TotalRecall: A Bidirectional Candidates Generation Framework for Large Scale Recommender & Advertising Systems

Abstract

Recommender (RS) and Advertising/Marketing Systems (AS) play the key roles in E-commerce companies like Amazaon and Alibaba. RS needs to generate thousands of item candidates for each user ($u2i$), while AS needs to identify thousands or even millions of high-potential users for given items so that the merchant can advertise these items efficiently with limited budget ($i2u$). This paper proposes an elegant bidirectional candidates generation framework that can serve both purposes all together. Besides, our framework is also superior in these aspects: i). Our framework can easily incorporate many DNN-architectures of RS ($u2i$), and increase the HitRate and Recall by a large margin. ii). We archive much better results in $i2u$ candidates generation compare to strong baselines. iii). We empirically show that our framework can diversify the generated candidates, and ensure fast convergence to better results.

1 Introduction

In the Internet era, E-commerce companies usually act as a platform to connect both users and merchants. They can collect huge amount of data of users' behavior on merchants' items, and utilize the data to serve them better, for example, to build better search/recommender/advertising systems.

When users browse the E-commerce websites/apps, they usually want to buy some desired items, or find something interesting, and that's what the search engine and recommender system (**RS**) are built for. Besides, the merchant usually wants to mine the potential users of its items, and then starts a campaign to prompt those users to buy the items. The advertising system has the functionality to help the merchant, and we may call it the potential users mining system (**PUMS**).

In an industrial large-scale RS, there are usually two stages, the candidates generation (**CG**) stage and the ranking stage (Covington et al., 2016). CG plays a very import role as it sets the upper bound of the recommender. A single CG method usually lacks diversity, so the industrial CG system usually consists of different subsystems to generate candidate items, for example, i). hot items, ii). items similar to users (Covington et al., 2016; Li et al., 2019), iii). items similar to clicked items (Linden et al., 2003), iv). items clicked by similar users (Wang et al., 2006).

The PUMS has been studied and applied in marketing community for many years (Bult & Wansbeek, 1995; Kim et al., 2005), and recently it is also introduced to social network to attract potential customers of companies (Pennacchiotti & Popescu, 2011; Pang et al., 2013). Similarly in E-commerce companies, it can be used to discover potential customers for merchants, brands and etc. Although it is widely used, people usually treat it as a simple binary classification problem, i.e., to predict whether a given user is the potential user or not. Models like LR, SVM, XGBoost and etc. (Hosmer Jr et al., 2013; Chang & Lin, 2011; Chen & Guestrin, 2016) are usually employed.

In this paper, we unify the two systems in our TotalRecall (**TR**) framework, and demonstrate the superiority using different metrics. Our main contributions are listed below:

- **Bidirectional Candidates Generation**: TR can be trained once and then used to generate candidate items ($u2i$) and users ($i2u$) all together without any additional operations. The-

oretically we show that the superiority is due to the modeling of joint probability of u and i.

- **Improving the HitRate and Recall of RS**: We compare to two different recommender algorithms, i.e., Matrix Factorization (**MF**) with Bernoulli distribution and sequential modeling with Multinormial distribution, and archive comparable or better results than MF's SOTA, and improve the HitRate and Recall by a large margin in sequential modeling.

- **Mining High-Quality Potential Users in PUMS**: TR mines potential users with higher accuracy compare to other methods. It can be applied in E-commerce and easily customized for various needs, for example, to mine users of a single item or a group of items, and the item could be the merchant, brand and etc.

- **Fast Convergence, and Diversified Candidates**: TR converges much faster compare to MF models, up to $16\times$ times. TR also increases the diversity of both generated users and items.

2 RELATED WORK

2.1 RECOMMENDER SYSTEM (RS)

RS has been studied for many years, and in the early years, Collaborative Filtering (**CF**) and its variants (Su & Khoshgoftaar, 2009) are widely adopted. Later its descendant MF (Funk) is proposed to solve the problem more elegantly with higher accuracy, and Probabilistic Matrix Factorization (**PMF**) (Mnih & Salakhutdinov, 2008) builds a solid theoretic foundation for MF based on probability theory.

Although MF performs very well in many datasets (Rendle et al., 2020), it is usually not adopted in industry. The modern industrial RS can involve up to billions of users and hundreds of millions of items, and consist of multiple stages, e.g., CG and ranking stages (Covington et al., 2016).

Various deep neural networks are adopted to tackle the complicated system, for example, in the CG stage, the problem is formulated as the multi-class classification, and users' and items' representations are detached with the two-tower architecture to balance the efficiency and accuracy in online serving (Covington et al., 2016; Li et al., 2019; Cen et al., 2020).

