Kernel Normalized Convolutional Networks for Privacy-Preserving Machine Learning

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***Abstract*—Normalization is an important but understudied challenge in privacy-related application domains such as federated learning (FL) and differential privacy (DP). While the unsuitability of batch normalization for FL and DP has already been shown, the impact of the other normalization methods on the performance of federated or differentially private models is not well-known. To address this, we draw a performance comparison among layer normalization (LayerNorm), group normalization (GroupNorm), and the recently proposed kernel normalization (KernelNorm) in FL and DP settings. Our results indicate LayerNorm and GroupNorm provide no performance gain compared to the baseline (i.e. no normalization) for shallow models, but they considerably enhance performance of deeper models. KernelNorm, on the other hand, significantly outperforms its competitors in terms of accuracy and convergence rate (or communication efficiency) for both shallow and deeper models. Given these key observations, we propose a kernel normalized ResNet architecture called KNResNet-13 for differentially private learning environments. Using the proposed architecture, we provide new state-of-the-art accuracy values on the CIFAR-10 and Imagenette datasets.**

***Index Terms*—Differential Privacy, Federated Learning, Kernel Normalization, Group Normalization, Batch Normalization**

I. Introduction

Deep convolutional neural networks (*CNNs*) are popular in a diverse range of image vision tasks including image classification [1] and object detection [2]. Deep CNNs rely on large-scale datasets to effectively train the model, which might be difficult to provide in a centralized manner [3]. This is because datasets are often distributed across different sites such as hospitals, and contain sensitive data which cannot be transferred to a centralized location due to privacy regulations [4]. Even if such datasets become available, training algorithms can pose privacy risks to the individuals participating in the dataset, leaking privacy-sensitive information through the trained model [5]–[7].

Federated learning (*FL*) [8] addresses the large-scale data availability challenge by enabling clients to jointly train a global model under the coordination of a central server without sharing their private data. *Network communication*, on the other hand, emerges as a new challenge in federated environments, requiring a large number of communication rounds for model convergence, and exchanging a large amount of traffic in each round [9]. FL also causes utility (e.g. in terms of accuracy) reduction due to the *Non-IID* (not independent and identically distributed) nature of the data across the clients [10]. Finally, although FL eliminates the requirement of data sharing, it might still lead to privacy leakage, where the private data of the clients can be reconstructed from the model updates shared with the server [11]–[13].

Differential privacy (DP) [14] copes with the privacy challenge in both centralized and federated environments by injecting random noise into the model parameters (updates) to limit the information learnt about a particular sample in the dataset [15]. DP, however, adversely affects the model utility similar to FL because of the injected noise. In general, there is a trade-off between privacy and utility in DP, where stronger privacy leads to lower utility [16].

Batch normalization (BatchNorm) [17] is the de facto normalization layer in popular deep CNNs such as ResNets [18] and DenseNets [19], which remarkably improves the model convergence rate and accuracy in centralized training. BatchNorm, however, is not suitable for FL and DP settings. This is because BatchNorm relies on the IID distribution of feature values in the batch [17], which is not the case in federated environments. Moreover, DP requires to compute per-sample gradients [15], which is not possible for batch normalized CNNs. *Batch-independent* layers including *layer normalization* (LayerNorm) [20], *group normalization* (GroupNorm) [21], and the recently proposed *kernel normalization* (KernelNorm) [22] do not suffer from the BatchNorm's limitations, and thus, are applicable to FL and DP.

Normalization challenge. Unsuitability of BatchNorm for federated and differentially private learning has presented a real challenge in the corresponding environments. Unlike the other challenges (i.e. utility, network communication, and

privacy), the normalization issue has remained understudied in the context of FL and DP. Previous works [10], [23] illustrate that GroupNorm outperforms BatchNorm in terms of accuracy in federated settings. Likewise, GroupNorm also delivers higher accuracy than LayerNorm in differentially private learning [24]–[26]. Additionally, KernelNorm provides significantly higher accuracy and faster convergence rate compared to LayerNorm and GroupNorm in both FL and DP settings according to the original study [22].

However, the previous studies have not made a comparison between different normalization layers and the NoNorm (no normalization layer) case in the first place. Moreover, the experimental evaluation of KernelNorm for FL and DP environments is limited in the original study [22], focusing only on cross-silo federated setting (few clients with relatively large datasets) [27] and a shallow model in DP. Given that, two fundamental questions arise: (1) *Do LayerNorm, GroupNorm, and KernelNorm also deliver higher performance compared to NoNorm in federated and differentially private learning?*, and (2) *Does KernelNorm still outperform the other normalization layers in the cross-device FL setting (many clients with small datasets) and using deeper models in DP?*

Our findings. We conduct extensive experiments using the VGG-6 [28], ResNet-8 [22], PreactResNet-18 [29], and DenseNet20×16 [19] models trained on the CIFAR-10/100 [30] and Imagenette [31] datasets in FL and DP settings to address those questions. The key findings are as follows:

1) LayerNorm and GroupNorm do not necessarily outperform the NoNorm case for shallow models in FL and DP settings. For instance, LayerNorm and GroupNorm provide slightly lower accuracy and communication efficiency than NoNorm in the cross-silo federated setting, where the shallow VGG-6 model is trained on CIFAR-10. Similarly, LayerNorm and GroupNorm achieve lower accuracy than NoNorm using the shallow ResNet-8 model on CIFAR-10 in DP (Section III).
2) In both cross-silo and cross-device FL, and with both shallow and deeper models in DP, KernelNorm significantly outperforms NoNorm, LayerNorm, and GroupNorm in terms of communication efficiency (convergence rate) and accuracy (Section III).

Solution. Based on our findings, we advocate employing KernelNorm as the effective normalization layer for FL and DP settings. Given that, we propose a KernelNorm based ResNet architecture called KNResNet-13, and show it delivers considerably higher accuracy than the state-of-the-art GroupNorm-based architectures on the CIFAR-10 and Imagenette datasets in differentially private learning settings (Section IV).

