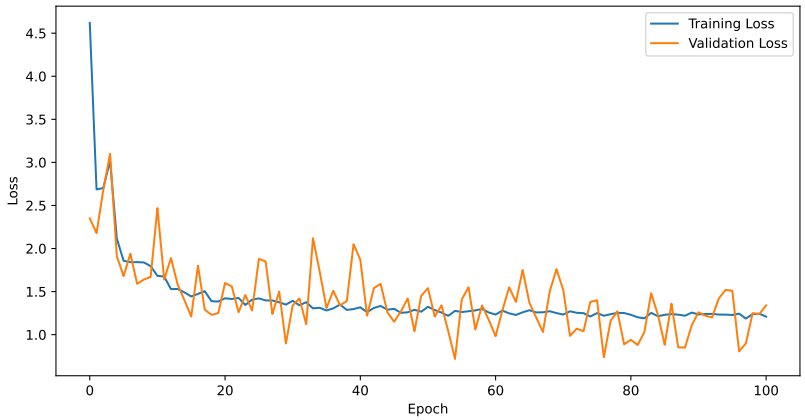

Figure 4: Training history chart of ProteinReDiff, showcasing the evolution of training and validation losses over epochs.

5.2 Evaluation process

5.2.1 Ligand binding affinity (LBA)

Ligand binding affinity is a fundamental measure that quantifies the strength of the interaction between a protein and a ligand. This metric is crucial as it directly influences the effectiveness and specificity of potential therapeutic agents; higher affinity often translates to increased drug efficacy and lower chances of side effects (Sawada et al., 2024). Within this context, ProteinReDiff is evaluated on its ability to generate protein sequences for significantly improved binding affinity with specific ligands. We utilize a docking score-based approach for this assessment, where the docking score serves as a quantitative indicator of affinity. Expressed in kcal/mol, these scores inversely relate to binding strength — lower scores denote stronger, more desirable binding interactions.

5.2.2 Sequence diversity

Sequence diversity is crucial for exploring protein's functional space (Ziegler et al., 2023). It reflects the capacity of our model, ProteinReDiff, to traverse the vast landscape of protein sequences and generate a wide array of variations. To quantitatively assess this diversity, we utilize the average edit distance (Levenshtein distance) (Miller et al., 2009) between all pairs of sequences generated by the model. This metric offers a nuanced measure of variability, surpassing traditional metrics that may overlook subtle yet significant differences. The diversity score is calculated using the formula:

$$\text{Diversity Score} = \frac{1}{\binom{n}{2}} \sum_{i=1}^{n-1} \sum_{j=i+1}^{n} d(S_i, S_j), \tag{20}$$

where $d(S_i, S_j)$ represents the edit distance between any two sequences S_i and S_j. This calculation provides an empirical gauge of ProteinReDiff's ability to enrich the protein sequence space with novel and diverse sequences, underlining the practical variance introduced by our model.

5.2.3 Structure preservation

Structural preservation is paramount in the redesign of proteins, ensuring that essential functional and structural characteristics are maintained post-modification. To effectively measure structural preservation between the original and redesigned proteins, three key metrics: the Template Modeling Score (TM Score) (Zhang & Skolnick, 2004), the Root Mean Square Deviation (RMSD) (Laskowski & de Beer, 2014), and the Contact Overlap (CO) (Bastolla et al., 2023). These two metrics collectively provide a comprehensive assessment of structural integrity and similarity, essential for evaluating the success of our protein redesign efforts.

The Root Mean Square Deviation (RMSD) is a measure used to quantify the distance between two sets of points. In the context of protein structures, these points are the positions of the atoms in the protein. The RMSD is given by the formula:

$$\text{RMSD}(\mathbf{p}, \mathbf{p}') = \min_{(R,t) \in \text{SO}(3) \times \mathbb{R}_3} \left[\frac{1}{N} \sum_{i=1}^{N} \|p_i - (Rp'_i + t)\|_2^2 \right]^{1/2}, \tag{21}$$

where $\mathbf{p} = (x_i, y_i, z_i)_{i=1}^N$ and $\mathbf{p}' = (x'_i, y'_i, z'i)_{i=1}^N$ denote two sequences of N 3D coordinates representing the atomic positions in the original and redesigned proteins, respectively. This formula calculates the minimum root mean square of distances between corresponding atoms, after optimal superposition, which involves finding the best-fit rotation R and translation t that aligns the two sets of points. A lower RMSD value indicates a higher degree of structural similarity, making it a direct measure of the extent to which structural deviation has been minimized. Achieving a low RMSD is desirable, as it signifies that the redesign process has successfully preserved the core structural configuration of the original protein.