In the ranking stage, the problem is formulated as the binary classification, and various models has been developed: wide & deep model (Cheng et al., 2016) captures explicit and implicit feature crossing, Deep Interest Network (Zhou et al., 2018) and Deep User Perception Network (Ni et al., 2018) utilize attention mechanism (Bahdanau et al. (2014)) to capture users' short-term interests.

2.2 POTENTIAL USERS MINING SYSTEM (PUMS)

PUMS mines the potential users for given items. The 'item' could be anything that users can interact with, for example, an insurance product (Kim & Street, 2004), a company/business (Pennacchiotti & Popescu, 2011; Pang et al., 2013; Lo et al., 2016), a specific information (e.g., tweet) in social medias (Tang et al., 2015; Gui et al., 2019) and even another user (Guy, 2018). These problems are usually treated as binary classification and solved with tools like SVM, LR and etc. for each individual item independently (Hosmer Jr et al., 2013; Chang & Lin, 2011; Chen & Guestrin, 2016).

In the E-commerce company like Amazon, the 'item' could be a product, a brand, a product category, a merchant and etc, and the number of the 'items' range from thousands to hundreds of millions. It will be impractical to model each item individually, so we usually model the items all together using binary classification similar to Rendle et al. (2020), which will be stated in detail later in Sec. 5.

2.3 SAMPLED-SOFTMAX AND INFONCE LOSS

In the CG stage of RS, sampled-softmax (**SSM**) loss (Jean et al., 2015) is widely used with different background distributions, such as log-uniform distribution (Powers, 1998), empirical marginal distribution (Yi et al., 2019) and mixed distribution (Yang et al., 2020).

In contrastive learning, InfoNCE loss is proposed in Oord et al. (2018) to learn representations through self-supervision. Later it is widely adopted in CV (Chen et al. (2020)) and NLP (Gao et al. (2021)) and performs very well.

InfoNCE and SSM losses are both trying to solve multi-class classification of very large vocabulary. They both use negative sampling and can be written in the same analytical form:

$$l = \frac{1}{|\mathcal{D}|} \sum_{(x,y) \in \mathcal{D}} - \log \frac{\exp(f_\theta(x,y) - \log p_n(y|x))}{\exp(f_\theta(x,y) - \log p_n(y|x)) + \sum_{y' \in \mathbb{Y}_x} \exp(f_\theta(x,y') - \log p_n(y'|x))}, \quad (1)$$

where $(x,y) \in \mathcal{D}$ is the training data, $f_\theta(x,y)$ is the output of the neural network parametrized by θ, and $\mathbb{Y}_x$ contains hundreds or thousands of negative samples from background distribution $p_n(y|x)$. The main differences are that the $p_n(y|x)$ in SSM can be arbitrarily chosen, while in InfoNCE it is the empirical marginal distribution $\hat{p}_{\text{data}}(y)$.

Recently, InfoNCE loss is exploited in RS to optimize $\frac{p(y|x)}{p(y)}$ instead of $p(y|x)$, since it can be easily implemented with in-batch negative sampling and features of y can be fully utilized (Zhou et al., 2021).

3 METHOD

3.1 PROBLEM DEFINITION

In E-commerce companies, when a user u clicked an item i at time t, a record (u,i,t) was logged as the implicit feedback.

Given the raw logs $\{(u,i,t)\}$, there are usually two ways to process the data: one is to directly create a user-item interaction matrix $\boldsymbol{S}_{ui}$ with the value $s_{u,i} = 1$ if the (u,i) pair appears in the log (Su & Khoshgoftaar (2009)); the other is to formulate the problem as next-item prediction, i.e., from the raw log we create a dataset $\mathcal{D} = \{(x_{u,t}, y_{u,t}) : t \in \{1, 2, ..., T_u\} | u \in \{1, 2, ..., N\}\}$, where $x_{u,t} = \{y_{u,1:(t-1)}\}$ represents u's clicks prior to t-th click $y_{u,t}$ and T_u is the number of clicks of u (Covington et al. (2016)). We define the click sequence $x_{u,t}$ as the pseudo-user, so we can create a pseudo-user-item interaction matrix from $\mathcal{D}$, and all possible click sequences form the pseudo-user set.

Therefore, they both deal with the 2D interaction matrix $\boldsymbol{S}_{ui}$, irrespective of whether the u is a real user or pseudo-user or not. In the remaining of the paper, we will not distinguish between user and pseudo-user, and only focus on solving the $\boldsymbol{S}_{ui}$.

$\boldsymbol{S}_{ui}$ consists of all users as the row and all items as the column, and its entries are either 1 or unknown. Let's assume all users form the set $\mathbb{U} = \{u_1, u_2, ..., u_M\}$, and all items form the set $\mathbb{I} = \{i_1, i_2, ..., i_K\}$. Given a user $u \in \mathbb{U}$, we will generate candidate items from the item pool $\mathbb{I}$ (RS, $u2i$), while given an item $i \in \mathbb{I}$, we shall find out the potential users out of all users $\mathbb{U}$ (PUMS, $i2u$).