Contributions. We make the following contributions: (I) we show that LayerNorm and GroupNorm do not deliver better accuracy than NoNorm using shallow networks in FL and DP environments, (II) we illustrate that the recently proposed KernelNorm layer has great potential to become the de facto normalization layer in privacy-enhancing/preserving machine learning, and (III) we provide new state-of-the-art accuracy values on CIFAR-10 and Imagenette using our proposed KNResNet-13 architecture in the DP setting, when trained from scratch.

II. Preliminaries

Federated learning (FL). A federated environment consists of multiple clients as data holders and a central server as coordinator. FL is a privacy-enhancing technique, which enables the clients to train a global model without sharing their private data with a third party. In FL, or more precisely in the `FederatedAveraging` (*FedAvg*) algorithm [8], the server randomly chooses K clients, and sends them the global model parameters W_i^g in each communication round i. Next, each selected client j trains the global model on its local dataset using *mini-batch gradient descent*, and shares the local model parameters $W_{i,j}^l$ with the server. Finally, the server takes the weighted average over the local parameters from the clients to update the global model:

$$W_{i+1}^g = \frac{\sum_{j=1}^{K} N_j \cdot W_{i,j}^l}{\sum_{j=1}^{K} N_j},$$

where N_j is the number of samples in client j.

A *cross-device* federated setting contains a large number of clients such as mobile devices with small datasets [27]. The server selects a fraction of clients in each round. Moreover, the underlying assumption is that the communication between clients and server is unstable, and the clients might drop out during training. A *cross-silo* setting, on the other hand, consists of few clients such as hospitals or research institutions with relatively large datasets and stable network connection [27]. All clients participate in model training in all communication rounds. For more details on federated learning, the readers are referred to [8] and [27].

Differential privacy (DP). The differential privacy approach provides a theoretical framework and collection of techniques for privacy-preserving data processing and release [14]. Its guarantees are formulated in an information-theoretic fashion and describe the upper bound on the multiplicative information gain of an adversary observing the output of a computation over a sensitive database. This definition endows DP with a robust theoretical underpinning and ascertains that its guarantees hold in the presence of adversaries with unbounded prior knowledge and under infinite post-processing. Moreover, DP guarantees are *compositional*, meaning that they degrade predictably when a DP system is executed repeatedly on the same database. Formally, a randomised mechanism $\mathcal{M}$ is said to preserve (ε, δ)-DP if, for all databases D and D' differing in the data of one individual and all measurable subsets S of the range of $\mathcal{M}$, the following inequality holds:

$$\mathbb{P}(\mathcal{M}(D) \in S) \leq e^{\varepsilon}\mathbb{P}(\mathcal{M}(D') \in S) + \delta,$$

where $\mathbb{P}$ is the probability measure, $\varepsilon \geq 0$ and $0 \leq \delta < 1$. Of note, this inequality must hold also if D and D' are swapped. The guarantee is given over the randomness of $\mathcal{M}$. Intuitively, this characterisation implies that the output of the mechanism should not change *too much* when one individual's

data is added or removed from a database, or, equivalently, the influence of one individual's data on the result of the computation should be small.

The application of DP to the training of neural networks is usually (and in our work) based on the differentially private stochastic gradient descent (DP-SGD) algorithm [15]. Here, the role of the database is played by the individual (per-sample) gradients of the loss function with respect to the parameters. For the DP guarantee to be well-defined, the intermediate layer outputs (activations), leading to the computation of a per-sample gradient, are not allowed to be influenced by more than one sample. Hence, layers like BatchNorm, which normalize the activations of a layer by considering either other samples in the batch or the statistics of previously seen batches, cannot be employed in DP. We refer the readers to [14], [15], [32] for more information on differential privacy.

Normalization. The normalization layers are different from each other in their normalization unit, which is a subset of elements from the original input that are normalized together with the mean and variance of the unit [22]. Assume that the input is a 4-dimensional tensor with batch, channel, height, and width as dimensions. BatchNorm [17] considers all elements in the batch, height, and width dimensions as its normalization unit. LayerNorm [20], on the other hand, performs normalization across all elements in the channel, height, and width dimensions but separately for each sample in the batch. The normalization unit of GroupNorm [21] contains all elements in the height and width dimensions similar to LayerNorm, but a subset of elements (specified by the group size) in the channel dimension.

BatchNorm, LayerNorm, and GroupNorm are referred to as *global normalization* layers because they consider all elements in the height and width dimensions during normalization [33]. There is also a one-to-one correspondence between the input and output elements in the aforementioned layers, implying that they do not modify the input shape [22]. These layers have *shift* and *scale* as learnable parameters too for ensuring that the distributions of the input and output elements remain similar [17]. In contrast to BatchNorm, LayerNorm and GroupNorm are *batch-independent* because they perform normalization independently of the batch dimension.

KernelNorm [22] considers a subset of elements specified by the kernel window in the height and width dimensions, but all elements in the channel dimension as its normalization unit. Thus, KernelNorm is a *local normalization* layer. Moreover, KernelNorm has no learnable parameters, and its output might have very different shape than the input. Similar to LayerNorm and GroupNorm, KernelNorm is batch-independent because it performs normalization separately for each sample of the batch. The *kernel normalized convolutional* (*KNConv*) layer [22] is the combination of the KernelNorm and convolutional layer, where the output of the former is given as input to the latter. KernelNorm and KNConv capitalize on the dropout operation to introduce regularization effect during normalization. They normalize the elements of the original unit with mean and standard deviation of the dropped-out version of the unit [22]. Both KernelNorm and KNConv, thus, take dropout probability p as additional hyper-parameter.

The modern CNNs are batch-normalized, leveraging the BatchNorm and convolutional layers in their architecture. The layer/group normalized counterparts of these networks are obtained by simply replacing BatchNorm with LayerNorm/GroupNorm. The kernel normalized convolutional networks (*KNConvNets*) [22], on the other hand, employ the KernelNorm and KNConv layers as the main building blocks, while forgoing the BatchNorm layers. For more details on normalization layers, the readers can see [17], [20]–[22].

III. Evaluation

We conduct extensive experiments to investigate the performance of different batch-independent normalization layers including LayerNorm, GroupNorm, and KernelNorm in the cross-silo and cross-device federated settings as well as differentially private learning environments. In the following, we first provide the description of the datasets, models, and case studies, and then discuss the results and findings.