TM Score provides a normalized measure of structural similarity between protein configurations, which is less sensitive to local variations and more reflective of the overall topology. The TM Score is defined as follows:

$$\text{TM Score}(\mathbf{p}, \mathbf{p}') = \max_{(R,t)\in \text{SO}(3)\times\mathbb{R}_3} \left[\frac{1}{1 + \frac{1}{N}\sum_{i=1}^{N} \frac{\|p_i - (Rp'_i + t)\|_2^2}{d_0^2}} \right], \tag{22}$$

where d_0 is a scale parameter typically chosen based on the size of the proteins. The closer the TM Score is to 1, the more similar the structures are, indicating global structural alignment.

Contact Overlap (CO) provides a complementary perspective to RMSD and TM Score by focusing on the preservation of local structural motifs rather than overall geometric similarity. Several studies show that having high CO indicates protein's residue pairs having co-evolutionary signals (Cheng et al., 2019; Bastolla et al., 2023) and performing related functions (Iyer et al., 2020). CO quantitatively measures the conservation of inter-atomic contacts between the original and redesigned protein structures, which are crucial for the protein's structural integrity and functional capabilities. The metric is defined as:

$$\text{CO}(\mathbf{p}, \mathbf{p}') = \frac{|C \cap C'|}{|C \cup C'|}, \tag{23}$$

where $C = \{(i,j) : \|p_i - p_j\| < r_c, i \neq j\}$ and $C' = \{(i,j) : \|p'_i - p'_j\| < r_c, i \neq j\}$ represent the sets of contacts in the original and redesigned proteins, respectively. Here, p_i and p'_i are the positions of atoms in the original and redesigned proteins, and r_c is a predefined cutoff distance that determines when two atoms are considered to be in contact. A high CO score indicates that many of the original contacts are preserved in the redesigned structure, suggesting that the redesign maintains much of the original protein's structural network, which is crucial for its stability and function.

5.2.4 Ablation study

Efficiency of architecture and framework To further validate the effectiveness of the enhancements introduced in ProteinReDiff, we conducted experiments comparing two variants of our model: one incorporating our proposed enhancements and the original DPL model, which was initially designed to generate ensembles of complex structures rather than for targeted protein redesign. To adapt DPL for our purposes, sequence-based loss functions were added to align it with the specific requirements of ligand-binding protein redesign. These modifications allowed us to evaluate how well our enhancements improve upon the base model in terms of ligand binding affinity. This comparative assessment, as presented in Table 3, not only highlighted the added value of our improvements but also showcased the adaptability and potential of the original DPL framework when reconfigured for protein redesign tasks.

Impact of masking ratios We examined the impact of varying the percentage of masked amino acids on ProteinReDiff's efficacy. This investigation is key to understanding the optimal level of sequence modification needed to enhance ligand binding affinity and ensure sequence diversity as well as structural preservation. We adjusted the percentage of masked amino acids in the original sequences, observing the effects on performance metrics such as ligand binding affinity and structural integrity. This approach allowed us to determine how changes in the sequence masking strategy influence the model's redesign capabilities. The initial setup involved a minimal percentage of sequence masking, essential for the redesign process, gradually increasing to explore the model's flexibility and its ability to generate sequences with improved characteristics. The study aims to identify a balance that maximizes protein function enhancement while maintaining crucial structural and functional motifs. Findings will inform strategies for sequence modification, highlighting its significance in computational protein design.