The candidates generation of RS and PUMS are of the opposite direction, and traditionally they are solved separately. But essentially they are both trying to estimate some kind of probabilities of the unknown entries in $\boldsymbol{S}_{ui}$, so we propose to model them jointly.

3.2 RECOMMENDER SYSTEM

In RS, there are usually two types of modeling objectives when dealing with $\boldsymbol{S}_{ui}$, and we briefly introduce them in the following sections (See App. A.1 for more details).

3.2.1 GAUSSIAN AND BERNOULLI DISTRIBUTION

The u-i interaction score $s_{u,i}$ of $\boldsymbol{S}_{ui}$ is treated as the random variable, and assumed to be i.i.d. following a certain distribution, for example, Gaussian (Mnih & Salakhutdinov (2008)) or Bernoulli (Johnson (2014); He et al. (2017); Rendle et al. (2020)) distributions.

3.2.2 Multinormial Distribution

Here the modeling objective is the random variable s_u, defined as the interacting item of u. For example, given the total number of interactions $N_u = \sum_{i \in \mathbb{I}} s_{u,i}$ of u, s_u is assumed to be sampled from a multinomial distribution $\text{Mult}(N_u, \boldsymbol{p}_u)$, where $\boldsymbol{p}_u$ is a K-dimensional vector whose elements are the probability and sum to 1 (Liang et al., 2018). Although not explicitly stated in many papers (Covington et al., 2016; Yi et al., 2019; Li et al., 2019; Cen et al., 2020), the multinormial distribution is actually assumed.

The modeling objectives in Sec. 3.2.1 and 3.2.2 are quite different, as the former is $s_{u,i}$ and the latter is s_u. In MF, we usually model $s_{u,i}$, while in the sequential modeling of the CG stage in industry, we model s_u. Later in Sec. 4.1, we will show that modeling s_u in MF can archive comparable or better results than modeling $s_{u,i}$, and boost the converging speed a lot.

3.3 Potential Users Mining System

The PUMS seems to be the twin system of RS, and similarly we could also define two modeling objectives $s_{u,i}$ and s_i, where s_i denotes the user who interacts with the item i. $s_{u,i}$ and s_i are assumed to follow Bernoulli and Multinormial distributions respectively. In Sec. 5 we will compare the two methods.

3.4 TotalRecall: Unification of RS and PUMS

Motivated by Sec. 3.2 and 3.3, we propose to model the two systems jointly. Specifically, the optimization objectives s_u and s_i in Sec. 3.2.2 and 3.3 are formulated in one framework and optimized together. Later we show that by properly choosing the model architecture and loss function, we are treating u and i equally and modeling the joint probability.

Figure 1: Model architecture of TotalRecall. Our framework will make to dot product $\phi_\theta(u, i)$ converge to the logarithm of the joint probability $p(u, i)$, and thus can be directly applied in RS to emulate the conditional probability $p(i|u)$, and also in PUMS to replace $p(u|i)$.

3.4.1 Model Architecture

We choose the classical two-tower architecture (Huang et al., 2013; Covington et al., 2016; Rendle et al., 2020) for two reasons: one is that users and items can be treated equivalently, and the other is that no feature crossing occurs before the final logits (See Fig. 1). So users' and items' embeddings can be inferred separately, and then approximate nearest neighbor (ANN) (Liu et al., 2004) search algorithm can be applied in online serving .

The output of two towers are d-dimensional vectors $\boldsymbol{u} = f_\theta(u) \in \mathbb{R}^d$ and $\boldsymbol{i} = g_\theta(i) \in \mathbb{R}^d$, where θ is the model parameter. The dot product $\phi_\theta(\boldsymbol{u}, \boldsymbol{i}) = \langle \boldsymbol{u}|\boldsymbol{i} \rangle$, or the function of it is used as the sufficient statistics of the probability distributions defined in Sec. 3.2 and 3.3 (Check App. A.1 for

details). We find that l2-normalize $\boldsymbol{u}$ and $\boldsymbol{i}$ and then rescale the dot product by the temperature τ will lead to better and robust results:

$$\phi_\theta(\boldsymbol{u}, \boldsymbol{i}) = \frac{1}{\tau} \frac{\langle \boldsymbol{u}|\boldsymbol{i} \rangle}{||\boldsymbol{u}||_2 ||\boldsymbol{i}||_2}. \tag{2}$$