A. Experimental Setup

Datasets. The CIFAR-10/100 dataset [30] contains 50000 train and 10000 test samples of shape 32×32 from 10/100 classes. The Imagenette dataset (160-pixel version) [31] is a subset of Imagenet [34], including 9469 train and 3925 test images from 10 "easily classified" labels. The samples of Imagenette are resized to 128×128 pixel. The feature values are normalized using the mean and standard deviation of the dataset for NoNorm, LayerNorm, and GroupNorm based models, whereas they are divided by 255 in the kernel normalized models.

Models. We adopt the VGG-6 architecture from [28] and [22], ResNet-8 model from [22], PreactResNet-18 implementation from [35], and DenseNet-20$\times$16 (depth of 20 and growth rate of 16) implementation from [36]. In layer/group normalized networks, the BatchNorm layer is replaced with LayerNorm/GroupNorm. The kernel normalized counterparts are implemented according to the guidelines in the original paper [22], where the convolutional layers are replaced by KNConv, BatchNorm layers are removed, and a KernelNorm layer is placed before the final average pooling layer in the ResNet, PreactResNet, and DenseNet models. The models employ the ReLU and Mish [37] activation functions in the FL and DP settings, respectively. We implement the models in the PyTorch library [38].

Case Studies. We design seven different case studies, four in FL and three in DP, to make the performance comparison among the normalization layers:

1) **CIFAR-10-VGG-6 (cross-silo FL):** This case study aims to train the *shallow* VGG-6 model on the *low-resolution* CIFAR-10 dataset in a cross-silo federated environment containing 10 clients, where each client has samples from only 2 classes. The sample sizes of the clients are almost the same.

TABLE I: **Federated learning**: Test accuracy for different normalization layers; NoNorm (no normalization) slightly outperforms LayerNorm and GroupNorm in (a); KernelNorm delivers higher accuracy than the competitors; B: batch size.

(a) CIFAR-10-VGG-6 **(cross-silo FL)**

B	NoNorm	LayerNorm	GroupNorm	KernelNorm
16	80.19±0.29	78.93±0.43	78.63±0.56	**83.64**±0.41
64	79.23±0.31	78.97±0.36	79.4±0.38	**82.13**±0.25

(b) CIFAR-10-VGG-6 **(cross-device FL)**

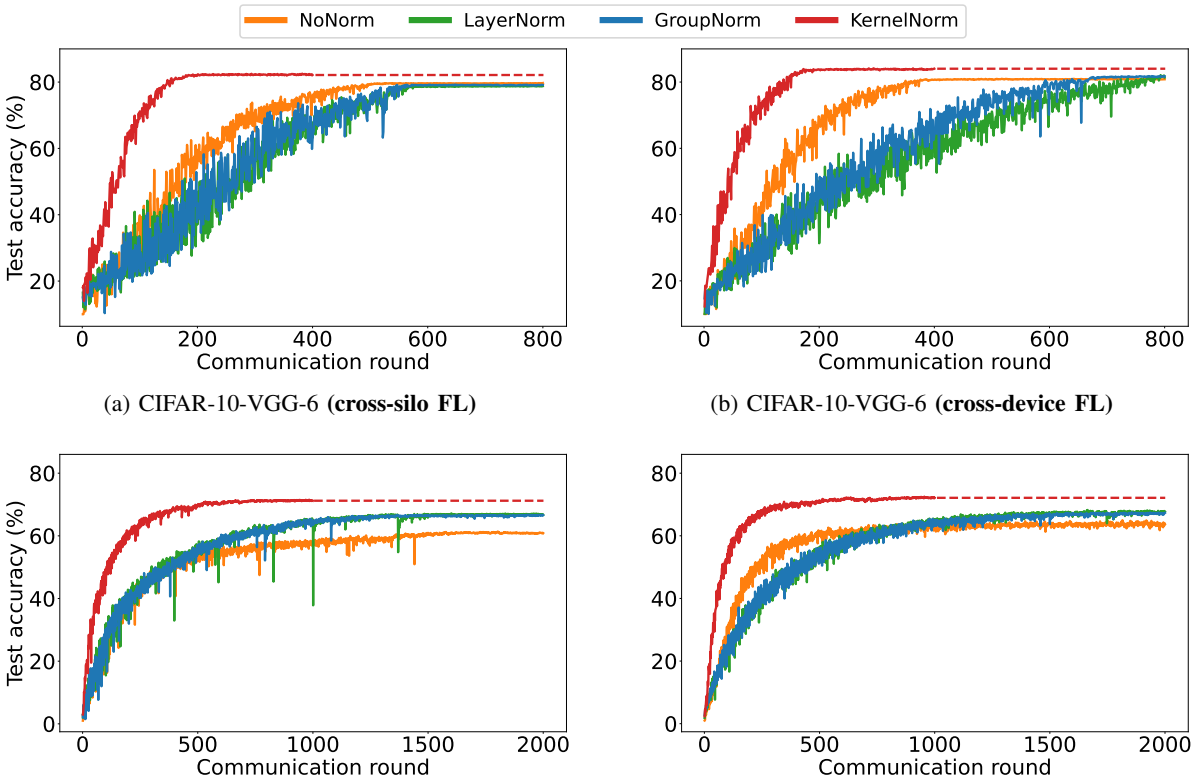
B	NoNorm	LayerNorm	GroupNorm	KernelNorm
16	80.95±0.27	81.89±0.32	81.39±0.47	**84.13**±0.26
64	80.72±0.06	81.43±0.19	81.44±0.18	**83.77**±0.11

(c) CIFAR-100-PreactResNet-18 **(cross-silo FL)**

B	NoNorm	LayerNorm	GroupNorm	KernelNorm
16	61.89±0.13	68.16±0.44	67.86±0.1	**71.72**±0.19
64	60.8±0.33	66.9±0.41	66.45±0.18	**71.29**±0.21

(d) CIFAR-100-PreactResNet-18 **(cross-device FL)**

B	NoNorm	LayerNorm	GroupNorm	KernelNorm
16	63.54±0.22	68.05±0.92	68.23±0.13	**71.75**±0.24
64	63.33±0.36	67.84±0.43	67.47±0.24	**71.99**±0.09



(a) CIFAR-10-VGG-6 **(cross-silo FL)**

(b) CIFAR-10-VGG-6 **(cross-device FL)**

(c) CIFAR-100-PreactResNet-18 **(cross-silo FL)**

(d) CIFAR-100-PreactResNet-18 **(cross-device FL)**

Fig. 1: **Federated learning:** Communication efficiency for various normalization layers; KernelNorm provides significantly higher communication efficiency than the competitors. Surprisingly, NoNorm outperforms both LayerNorm and GroupNorm in terms of communication efficiency in most cases, i.e (a), (b), (d); B=64.