5.2.5 Experimental setup

To evaluate ProteinReDiff, we employed Omegafold (Wu et al., 2022b) to predict the three-dimensional structures of all designed protein sequences. The choice of Omegafold over AF2 was favorable because Omegafold can more accurately fold proteins with low similarity to existing proteomes, making it suitable

for proteins lacking available ligand-binding conformations. Next, we utilized AutoDock Vina (Trott & Olson, 2010) to conduct docking simulations and evaluate the binding affinity between the redesigned proteins and their respective ligands based on the predicted 3D structures. To ensure fair comparisons and mitigate potential biases introduced by pre-docked structures, we aligned our redesigned protein structures with reference structures before docking. This approach is crucial, particularly because the use of pre-docked structures may favor certain conformations, leading to inaccurate evaluations. Additionally, to provide context for our results, we compared the binding scores of our redesigned proteins not only with those of the original proteins but also with proteins generated by other protein design models. Although these models may exhibit different sequence characteristics compared to those explicitly designed for ligand binding affinity, comparing their scores offers valuable insights. Such comparisons help elucidate the interplay between protein sequence and structure in determining ligand interactions, enriching the interpretation of our findings and advancing our understanding of protein-ligand interactions.

Benchmark Model Selection In selecting benchmark models for performance comparison, we focused on state-of-the-art approaches, particularly those relevant to protein design tasks. Traditionally, protein design has been primarily based on inverse folding, utilizing protein structure information. Our choices encompass a range of methodologies:

- MIF (Yang et al., 2022), MIF-ST (Yang et al., 2022), and ProteinMPNN (Dauparas et al., 2022) are notable for generating sequences with high identity and experimental significance, utilizing protein structure information.
- The Protein Generator (Lisanza et al., 2023), a representative of RosettaFold models (Watson et al., 2023), employs diffusion-based methods, making it an intriguing comparative candidate. The model also shares a similar loss function, L_{KL}, in sequence space with our model but diverges in modules and training procedures (i.e., stochastic masking).
- ESMIF (Hsu et al., 2022), belonging to the ESM model family (Lin et al., 2023b), stands as another competitive benchmark, emphasizing the generation of high-quality sequences.
- CARP, while lacking ligand information, shares similar protein input and output characteristics with our models, warranting inclusion for comparison.
- DPL (Nakata et al., 2023), originally geared towards protein-ligand complex generation, was adapted for our purposes by modifying loss functions and incorporating a sequence prediction module, given its alignment with our model architecture.
- LigandMPNN (Dauparas et al., 2023), resembling the most to our task in designing ligand-binding proteins, necessitates binding pocket information, unlike our model, which emphasizes a simplified yet effective approach for ligand-binding protein tasks.

Our model's design prioritizes simplicity in input while achieving effectiveness in output for ligand-binding protein tasks. For a comprehensive comparison of input-output dynamics across each model, please consult Table 2.

5.2.6 Results and discussion

Our comprehensive evaluation of ProteinReDiff, as detailed in Table 3 and visually represented in Figure 6, across the metrics of ligand binding affinity, sequence diversity, and structure preservation, has yielded insightful findings. These evaluations provide a clear depiction of the model's performance relative to established baselines and within its variations.

For ProteinReDiff, we aimed to capture the diverse conformations of ligand-binding proteins, recognizing that they can adopt multiple structural states. To assess these conformations, we employed alignment metrics such as TM score, RMSD, and contact overlap (CO). In Figure 5, we presented several instances where the contact overlap appeared to be maintained, yet the RMSD is large and TM score is low. This

Table 2: Comparison of protein design models based on input and output characteristics

Model	Input				Output		
	Protein Sequence	Protein Structure	Ligand SMILES	Binding Pocket	Protein Sequence	Protein Structure	Ligand Structure
CARP (Yang et al., 2023a)	✓	×	×	×	✓	×	×
ESMIF (Hsu et al., 2022)	×	✓	×	×	✓	×	×
MIF (Yang et al., 2022)	✓	✓	×	×	✓	×	×
MIF-ST (Yang et al., 2022)	✓	✓	×	×	✓	×	×
ProteinMPNN (Dauparas et al., 2022)	×	✓	×	×	✓	×	×
LigandMPNN (Dauparas et al., 2023)	×	✓	✓	✓	✓	✓	×
Protein Generator (Lisanza et al., 2023)	×	✓	×	×	✓	×	×
DPL (Nakata et al., 2023)	✓	×	✓	×	×	✓	✓
ProteinReDiff (Ours)	✓	×	✓	×	✓	✓	✓

discrepancy suggests that while global alignment metrics like TM score and RMSD may not adequately capture the domain shift within these complex ensembles, the preservation of local motifs, as indicated by contact overlap, remains crucial in our framework. This underscores the importance of capturing both global and local structural features for a comprehensive understanding of protein-ligand interactions.