3.4.2 Loss Function

We propose the Bi-InfoNCE loss:

$$
\begin{aligned}
l = \frac{1}{|\boldsymbol{S}_{u,i}|} \sum_{u \in \mathbb{U}, i \in \mathbb{I}, s_{u,i}=1} & -\log \frac{\exp(\phi_\theta(u,i) - \log q(i))}{\exp(\phi_\theta(u,i) - \log q(i)) + \sum_{i' \in \mathbb{I}_u} \exp(\phi_\theta(u,i') - \log q(i'))} \\
& -\log \frac{\exp(\phi_\theta(u,i) - \log \hat{q}(u))}{\exp(\phi_\theta(u,i) - \log \hat{q}(u)) + \sum_{u' \in \mathbb{U}_i} \exp(\phi_\theta(u',i) - \log \hat{q}(u'))}
\end{aligned}, \tag{3}
$$

where $\mathbb{I}_u \subset \mathbb{I}$ and $\mathbb{U}_i \subset \mathbb{U}$ contain hundreds or thousands of in-batch negative samples, and $q(i)$ and $\hat{q}(u)$ are empirical marginal distribution calculated using the training data $\boldsymbol{S}_{ui}$. It can be shown that optimizing this loss will make $\phi_\theta(u,i)$ converge to $\log \hat{p}_{\text{data}}(u,i)$ (See App. A.3 for details.).

If we only optimize the first part of Eq. 3, $\phi_\theta(u,i)$ will converge to $\log \hat{p}_{\text{data}}(i|u)$, and optimizing only the second part will let $\phi_\theta(u,i)$ converge to $\log \hat{p}_{\text{data}}(u|i)$. We refer to the two cases as Uni-InfoNCE losses.

4 Experiments: RS

As stated in Sec. 3.2, two types of modeling objective are well studied in literature, and usually they use different datasets and baselines. So we compare our results with them separately using different datasets. The details of the datasets and processing methods can be found in App. A.4.

4.1 MF with Bernoulli Distribution

We compare TR to MF with Bernoulli distribution (MF$_b$) in Rendle et al. (2020), as described in Sec. 3.2.1. Our implementation of MF$_b$ is a bit different from Rendle et al. (2020): we implement it using tensorflow (Abadi et al., 2016) with Adam optimizer (Kingma & Ba, 2014).

We tried L2 regularization but failed to obtain the results reported by Rendle et al. (2020). We also tried dropout (Srivastava et al., 2014), but it was unstable and need to be re-tuned for different dimensions d. Finally we find that the $\phi_\theta(\boldsymbol{u}, \boldsymbol{i})$ defined in Eq. 2 can actually act as a kind of regularization, so we use it rather than the one defined by Eq. (2) in Rendle et al. (2020).

We use Movielens-1m and Pinterest datasets, and the evaluation metrics are HiteRate@10 and NDCG@10. MF$_b$ and TR have the same two-tower architecture and same number of parameters, and the key differences are the training data and the optimizing objectives: MF$_b$ uses explicit negative sampling and optimize the binary cross-entropy loss, and TR uses implicit in-batch negative sampling and Bi-InfoNCE loss.

The hyper-parameters τ and batch-size are chosen using the validation data. For Movielens-1m, we use $\tau = 0.125$, batch-size $= 4096$ for MF$_b$, and $\tau = 0.111$, batch-size $= 512$ for TR. For Pinterest, we use $\tau = 0.143$, batch-size $= 8192$ for MF$_b$, and $\tau = 0.167$, batch-size $= 8192$ for TR. We have $d \in \{16, 32, 64, 96, 128, 196\}$ for a comprehensive comparison. The results are shown in Fig. 2 and Tab. 1.

In general, MF$_b$ and TR are comparable, and TR is slightly better in ranking as measured by NDCG@10. When measuring the training efficiency, TR converges to the optima up $16\times$ times faster than MF$_b$ (See Fig. 3 in Appendix), so it is more practical to use TR in industrial applications with huge amount of data. Besides, the diversity of TR is also larger than MF$_b$ as shown in Fig. 3.

Figure 2: Comparison of results of MF given by Bernoulli distribution and Multinormial distribution. 'MF by Rendle' is from Rendle et al. (2020), 'MF by us' is our implementation. In general these results are quite close and outperform NCF by a large margin (Rendle et al. (2020)). At the same time, the ranking performance of TR is better than MF as measured by NDCG.

Table 1: Baselines from Dacrema et al. (2021) and Rendle et al. (2020) and our results. The best results are highlighted in bold, the second best result is underlined.

Method	Movielens		Pinterest		Result from
	HR@10	NDCG@10	HR@10	NDCG@10	
Popularity	0.4533	0.2542	0.2740	0.1409	Dacrema et al. (2021)
SLIM	0.7162	0.4468	0.8679	0.5601	Dacrema et al. (2021)
iALS	0.7109	0.4382	0.8761	0.5590	Dacrema et al. (2021)
MLP+GMF	0.7093	0.4349	0.8777	0.5576	Dacrema et al. (2021)
MF_b by Rendle	**0.7294**	0.4523	0.8895	0.5794	Rendle et al. (2020)
MF_b (ours)	0.726	0.4505	0.8925	0.5838	Fig. 2
TR (ours)	0.7281	**0.4541**	**0.8936**	**0.5866**	Fig. 2

4.2 SEQUENTIAL MODELING WITH MULTINORMIAL DISTRIBUTION

We compare TR to the sequential modeling with Multinormial distribution, as described in Sec. 3.2.2. This modeling method is usually used in the CG stage of industrial large-scale RS, because it can deal with huge amount of data very efficiently, and yield good results.