2) **CIFAR-10-VGG-6 (cross-device FL):** Similar to the cross-silo counterpart, but in a cross-device federated setting including 100 clients, where 20 clients are randomly selected in each round.
3) **CIFAR-100-PreactResNet-18 (cross-silo FL):** The purpose of this case study is to train the *deeper* PreactResNet-18 model on *more challenging* low-resolution CIFAR-100 dataset in a cross-silo federated environment consisting of 10 clients with samples from 20 labels. The clients have highly similar sample sizes.
4) **CIFAR-100-PreactResNet-18 (cross-device FL):** Akin to the cross-silo counterpart, but in a cross-device federated setting consisting of 100 clients, where 20 clients are randomly chosen by the server in each round.
5) **CIFAR-10-ResNet-8 (DP):** The goal of this case study is to train the *shallow* ResNet-8 model on the *low-resolution* CIFAR-10 dataset in the DP environment.
6) **CIFAR-10-DenseNet-20×16 (DP):** This case study aims to train the *deeper* DenseNet-20×16 model on the *low-resolution* CIFAR-10 dataset in the DP setting.
7) **Imagenette-PreactResNet-18 (DP).** The purpose of this case study is to train the *deeper* PreactResNet-18 model on the relatively *high-resolution* Imagenette dataset in the differentially private setting.

Federated Training. We employ five different values for learning rate tuning in federated case studies: η={0.005, 0.01, 0.025, 0.05, 0.1}. The kernel normalized models are trained for 400 and 1000 communication rounds in the CIFAR-10 and CIFAR-100 case studies, respectively. The number of rounds for the NoNorm, LayerNorm, and GroupNorm based models is as twice as the kernel normalized counterparts due to their slower convergence rate. The group size is the default value of 32 for the group normalized models [21]. The dropout probability for KNConv and KernelNorm layers are the default values of 0.1 and 0.5, respectively. The loss function is cross-entropy, optimizer is SGD with momentum of zero, and training algorithm is FedAvg (local epochs of 1).

Differentially Private Training. We set ε=6.0 and $\delta = 10^{-5}$ for all DP case studies. Regarding parameter tuning, we use learning rates of η={1.0, 1.5, 2.0} and clipping values of C={1.0, 1.5, 2.0}. The ResNet-8, DenseNet-20×16, and PreactResNet-18 models are trained for 50, 70, and 70 epochs, respectively. The learning rate is divided by 2 at epochs (T-30) and (T-10), where T is the number of epochs (i.e. 50 or 70). The group size of GroupNorm is 16 for DenseNet-20×16, but 32 for the other models. Notice that we cannot set group size to 32 for DenseNet-20×16 because the number of channels must be divisible by the group size. Dropout probability is 0.1 for all KNConv layers in the kernel normalized models. For ResNet-8, KernelNorm's dropout probability is 0.25, whereas it is 0.5 for DenseNet-20×16 and PreactResNet-18. We employ cross-entropy as loss function, SGD with momentum of zero as optimizer, and the Opacus library [39] for model training. We observe that changing the kernel size of the shortcut connections in PreactResNet-18 from 1×1 to 2×2 slightly enhances the accuracy of the kernel normalized version, but provides no accuracy gain for the competitors. Thus, the aforementioned kernel size remains 1×1 for NoNorm, LayerNorm, and GroupNorm, whereas it is 2×2 for KernelNorm.

B. Results

For all case studies, we first determine the best learning rate (and clipping value) based on the model accuracy on the test dataset. We repeat the experiment achieving the best accuracy three times and report mean/median and the standard deviation of the runs for the FL/DP case studies. For the FL case studies, we consider the average test accuracy over the last 10 communication rounds as the representative accuracy of the run. For the DP case studies, on the other hand, the final accuracy is the representative accuracy of the run too. The learning rate and clipping values corresponding to the experiments of each case study is available at the Appendix.

Federated Learning. Table I lists the test accuracy values for different FL case studies. According to the table, (1) NoNorm slightly outperforms LayerNorm and GroupNorm in terms of accuracy in the CIFAR-10-VGG-6 (cross-silo FL) case study; (2) LayerNorm and GroupNorm deliver higher accuracy than NoNorm in the other case studies; (3) KernelNorm achieves considerably higher accuracy than the competitors for all case studies.

Figure 1 illustrates the communication efficiency (i.e. accuracy vs. communication round) for the FL case studies. As shown in the figure, (1) NoNorm, surprisingly, provides higher communication efficiency compared to LayerNorm and GroupNorm for most case studies; (2) KernelNorm significantly outperforms the competitors in terms of communication efficiency for all case studies.

Differential Privacy. Table II and Figure 2 demonstrate the test accuracy and convergence rate of different normalization layers for the DP case studies, respectively. According to the table and figure, (1) NoNorm slightly outperforms LayerNorm and GroupNorm in terms of accuracy in the CIFAR-10-ResNet-8 case study, (2) KernelNorm provides (significantly) higher accuracy than the competitors in all case studies, and (3) KernelNorm based models converge much faster than those based on NoNorm, LayerNorm, and GroupNorm.

C. Findings

Based on our experimental results, (I) LayerNorm and GroupNorm do not necessarily outperform NoNorm in shallow networks such as VGG-6/ResNet-8 under the FL/DP settings. However, they achieve significant accuracy gain compared to NoNorm in deeper models (e.g. DenseNet-20×16 and PreactResNet-18), and (II) KernelNorm delivers considerably higher accuracy and convergence rate (communication efficiency) than NoNorm, LayerNorm, and GroupNorm with both shallow and deeper networks trained in differentially private settings as well as the cross-silo and cross-device federated environments. Therefore, KernelNorm is the most effective normalization method for DP and FL settings.