A pivotal observation from our study is ProteinReDiff's unparalleled ability to enhance ligand binding affinity, particularly pronounced at a 15% masking ratio. This configuration not only eclipses the performance of Inverse Folding (IF) models and the original DPL framework but also crucially exceeds the binding efficiencies of the original protein designs. By incorporating advanced computational modules from AlphaFold2, ProteinReDiff has successfully represented the complex interplay between proteins and ligands, demonstrating its effectiveness in enhancing ligand-binding affinity beyond the capabilities of the original DPL model. While other masking ratios within ProteinReDiff exhibit a range of effectiveness, lower ratios, though better than baseline models, fall short of the peak performance observed at 15%. Conversely, higher ratios miss the mark on achieving the necessary balance between introducing beneficial modifications and maintaining functional precision, highlighting the critical nature of optimizing the masking ratio.

In analyzing sequence diversity and structure preservation metrics, we found an intricate balance that underscores the complexity of protein redesign. The 15% masking ratio, our model's sweet spot for enhancing ligand binding affinity, also achieves outcomes equivalent to baseline methods in both sequence diversity and structure preservation. This equilibrium suggests that while ProteinReDiff excels in optimizing ligand interactions, a paramount objective in protein redesign, it does so without compromising on the diversity of sequences explored or the structural integrity of the original proteins. Notably, extreme values in either sequence diversity or structure preservation, which could be seen in other masking ratios, do not lead to optimal ligand binding affinities. This finding highlights an inverse relationship between pushing the limits of diversity and preservation and achieving the primary goal of binding enhancement. Thus, the 15% masking ratio not only stands out for its ability to significantly improve ligand binding affinity but also for maintaining a balanced approach, ensuring that enhancements in functionality do not detract from the protein's structural and functional viability. This nuanced understanding of the interplay between these critical metrics emphasizes the sophistication of ProteinReDiff's approach to protein redesign, promising a method that respects the delicate balance necessary for successful therapeutic development.

Moreover, the capability of ProteinReDiff to operate efficiently using merely protein sequences and ligand SMILES as inputs, without the requirement for detailed 3D structural data, marks a significant leap in computational protein design. This feature gains particular importance considering that the model not only achieves structure preservation at levels competitive with Inverse Folding (IF) models, which rely heavily on structural information for sequence optimization but also excels in enhancing ligand binding affinity. This approach insightfully captures and applies the core principles of protein-ligand interactions and structural fidelity directly from sequence data.

In the visualizations provided in Figure 7, the nuanced distinctions between the original and redesigned proteins underscore the targeted precision of ProteinReDiff. This precision manifests in strategic adjustments