For simplicity, we use the popular Youtube DNN (Covington et al., 2016) implemented in Cen et al. (2020) as the backbone architecture of TR. Other complicated architectures can be easily incorporated into TR framework.

We use the same datasets as Cen et al. (2020) for a fair comparison, i.e., Amazon books data [1] and Taobao click data in Tianchi competition [2]. The data is split into train, validation and test data. The training data is usually processed as next-item prediction as in Sec. 3.1, and we extend it into

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[1]http://jmcauley.ucsd.edu/data/amazon/index.html
[2]https://tianchi.aliyun.com/dataset/dataDetail?dataId=649&userId=1

Table 2: For Amazon books data, we use $\tau = 0.1$, batch-size $= 128$. For Taobao data, we use $\tau = 0.067$, batch-size $= 2048$. ComiRec-SA and ComiRec-DR are two multi-interest models proposed in Cen et al. (2020).

	Amazon Books Metrics@50		Taobao Metrics@50	
	Recall	Hit Rate	Recall	Hit Rate
Popular	2.400	5.226	0.735	9.309
YouTube DNN	7.312	15.894	6.172	39.108
ComiRec-SA	8.467	17.202	9.462	51.064
ComiRec-DR	8.106	17.583	9.818	52.418
Youtube [SSM with l2-norm]	9.37 (+28%)	19.25 (+21%)	6.9 (+12%)	42.87 (+10%)
TR-Youtube [Uni-InfoNCE $u2i$]	10.34 (+41%)	21.15 (+33%)	**7.15 (+16%)**	**43.79 (+12%)**
TR-Youtube [Bi-InfoNCE]	10.12 (+38%)	20.554 (+29%)	7.14 (+16%)	43.57 (+11%)
TR-Youtube [next-7-prediction]	**11.571 (+58%)**	**23.221 (+46%)**	-	-

next-n-item prediction, i.e., instead of predicting only the next item, we predict all the next n items. The results are shown in Tab. 2. More results are shown in Fig. 4 and 5 in Appendix.

Our experiments show that TR surpasses baselines in the three aspects. i). **Better results by a large margin**: TR achieves much better results in terms of Recall and HitRate as shown in Tab. 2. The improvement is mainly attributed to l2-normalization and better training data, i.e., next-n-prediction. Specifically, l2-normalization acts like a regularizer, as it confines $\phi_\theta(u, i)$ inside $[-1/\tau, 1/\tau]$. Next-n-prediction alters the distribution of the training data so that it gets close to the test data (See Fig. 6 in Appendix). ii). **Improved diversity**: We tried SSM with different background distributions, and compare with Uni-InfoNCE and Bi-InfoNCE, and found that Bi-InfoNCE gives better overall diversity as measured by the number of distinct items and categories of items (See Fig. 4 in Appendix). This could be due to that Bi-InfoNCE can build a more coherent vector space for u and i. iii). **Faster convergence**: Compare to SSM or Uni-InfoNCE without l2-normalization, adding l2-normalization or using Bi-InfoNCE will make the models learn faster (See Fig. 4 in Appendix). This is because l2-normalization will restrict the vector space that $\boldsymbol{u}$ and $\boldsymbol{i}$ could explore, and Bi-InfoNCE can utilize the data more efficiently.

5 EXPERIMENTS: PUMS

In E-commerce, there are usually two practical scenarios of $i2u$ candidates generation: one is to mine the potential users for a single item, and the other is to find users for a group of similar items. Previously, the problem is usually formulated as the binary classification for each individual case, but it is not generally applicable because the number of items or groups are quite large, and it is impractical to build so many models.

One solution is to merge all the binary classification models into one, just like MF_b as in Sec. 3.2.1 and 3.3. The other is our TR framework.

We use 4 variants of MF_b as the baselines. These variants are due to different negative sampling methods, i.e., for a given positive (u, i) pair, we sample the negative pairs in these ways: i). 'MF_b [0:8]'[3], we randomly sample 8 is from the item set $\mathbb{I}$, and construct 8 negative pairs with the given u; 2). 'MF_b [8:0]', we sample 8 us from the user set $\mathbb{U}$, and construct 8 negative pairs with the given i; 3). 'MF_b [4:4]', we sample 4 us and 4 is, and construct 8 negative pairs with the given i and u respectively; 4). similar to 3), but the negative samples are doubled.