IV. Kernel Normalized ResNet-13

Given the superior performance of KernelNorm in our experimental evaluation, we propose a kernel normalized ResNet architecture (Figure 3) to improve the state-of-the-art (SOTA) accuracy on the CIFAR-10 and Imagenette datasets in differentially private learning settings. We refer to the proposed architecture as KNResNet-13, which includes twelve kernel normalized convolutional layers (KNConv) and a final classification (linear) layer.

The convolutional blocks in KNResNet-13 are either residual (Figure 3a) or transitional (Figure 3b). The residual blocks contain two KNConv layers with the same number of input and output channels. The transitional blocks include a KNConv layer and max-pooling layer, aiming to downsample the input. All KNConv layers have kernel size 3×3, stride 1×1, padding 1×1, and dropout probability 0.1. The kernel size of the max-pooling layers is 2×2. The architecture employs Mish as the activation function. The last residual block is followed by a KernelNorm layer with dropout probability 0.5, Mish activation, 2×2 adaptive average-pooling, and final linear layer with 1024 neurons. For high-resolution images (e.g. 224×224), the first KNConv layer is replaced by a 7×7 KNConv layer followed by a Mish activation and 2×2 max-pooling layer.

TABLE II: **Differential privacy**: Test accuracy for various normalization layers; NoNorm (no normalization) delivers slightly higher accuracy than LayerNorm and GroupNorm in (a); KernelNorm considerably outperforms the competitors; ε=6.0, δ=10^{-5}.

(a) CIFAR-10-ResNet-8 (DP)

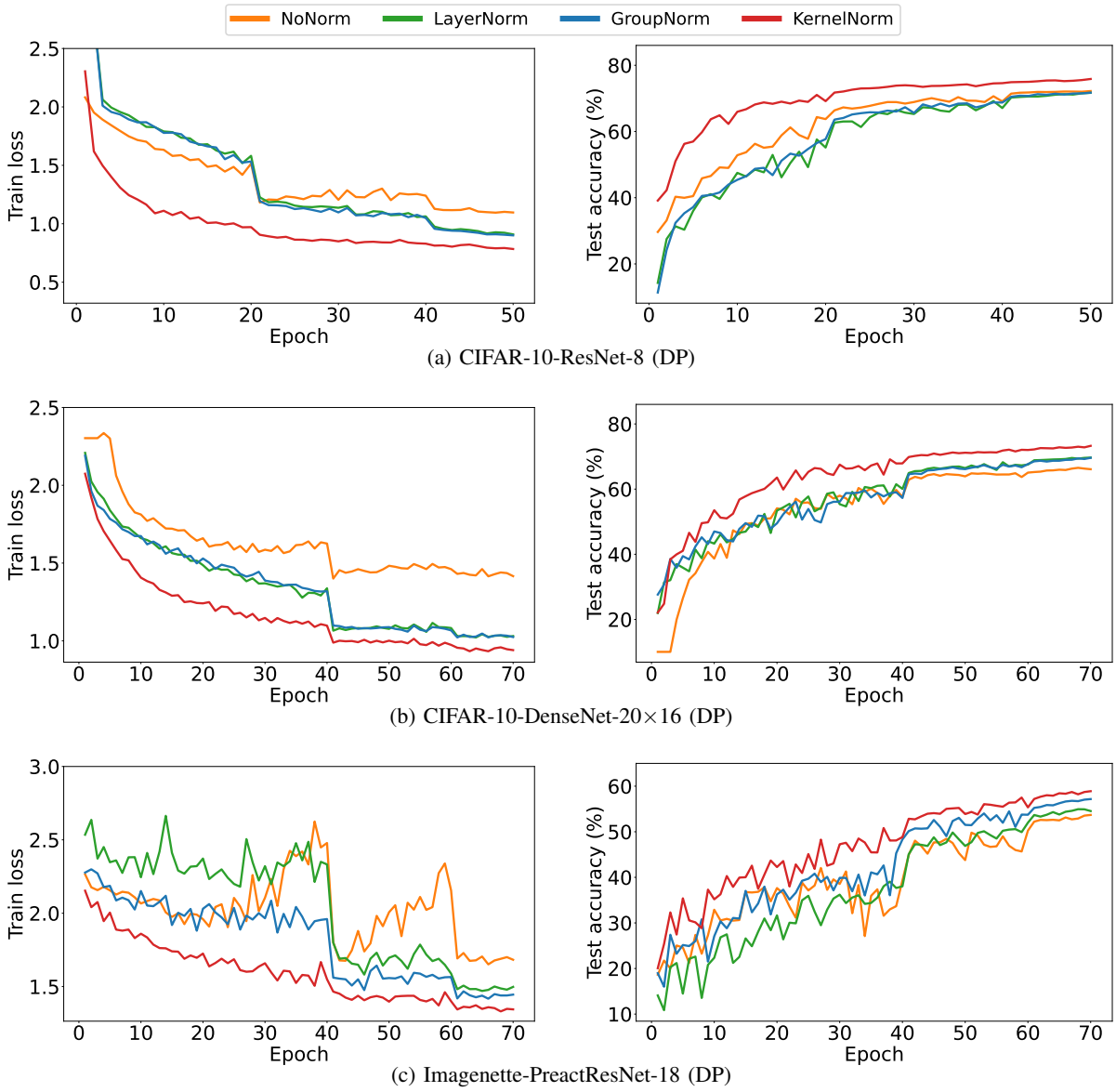
B	NoNorm	LayerNorm	GroupNorm	KernelNorm
512	65.11±0.29	70.01±0.19	70.27±0.08	**72.18**±0.15
1024	69.05±0.4	71.38±0.5	71.75±0.45	**74.31**±0.14
2048	72.7±0.25	71.67±0.42	71.73±0.31	**75.46**±0.34
3072	71.99±0.14	69.39±0.27	68.99±0.27	**75.48**±0.24

(b) CIFAR-10-DenseNet-20×16 (DP)