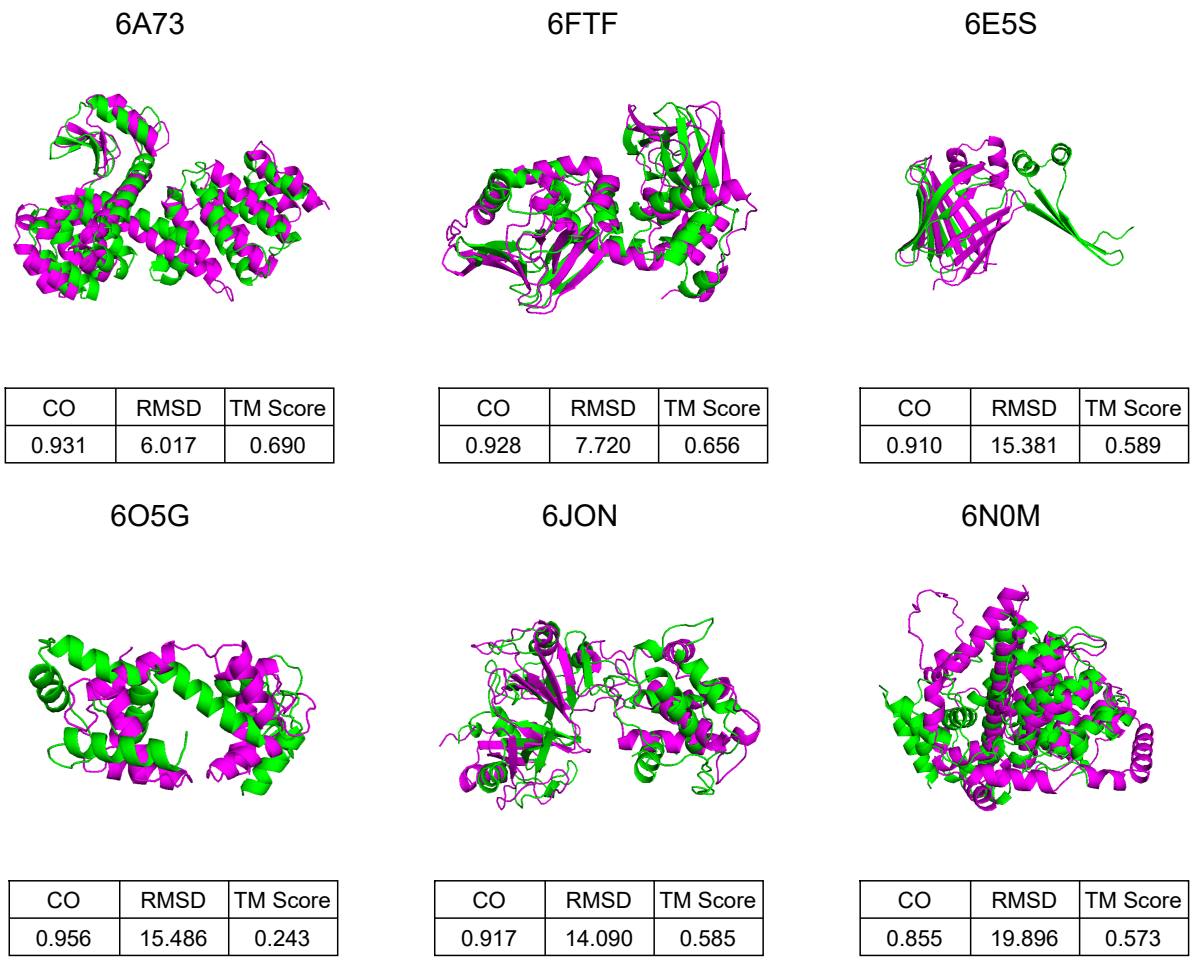

Figure 5: Comparative visualizations of protein structures, each annotated with its corresponding PDB ID. The figure includes a succinct table detailing Contact Overlap (CO) and Root Mean Square Deviation (RMSD) metrics. Original protein structures are highlighted in green, and the redesigned versions by ProteinReDiff are depicted in pink, illustrating the precise structural changes and enhancements achieved through the redesign.

at the molecular level, specifically engineered to amplify ligand binding efficiency. Despite the profound impact on binding affinity, these adjustments are executed with such finesse that structural deviations from the original framework are minimal. This approach not only enhances the protein's interaction with ligands but also preserves its structural and functional integrity. The modifications, though seemingly minor, are the result of a complex optimization process, balancing the need for improved functionality with the imperative to maintain the protein's overall architecture.

6 Conclusions

In conclusion, this study presents ProteinReDiff, a novel computational framework designed for the advanced redesign of ligand-binding proteins. Leveraging state-of-the-art techniques inspired by Equivariant Diffusion-Based Generative Models and the transformative insights of AlphaFold2, ProteinReDiff showcases a profound ability to decipher and enhance complex protein-ligand interactions. Uniquely, our model excels in optimizing ligand binding affinity based solely on the initial protein sequences and ligand SMILES strings, circumventing the traditional reliance on comprehensive structural data. The experimental validations of ProteinReDiff illuminate its remarkable capacity not only to elevate ligand binding affinity but also to main-

Table 3: Comparison of method performance across multiple metrics: Ligand binding affinity (LBA), sequence diversity, and structure preservation. Ligand binding affinity (LBA), TM Score, and RMSD are reported as mean values with their respective margins of error.