5.1 DATASET AND EVALUATION METRICS

We use Movielens-1m because it is also used in MF_b of RS, and it can be used to mine the potential users of both the single item and the group of similar items.

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[3]This sampling method is actually used in MF_b in RS by Rendle et al. (2020)

Table 3: Overall performance of mining the potential users of a single item. The % is omitted for precision and recall. The hyper-parameters of MF_b are batch-size $= 4096$ and $\tau = 0.125$, and for TR they are batch-size $= 512$ and $\tau = 0.125$. We use $d = 96$ for all models for a fair comparison. The diversity values of models with very low accuracy are omitted.

model	precision@10	recall@10	distinct users
MF_b [0:8]	1.47	5.61	-
MF_b [8:0]	4.44	12.82	2046
MF_b [4:4]	3.12	9.28	-
MF_b [8:8]	3.02	8.64	-
TR [Uni-InfoNCE $u2i$]	1.19	4.51	-
TR [Uni-InfoNCE $i2u$]	4.35	12.78	2064
TR [Bi-InfoNCE]	**4.58**	**13.82**	**2202**

Movielens-1m records 6040 users and 3706 movies. The data is split into training, validation and test data, and we use the validation data to select the proper model configurations. The final results are reported on the test data.

We use precision@10 and recall@10 to evaluate the accuracy of different algorithms, i.e., we mine the top 10 users for a single item or a group of items, and then evaluate the precision and recall. We count the distinct users of the overall results to measure the diversity. (See App. A.5 for details about the dataset and metrics.)

5.2   POTENTIAL USERS OF A SINGLE ITEM

We first select movies which have been watched by at least 50 users, and it results in 2514 movies. For each of these movies, we randomly pick 1% of its users to form the valid and test datasets, with half of the movies as the validation data and the other half as the test data (See App. A.5.). The remaining data is used to train the model, and the validation data is for selecting the best hyper-parameters, and the results are reported on the test data.

The results are shown in Tab. 3. 'TR [Bi-InfoNCE]' archives the best results in terms of the accuracy and diversity. High diversity implies that the advertisements can reach more users, even the non-active users, thus alleviate the advertising fatigue.

Besides, TR uses the same training data and model configurations for both RS and PUMS, and archives the best results in both cases. The learned u/i representations can be applied to the two systems without any additional modifications. In contrast, MF_b's modeling objective (Eq. 4) seems to treat u and i equally, but the outcomes depend highly on the negative sampling methods (See Tab. 3). We tried different sampling methods (e.g., 'MF_b [4:4]' and 'MF_b [8:8]') in the hope that MF_b could do well in both $u2i$ and $i2u$, but it fails to give comparable results.

Last but not least, TR learns $16\times$ times faster than MF_b. (See Fig. 7 in Appendix).

5.3   POTENTIAL USERS OF A GROUP OF ITEMS

In practice, movies of different genres and different popularity will behave very differently, e.g., precision and recall of popular Action movies and unpopular Western movies will differ a lot. Movielens have 18 genres, and we divide the movies of the same genre into 3 categories based on their popularity, so we can split the chosen movies into 54 groups (See App. A.5 for the exact definition of groups).

Given a group and its affined items, we define its potential users this way: if a user interacts with one or more items in the group (excluding the items he has interacted previously), then he will be the potential users of the group. For example, given the group $\mathbb{G} = \{i_1, i_2, i_3\}$ and the user u_1, if u_1 has interacted with i_1 in the historical data, then we cannot pick him as the potential user; if in the future data, u_1 interact with i_2 or i_3, then he will be regarded as the potential user of $\mathbb{G}$.

Table 4: Overall performance of mining the potential users of a group of items. The % is omitted for precision and recall. The hyper-parameters of MF_b are batch-size $= 4096$ and $\tau = 0.125$, and for TR batch-size $= 512$ and $\tau = 0.111$. We use $d = 96$ for all models.

model	precision@10	recall@10	distinct users
MF_b [0:8] *mean*	5.93	1.52	-
MF_b [8:0] *sum*	5.93	2.58	-
MF_b [8:0] *max*	14.63	4.23	-
MF_b [8:0] *mean*	17.04	4.57	246
MF_b [4:4] *mean*	11.11	2.63	-
MF_b [8:8] *mean*	12.78	3.05	-
TR [Uni-InfoNCE $u2i$] *mean*	4.63	1.38	-
TR [Uni-InfoNCE $i2u$] *mean*	16.85	7.25	**262**
TR [Bi-InfoNCE] *sum*	12.41	6.79	-
TR [Bi-InfoNCE] *max*	16.48	7.01	-
TR [Bi-InfoNCE] *mean*	**20.56**	**7.58**	258

Different groups have different number of movies, e.g., the group 'Drama-top10%' contains 93 movies, while 'Documentary top10%' has only 3 movies, and their precision and recall will also differ a lot. We report the averaged precision and recall over all groups in Tab. 4.