B	NoNorm	LayerNorm	GroupNorm	KernelNorm
256	57.03±0.48	65.62±0.7	66.16±0.56	**68.49**±0.24
512	64.15±0.74	69.24±0.68	68.72±0.65	**70.86**±0.44
1024	64.98±0.6	69.68±0.8	69.57±0.97	**72.74**±0.34
2048	65.29±0.53	66.66±0.78	67.31±0.26	**72.49**±0.39

(c) Imagenette-PreactResNet-18 (DP)

B	NoNorm	LayerNorm	GroupNorm	KernelNorm
512	25.27±3.95	54.83±0.65	56.7±0.19	**59.1**±0.33
1024	53.69±0.83	54.54±0.23	57.17±0.42	**58.9**±0.42
2048	53.53±0.99	53.3±0.32	54.59±0.27	**56.11**±0.26

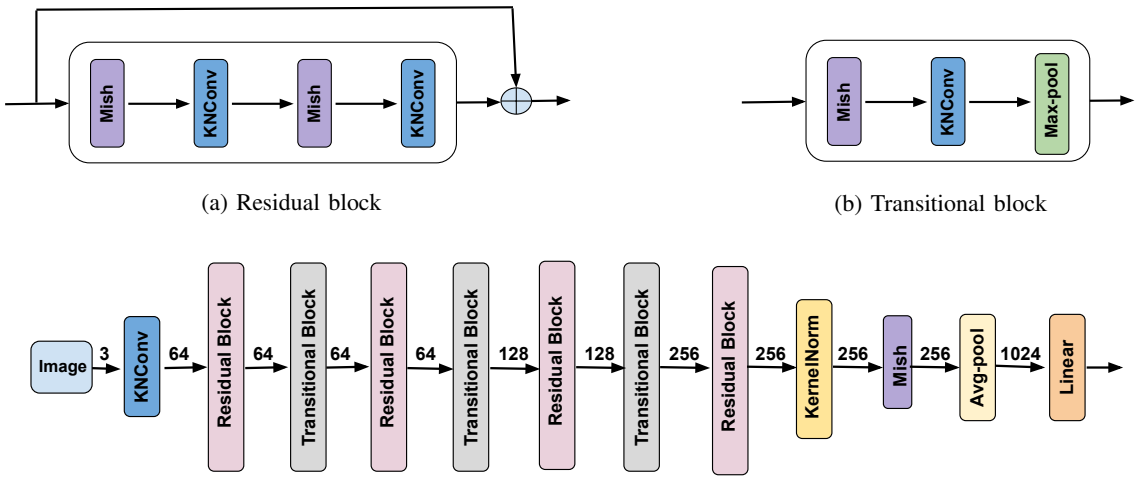


(a) CIFAR-10-ResNet-8 (DP)

(b) CIFAR-10-DenseNet-20×16 (DP)

(c) Imagenette-PreactResNet-18 (DP)

Fig. 2: **Differential privacy**: Convergence rate for different normalization layers; kernel normalized models provides much faster convergence rate than the competitors; batch size is 2048, 1024, 1024 for (a), (b), and (c), respectively.



(a) Residual block

(b) Transitional block

(c) KNResNet-13 architecture

Fig. 3: KNResNet-13 architecture consists of kernel normalized residual and transitional blocks. The kernel size, stride, and padding of the KNConv layers are 3×3, 1×1, and 1×1, respectively. The kernel size of the max-pooling layers is 2×2. The dropout probability of KNConv and KernelNorm are 0.1 and 0.5, respectively. For high-resolution images, the first KNConv layer is replaced by a KNConv layer with kernel size 7×7, stride 2×2, and padding 3×3, followed by a Mish activation and 2×2 max-pooling layer. The numbers indicate the input/output channels (filters) of KNConv or neurons of the linear layer.

In the following, we describe the data preprocessing and differentially private training procedure for CIFAR-10 and Imagenette. Then, we provide the accuracy values achieved by the KNResNet-13 model and compare them with those from the recent studies.

CIFAR-10. The only data preprocessing step is to divide the feature values by 255. KNResNet-13 is trained for T = 50, 70, 70, and 80 epochs with batch sizes of B=4096, 4096, 3072, and 3072 for ε=2.0, 4.0, 6.0, and 8.0, respectively. The learning rate is 2.0, clipping value is 1.5, and δ is 10^{-5}. The learning rate is divided by 2 at epochs (T - 30) and (T - 10). The optimizer is SGD with momentum of zero.

CIFAR-10 with augmentation multiplicity. The augmentation multiplicity is a recently proposed technique by *De et al.* [24], which computes the gradients for a given sample by taking average over the gradients computed for different augmentations of the same sample. For the CIFAR-10 dataset, this technique applies the sequence of random horizontal flipping and random cropping of size 32×32 and padding 4×4 to obtain an augmented version of a given sample. Here, we employ a slightly different way of augmentation multiplicity because the original technique provides negligible accuracy gain for our model. We first compute the gradients for the original sample, horizontally flipped (i.e. with probability of 1.0), and randomly cropped version of the sample, and then take the average over them to calculate the per-sample gradients. For ε=2.0, 4.0, 6.0, and 8.0, KNResNet-13 is trained for 80, 80, 100, and 100 epochs, respectively. The other training details are the same as CIFAR-10 with no augmentation multiplicity (previous paragraph).

Imagenette. We adopt the 320-pixel version of the dataset and resize the images to 224×224. We train KNResNet-13 with η=1.5, C=1.5, ε=7.0, δ=10^{-5}, and zero-momentum SGD for 100 epochs, where η is divided by 2 at epochs 70 and 90.

Results. Table III lists the test accuracy values from KNResNet-13 and the recent studies on CIFAR-10, CIFAR-10 with augmentation multiplicity, and Imagenette. KNResNet-13 delivers significantly higher accuracy than the models based on GroupNorm or NoNorm for all considered ε values on CIFAR-10 without augmentation multiplicity. Compared to kernel normalized ResNet-8 [22], KNResNet-13 provides up to 2% accuracy gain depending on the ε value.

On CIFAR-10 with augmentation multiplicity, KNResNet-13 outperforms both wide ResNet-16-4 and wide ResNet-40-4 [41] with much less augmentation multiplicity (3 vs. 16 vs. 32) for ε values of 2.0, 4.0, and 6.0. On Imagenette, KNResNet-13 achieves around 3% and 7% higher accuracy than GroupNorm based DenseNet-14 [26] and ResNet-9 [25] architectures.