Category	Method	LBA (kcal/mol) ↓	Sequence diversity ↑	Structure preservation		
				TM Score ↑	RMSD (Å) ↓	CO ↑
Baseline	CARP	-5.658 ± 0.301	185.532	0.850 ± 0.023	3.768 ± 0.553	0.922 ± 0.003
	MIF	-5.518 ± 0.381	185.600	**0.877** ± 0.020	**2.986** ± 0.468	0.938 ± 0.002
	MIF-ST	-5.596 ± 0.330	185.584	0.872 ± 0.021	3.026 ± 0.451	0.937 ± 0.003
	ESMIF	-5.555 ± 0.326	187.512	0.837 ± 0.021	4.000 ± 0.501	0.915 ± 0.003
	ProteinMPNN	-5.423 ± 0.225	188.792	0.714 ± 0.026	6.806 ± 0.616	0.859 ± 0.004
	LigandMPNN	-5.717 ± 0.287	**191.384**	0.782 ± 0.024	4.512 ± 0.668	0.915 ± 0.008
	Protein Generator	-5.674 ± 0.266	186.962	0.806 ± 0.022	4.431 ± 0.523	0.899 ± 0.003
	DPL	-5.551 ± 0.459	188.139	0.788 ± 0.024	5.094 ± 0.537	0.896 ± 0.009
	Reference cases	-5.847 ± 0.263	-	-	-	-
ProteinReDiff (Ours)	5% Masking	-5.805 ± 0.252	185.935	0.864 ± 0.022	3.197 ± 0.470	**0.942** ± 0.007
	15% Masking	**-6.803** ± 0.329	186.627	0.845 ± 0.023	3.690 ± 0.508	0.935 ± 0.007
	30% Masking	-5.769 ± 0.244	187.877	0.803 ± 0.024	4.467 ± 0.544	0.916 ± 0.008
	40% Masking	-5.617 ± 0.366	188.600	0.756 ± 0.026	5.639 ± 0.625	0.896 ± 0.008
	60% Masking	-5.467 ± 0.318	190.425	0.305 ± 0.024	18.056 ± 0.773	0.735 ± 0.010
	70% Masking	-5.470 ± 0.199	187.291	0.147 ± 0.004	23.197 ± 0.497	0.689 ± 0.007

tain essential sequence diversity and structural integrity. These findings herald a significant leap forward in protein-ligand complex modeling, suggesting a bright future for ProteinReDiff in various biotechnological and pharmaceutical domains. The success of ProteinReDiff paves the way for its further development and broad application in drug design and protein engineering.

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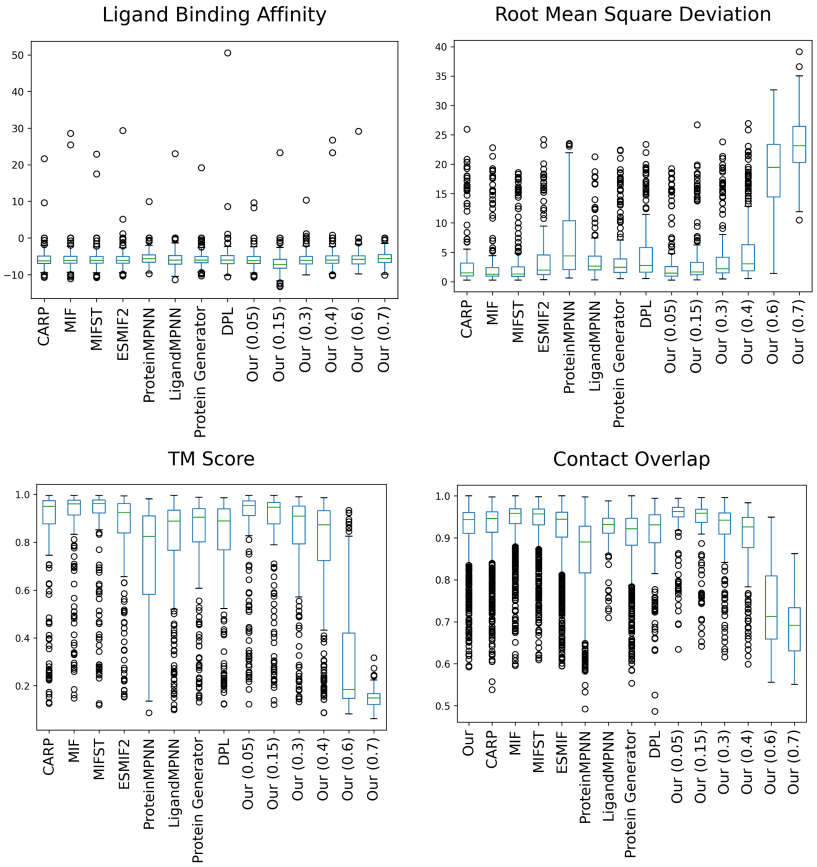