For small dataset like movie-lens-1m, the model generates the potential users of a group this way: for each item in the group, we first calculate $\phi_\theta(\boldsymbol{u}, \boldsymbol{i})$ of Eq. 2, and then the score $\hat{p}_{TR}(\boldsymbol{u}, \boldsymbol{i}) = \exp(\phi_\theta(\boldsymbol{u}, \boldsymbol{i}))$ for TR and $\hat{p}_{MF}(\boldsymbol{u}, \boldsymbol{i}) = \sigma(\phi_\theta(\boldsymbol{u}, \boldsymbol{i}))^4$ for MF_b, with respect to the candidate users. Thus each candidate user will have several scores, and then we aggregate the scores to obtain a match score between the user and the group, and finally pick the top-k users. The aggregation methods could be *max*, *mean* or *sum*.

In Tab. 4, 'MF_b [0:8]' and 'TR [Uni-InfoNCE $u2i$]' are specifically for $u2i$ CG of RS, so they give the worst results here. Models tailored for $i2u$ ('MF_b [8:0]' and 'TR [Uni-InfoNCE $i2u$]') and the general model for bidirectional CG ('TR [Bi-InfoNCE]') perform much better.

The aggregation methods also affect the accuracy, and *mean* > *max* > *sum*. If a user has scores with many items of the group, the *sum* could be high even if individual scores are low, and this also implies that the user has few interactions with the items of the group in the historical data. So it would not be suitable that *sum* ranks this user high. In contrast, *mean* and *max* will not have this problem, and *mean* considers more scores than just the *max* one and gives best results.

6 CONCLUSION

In this paper, CF and the sequential modeling (i.e., next-item prediction) of RS, and PUMS are abstracted into a unified u-i interaction matrix $\boldsymbol{S}_{ui}$, and thus are treated equivalently as deriving some probabilities for the unknown entries from the known entries of $\boldsymbol{S}_{ui}$. We also show their connections and differences based on probability theory. Built upon these observations, we propose the TR framework to unify them and solve $\boldsymbol{S}_{u,i}$ all together.

In TR, u and i are treated equally, and the joint probability $p(u, i)$ is actually derived, instead of the conditional probability $p(i|u)$ or $p(u|i)$. Therefore, the learned representations of u and i in TR can be used in both $u2i$ and $i2u$ CG.

Our extensive experiments show that TR can archive comparable and better results in each domain, and learns $16\times$ times faster than MF_b. Besides, TR generates diversified candidates.

In the future, we plan to study the vector space of TR in depth, and try to unify different objects and users into one space, for example, products, merchants, brands, categories of products. In such a space, everything is linked, and candidates generation can be applied on any pair of objects.

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[4]$\sigma(\cdot)$ is the sigmoid function.

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A APPENDIX

A.1 DISTRIBUTIONS

In Sec. 3.1 we define the interaction matrix $\boldsymbol{S}_{ui}$, and it has the known entries with value 1 and unknown entries. Here we define a corresponding matrix $\boldsymbol{P}$ of the same shape, and its entries are the probabilities estimated by a certain algorithm.

In Sec. 3.2.1, the corresponding probability matrix $\boldsymbol{P}_{\text{MF}}$ is defined as follows:

$$p_{u,i} := p(s_{u,i} = 1|u, i), \tag{4}$$

where $\sum_{s_{u,i} \in \{0,1\}} p(s_{u,i}|u, i) = 1$.

Here we can assume $s_{u,i}$ follows Gaussian distribution: $s_{u,i} \sim \mathbf{N}(\phi(\boldsymbol{u}, \boldsymbol{i}), \hat{\sigma}^2)$, or Bernoulli distribution: $s_{u,i} \sim \mathbf{B}(\sigma(\phi(\boldsymbol{u}, \boldsymbol{i})))$, where $\sigma(\cdot)$ is the sigmoid function.

In Sec. 3.2.2, the probability matrix $\boldsymbol{P}_{u2i}$ is:

$$p_{u,i} := p(\boldsymbol{s}_u = i|u), \tag{5}$$

where $\sum_{\boldsymbol{s}_u \in \mathbb{I}} p(\boldsymbol{s}_u|u) = 1$.