Given the results from Table III, we provide new SOTA accuracy values on the CIFAR-10 and Imagenette datasets, when trained from scratch:

- On CIFAR-10 *without* augmentation multiplicity, accuracy values of 74.51%, 77.09%, 78.51% for ε=4.0, 6.0, and 8.0, respectively.
- On CIFAR-10 *with* augmentation multiplicity, accuracy of 70.57%, 76.19%, and 79.09% for ε=2.0, 4.0, and 6.0, respectively.
- On Imagenette, accuracy value of 72.24% for ε=7.0.

V. Discussion

According to the original study [22], KernelNorm is a local normalization method which takes into account the spatial correlation of the elements in the height and width dimensions during normalization. LayerNorm and GroupNorm, on the

TABLE III: **Differential privacy**: Comparison of the test accuracy values from the proposed KNResNet-13 architecture with those from the recent studies; δ=10^{-5}.

(a) CIFAR-10

Study	Model	Normalization	ε	Test accuracy
Klause et al. (2022) [25]	ResNet-9	GroupNorm	9.88	73.0
Nasirigerdeh et al. (2022) [22]	ResNet-8	KernelNorm	8.0	76.66
Ours	KNResNet-13	KernelNorm	8.0	**78.51**$\pm$0.35
Dörmann et al. (2021) [40]	VGG-8	NoNorm	7.42	70.1
Klause et al. (2022) [25]	ResNet-9	GroupNorm	7.42	71.8
Remerscheid et al. (2022) [26]	DenseNet-14	GroupNorm	7.0	73.5
Nasirigerdeh et al. (2022)	ResNet-8	KernelNorm	6.0	75.46
Ours	KNResNet-13	KernelNorm	6.0	**77.09**$\pm$0.31
Dörmann et al. (2021) [40]	VGG-8	NoNorm	4.21	66.2
Nasirigerdeh et al. (2022)	ResNet-8	KernelNorm	4.0	73.32
Ours	KNResNet-13	KernelNorm	4.0	**74.51**$\pm$0.19
Klause et al. (2022) [25]	ResNet-9	GroupNorm	2.89	65.6
Nasirigerdeh et al. (2022)	ResNet-8	KernelNorm	2.0	**68.08**
Ours	KNResNet-13	KernelNorm	2.0	**68.05**$\pm$0.07

(b) CIFAR-10 with augmentation multiplicity (K)

Study	Model	Normalization	K	ε	Test accuracy
De et al. (2022) [24]	Wide ResNet-16-4	GroupNorm	16	8.0	79.5
De et al. (2022) [24]	Wide ResNet-40-4	GroupNorm	32	8.0	**81.4**
Ours	KNResNet-13	KernelNorm	3	8.0	80.8 $\pm$0.22
De et al. (2022) [24]	Wide ResNet-16-4	GroupNorm	16	6.0	77.0
De et al. (2022) [24]	Wide ResNet-40-4	GroupNorm	32	6.0	78.8
Ours	KNResNet-13	KernelNorm	3	6.0	**79.09**$\pm$0.07
De et al. (2022) [24]	Wide ResNet-16-4	GroupNorm	16	4.0	71.9
De et al. (2022) [24]	Wide ResNet-40-4	GroupNorm	32	4.0	73.5
Ours	KNResNet-13	KernelNorm	3	4.0	**76.19**$\pm$0.04
De et al. (2022) [24]	Wide ResNet-16-4	GroupNorm	16	2.0	64.9
De et al. (2022) [24]	Wide ResNet-40-4	GroupNorm	32	2.0	65.9
Ours	KNResNet-13	KernelNorm	3	2.0	**70.57**$\pm$0.24

(c) Imagenette

Study	Model	Normalization	ε	Test accuracy
Klause et al. (2022) [25]	ResNet-9	GroupNorm	7.42	64.8
Klause et al. (2022) [25]	ResNet-9	GroupNorm	9.88	67.1
Remerscheid et al. (2022) [26]	DenseNet-14	GroupNorm	7.0	69.7
Ours	KNResNet-13	KernelNorm	7.0	**72.24**$\pm$0.48

other hand, are global normalization methods that normalize all elements in the aforementioned dimensions together.

Moreover, LayerNorm and GroupNorm have scale and shift as learnable parameters. In FL these parameters are aggregated, while they are perturbed with noise in DP, which can negatively affect the performance of the layer and group normalized models in the corresponding environments. KernelNorm does not require these learnable parameters, and as a result, is free of such limitation.

Finally, the feature values are not required to be normalized with the per-channel mean and standard deviation of the dataset in KernelNorm based models due to self-normalizing nature of KNConv, which normalizes the input before computing convolution. This is beneficial in particular for federated

environments because the clients do no need to share the mean and standard deviation of their local datasets with server to compute the corresponding global values.

Our experimental results and the proposed KNResNet-13 architecture demonstrate the effectiveness of KernelNorm for FL and DP settings. The aforementioned interesting properties of KernelNorm combined with its superior performance indicate the great potential of KernelNorm to become the standard normalization layer for federated and differentially private learning environments.

VI. Related Work

There are few studies that compare the performance of various normalization layers in federated settings. *Hsieh et al.* [10] experimentally show GroupNorm delivers higher accuracy than BatchNorm in supervised FL. *Zhang et al.* [23] demonstrate this also holds for semi-supervised FL. However, these studies have not compared GroupNorm with NoNorm as the baseline. Our experiments illustrate GroupNorm does not necessarily provide accuracy gain compared to NoNorm for shallow models in supervised federated settings.