Figure 6: Boxplot illustrating the distribution of ligand binding affinities, and structure preservation metrics (TM Score and RMSD) across all methods evaluated, including baseline models and variations of ProteinReDiff. Each boxplot showcases the median, quartiles, and outliers within the data, providing insight into the variability and central tendency of each metric across the dataset's samples.

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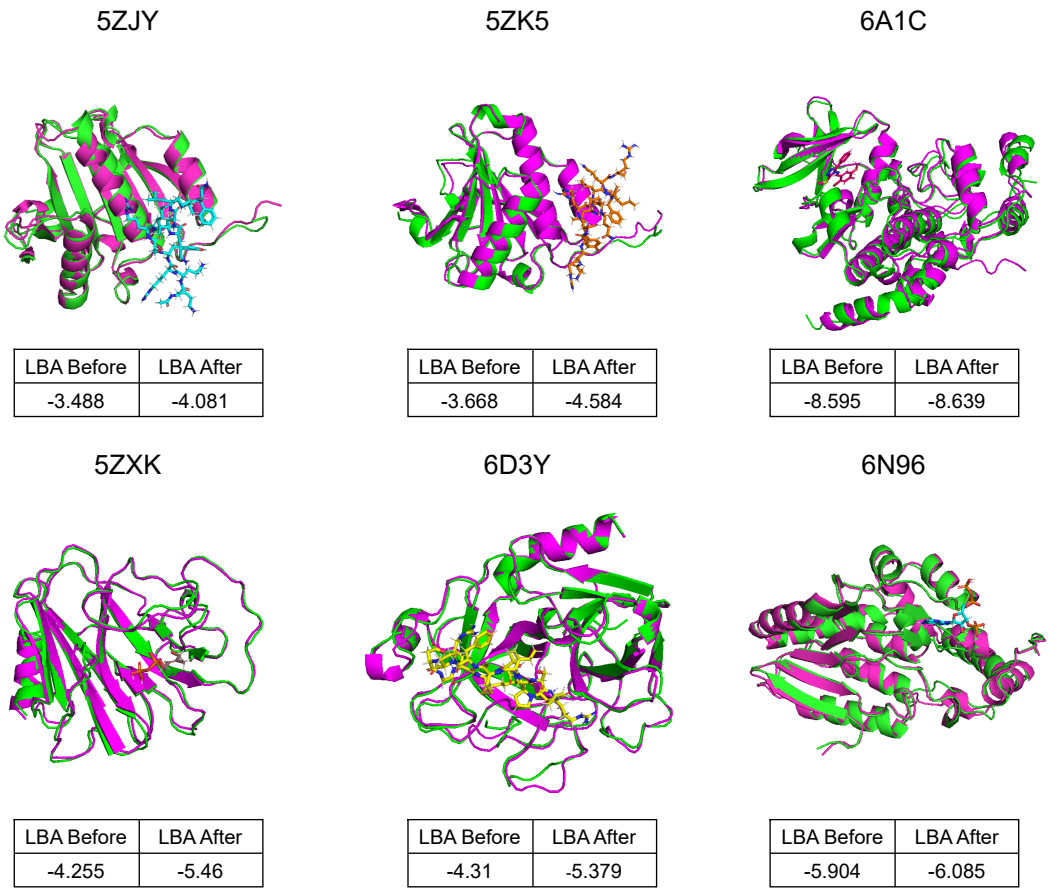