Several studies investigate the performance of different batch-independent normalization layers for differentially private learning. *Klause et al.* [25] and *Remerscheid et al.* [26] show GroupNorm outperforms LayerNorm in terms of accuracy in DP. *Nasirigerdeh et al.* [22] illustrate KernelNorm delivers considerable accuracy gain compared to both LayerNorm and GroupNorm in differentially private learning. These previous works, however, do not consider NoNorm as the baseline for comparison. Our evaluation indicates NoNorm slightly outperforms both LayerNorm and GroupNorm for the shallow ResNet-8 model on CIFAR-10, whereas KernelNorm still provides significant accuracy improvement compared to NoNorm for the aforementioned setting. The experimental evaluation of *Nasirigerdeh et al.* [22], moreover, is limited to a single case study. We conduct more extensive experiments with deeper models on both low-resolution and high-resolution datasets to draw the performance comparison among NoNorm, LayerNorm, GroupNorm, and KernelNorm.

Some studies propose novel architectures or data augmentation techniques to enhance the accuracy of differentially private models. *Klause et al.* [25] present a 9-layer ResNet architecture in which an additional normalization is performed after the addition operation of the residual block, and show their architecture improves the accuracy compared to the original ResNet architecture. *Remerscheid et al.* [26] introduce a novel DenseNet-based architecture called SmoothNet, which employs 3×3 convolutional layers with a high number of filters in DenseNet blocks, and demonstrate it outperforms the previous ones in terms of accuracy. Both architectures employ GroupNorm as their normalization layer. We propose the KernelNorm-based KNResNet-13 architecture, and show it delivers considerably higher accuracy than the aforementioned architectures on CIFAR-10 and Imagenette.

De et al. [24] present the augmentation multiplicity technique, which computes the per-sample gradients by taking average over the gradients from different augmentations of the sample. We adopt this technique to train the proposed KNResNet-13 architecture on CIFAR-10. The accuracy from KNResNet-13 is higher than the wide ResNet-16-4 and ResNet-40-4 used in [24] for ε values of 2.0, 4.0, and 6.0.

VII. Conclusion and Future Work

We address the normalization challenge in the context of federated and differentially private learning environments. Through extensive experiments, we demonstrate that in FL and DP settings: (1) using no normalization layer in the architecture of shallow networks such as VGG-6 and ResNet-8 delivers slightly higher accuracy than LayerNorm and GroupNorm, (2) on deeper models such as DenseNet-20$\times$16 and PreactResNet-18, however, LayerNorm and GroupNorm significantly outperforms NoNorm, and (3) the recently proposed KernelNorm method achieves considerably higher accuracy and convergence rate compared to NoNorm, LayerNorm, and GroupNorm with both shallow and deeper models.

Given the superior performance of KernelNorm, we propose a kernel normalized ResNet architecture called KNResNet-13 for differentially private learning settings. Using the proposed architecture, we provide new SOTA accuracy on CIFAR-10 with and without augmentation multiplicity as well as Imagenette for different ε values, when trained from scratch.

We employ a low augmentation multiplicity value (i.e. 3) in our study due to the remarkable computational overhead of the technique. KNResNet-13 might deliver even higher accuracy with larger augmentation multiplicity values (e.g. 16 or 32), which can be an investigated in future studies. Additionally, the performance evaluation of kernel normalized architectures on the large Imagenet-32$\times$32 dataset [34] is an interesting direction for future works.

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APPENDIX

We perform **parameter tuning** over the learning rate and clipping values. In the next page, we provide the values of these hyper-parameters achieving the highest accuracy in each case study.

TABLE IV: **Federated learning**: Learning rate values giving the highest accuracy for each normalization layer; B: batch size.

(a) CIFAR-10-VGG-6 **(cross-silo FL)**

B	NoNorm	LayerNorm	GroupNorm	KernelNorm
16	0.025	0.025	0.01	0.025
64	0.025	0.025	0.05	0.025

(b) CIFAR-10-VGG-6 **(cross-device FL)**

B	NoNorm	LayerNorm	GroupNorm	KernelNorm
16	0.025	0.025	0.05	0.025
64	0.05	0.025	0.05	0.05

(c) CIFAR-100-PreactResNet-18 **(cross-silo FL)**

B	NoNorm	LayerNorm	GroupNorm	KernelNorm
16	0.01	0.01	0.005	0.025
64	0.01	0.01	0.01	0.05

(d) CIFAR-100-PreactResNet-18 **(cross-device FL)**

B	NoNorm	LayerNorm	GroupNorm	KernelNorm
16	0.01	0.01	0.005	0.025
64	0.05	0.01	0.01	0.1

TABLE V: **Differential privacy**: Learning rate values giving the highest accuracy for each normalization layer; B: batch size.

(a) CIFAR-10-ResNet-8 (DP)

B	NoNorm	LayerNorm	GroupNorm	KernelNorm
512	1.0	1.0	1.0	1.0
1024	2.0	2.0	1.5	1.5
2048	2.0	2.0	2.0	2.0
3072	2.0	2.0	2.0	2.0

(b) CIFAR-10-DenseNet-20×16 (DP)

B	NoNorm	LayerNorm	GroupNorm	KernelNorm
256	1.0	1.5	2.0	1.5
512	1.0	2.0	2.0	1.5
1024	1.5	2.0	1.5	1.5
2048	2.0	2.0	2.0	1.5

(c) Imagenette-PreactResNet-18 (DP)

B	NoNorm	LayerNorm	GroupNorm	KernelNorm
512	1.0	1.0	1.0	1.5
1024	1.0	1.0	1.0	2.0
2048	1.5	1.0	1.0	2.0

TABLE VI: **Differential privacy**: Clipping values giving the highest accuracy for each normalization layer; B: batch size.

(a) CIFAR-10-ResNet-8 (DP)

B	NoNorm	LayerNorm	GroupNorm	KernelNorm
512	1.0	1.0	1.0	1.0
1024	1.0	1.5	2.0	1.5
2048	2.0	2.0	2.0	2.0
3072	2.0	2.0	2.0	2.0

(b) CIFAR-10-DenseNet-20×16 (DP)

B	NoNorm	LayerNorm	GroupNorm	KernelNorm
256	1.0	1.5	2.0	1.5
512	1.0	1.5	1.5	1.5
1024	2.0	2.0	2.0	1.5
2048	2.0	1.5	2.0	1.0

(c) Imagenette-PreactResNet-18 (DP)

B	NoNorm	LayerNorm	GroupNorm	KernelNorm
512	1.0	1.0	1.0	1.5
1024	1.0	1.5	1.0	1.0
2048	1.0	1.0	1.0	1.0