Figure 7: Comparative visualizations of protein-ligand complexes, each labeled with corresponding PDB IDs and accompanied by a small table showing Ligand Binding Affinity (LBA) before and after the redesign. Original structures are highlighted in green, while redesigned versions by ProteinReDiff appear in pink. Ligands are depicted in various colors to emphasize specific binding sites and molecular interaction enhancements post-redesign.

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A Evaluating Protein-Ligand Complex Representation

Evaluation Methodology In the continuation of our study's exploration of protein-ligand complex representations, we extended the use of the PDBBind v2020 dataset, previously detailed in our training process, to evaluate the effectiveness of embeddings generated by ProteinReDiff. Employing these embeddings as input features, we trained a Gaussian Process (GP) model aimed at predicting ligand binding affinity. The choice of a GP model, recognized for its probabilistic nature and adaptability to the nuanced, uncertain dynamics of biological interactions, was pivotal in assessing how well our embeddings encapsulate predictive information about protein-ligand interactions. The GP model used a Gaussian likelihood, which is appropriate for regression tasks, along with a Radial Basis Function (RBF) kernel. We chose the RBF kernel due to its effectiveness in modeling smooth, continuous variations, which is characteristic of protein-ligand binding affinities. The training of the GP model focused on optimizing the parameters to ensure a robust fit to the training data.

Table 4: Experimental results of ligand binding affinity prediction task on PDBBind v2020 dataset.

Approach	RMSE ↓ ($-\log K_d/K_i$)	MAE ↓ ($-\log K_d/K_i$)	Pearson ↑	Spearman ↑
Pafnucy (Stepniewska-Dziubinska et al., 2018)	1.435	1.144	0.635	0.587
OnionNet (Zheng et al., 2019)	1.403	1.103	0.648	0.602
IGN (Jiang et al., 2021)	1.404	1.116	0.662	0.638
SIGN (Li et al., 2021)	1.373	1.086	0.685	0.656
SMINA (Koes et al., 2013)	1.466	1.161	0.665	0.663
GNINA (McNutt et al., 2021)	1.740	1.413	0.495	0.494
dMaSIF (Sverrisson et al., 2021)	1.450	1.136	0.629	0.588
TankBind (Lu et al., 2022)	1.345	1.060	0.718	**0.689**
GraphDTA (Nguyen et al., 2020)	1.564	1.223	0.612	0.570
TransCPI (Chen et al., 2020)	1.493	1.201	0.604	0.551
MolTrans (Huang et al., 2020)	1.599	1.271	0.539	0.474
DrugBAN (Bai et al., 2023a)	1.480	1.159	0.657	0.612
DGraphDTA (Jiang et al., 2020)	1.493	1.201	0.604	0.551
WGNN-DTA (Bai et al., 2023b)	1.501	1.196	0.605	0.562
STAMP-DPI (Wang et al., 2022)	1.503	1.176	0.653	0.601
PSICHIC (Koh et al., 2023)	**1.314**	**1.015**	0.710	0.686
ProteinReDiff (Our)	1.443	1.168	**0.721**	0.639

Results and discussion The evaluation of our ProteinReDiff model on the PDBBind v2020 dataset demonstrates competitive results in predicting ligand binding affinity using protein-ligand complex representations, as evidenced in Table 4. It's important to note that this experiment aimed to verify the effectiveness of our protein-ligand complex representation rather than to fine-tune the model for this specific task. Consequently, while our results are promising and competitive with specialized studies focused solely on ligand binding affinity prediction, the primary goal was to validate the representation's capability within the protein redesign framework of ProteinReDiff. This underscores the model's utility in guiding the redesign process effectively, affirming the robustness and applicability of our protein-ligand complex representation strategy.