For a given user u, $\boldsymbol{s}_u \sim \text{Mult}(N_u, \boldsymbol{p}_u)$, where $\boldsymbol{p}_u = (p_{u1}, p_{u2}, ..., p_{uK})^T$ is a K-dimensional vector, and its element p_{ui} is defined as below:

$$p_{ui} = \frac{\exp \phi_\theta(\boldsymbol{u}, \boldsymbol{i})}{\sum_{\boldsymbol{j} \in \mathbb{I}} \exp \phi_\theta(\boldsymbol{u}, \boldsymbol{j})}. \tag{6}$$

In Sec. 3.3 of PUMS, we can define the specific $\boldsymbol{P}_{\text{MF}}$ and $\boldsymbol{P}_{i2u}$ by emulating Eq. 4 and 5. For example, $\boldsymbol{P}_{i2u}$ can be defined as below:

$$p_{u,i} := p(\boldsymbol{s}_i = u|i), \tag{7}$$

where $\boldsymbol{s}_i$ denotes the user who will interact with the item i, and $\sum_{\boldsymbol{s}_i \in \mathbb{U}} p(\boldsymbol{s}_i|i) = 1$, and $\boldsymbol{s}_i \sim \text{Mult}(N_i, \boldsymbol{p}_i)$ follows the Multinormial distribution, where $\boldsymbol{p}_i = (p_{1i}, p_{2i}, ..., p_{Mi})^T$ is a M-dimensional vector.

A.2 LOSS FUNCTIONS

In this paper, we focus on Bernoulli and Multinormial distributions, because they usually lead to better results than Gaussian distribution (He et al. (2017); Rendle et al. (2020)). Following the maximum likelihood estimation (MLE) principle, the loss for Bernoulli distribution is:

$$l = -\frac{1}{N} \sum_{u \in \mathbb{U}, i \in \mathbb{I}} s_{u,i} \log \sigma(\phi_\theta(u, i)) + (1 - s_{u,i}) \log(1 - \sigma(\phi_\theta(u, i))), \tag{8}$$

where $s_{u,i} \in \{0, 1\}$, and $s_{u,i} = 1$ are the positive entries in $\boldsymbol{S}$, and $s_{u,i} = 0$ are negative samples randomly sampled from the missing entries in $\boldsymbol{S}$, and N is the total number of records in the training data.

The loss for Multinormial distribution is softmax-cross-entropy loss:

$$l = \frac{1}{|\boldsymbol{S}_{u,i}|} \sum_{u \in \mathbb{U}, i \in \mathbb{I}, s_{u,i}=1} -\log \frac{\exp \phi_\theta(u, i)}{\sum_{i' \in \mathbb{I}} \exp \phi_\theta(u, i')}. \tag{9}$$

In practice, the vocabulary $\mathbb{I}$ can be very large so that calculating the partition function $\sum_{i' \in \mathbb{I}} \exp \phi_\theta(u, i')$ becomes impractical. SSM and InfoNCE loss can be used to solve this problem:

$$l = \frac{1}{|\boldsymbol{S}_{u,i}|} \sum_{u \in \mathbb{U}, i \in \mathbb{I}, s_{u,i}=1} -\log \frac{\exp(\phi_\theta(u, i) - \log p_n(i|u))}{\exp(\phi_\theta(u, i) - \log p_n(i|u)) + \sum_{i' \in \mathbb{I}_u} \exp(\phi_\theta(u, i') - \log p_n(i'|u))}, \tag{10}$$

where $\mathbb{I}_u \subset \mathbb{I}$ contains hundreds or thousands of negative samples, and $p_n(i|u)$ is a predefined background distribution. It has been shown that optimizing Eq. 10 will make $\phi_\theta(u, i)$ converge to $\log \hat{p}_{\text{data}}(i|u)$ (Jean et al. (2015); Oord et al. (2018)).

A.3 BI-INFONCE LOSS

Here we prove that $\phi_\theta(u, i)$ in Eq. 3 converges to $\log \hat{p}_{\text{data}}(u, i)$.

In Eq. 3, in the optimum of the first part, we will have $\frac{\exp(\phi_\theta(u,i))}{q_i} \propto \frac{\hat{p}_{\text{data}}(i|u)}{q_i}$, so we can assume:

$$\phi_\theta(u, i) = \log \hat{p}_{\text{data}}(i|u) + f(u) = \log \hat{p}_{\text{data}}(u, i) - \log \hat{p}_{\text{data}}(u) + f(u)$$

for a given u and any i. Similarly, in the optimum of the second part, $\phi_\theta(u, i) = \log \hat{p}_{\text{data}}(u, i) - \log \hat{p}_{\text{data}}(i) + g(i)$ for a given i and any u.

Thus, for any u and i, this will always hold: $-\log \hat{p}_{\text{data}}(u) + f(u) \equiv -\log \hat{p}_{\text{data}}(i) + g(i)$, so it must be some constant. Then we have $\phi_\theta(u, i) = \log \hat{p}_{\text{data}}(u, i) + C$, where C is some constant that is independent of u and i. And when $\phi_\theta(u, i)$ converges to $\log \hat{p}_{\text{data}}(u, i)$, both parts in Eq. 3 can reach their optima.

A.4 EXPERIMENT RESULTS: RS

A.4.1 MF WITH BERNOULLI DISTRIBUTION

We compare to MF in Rendle et al. (2020) using the same datasets: binarized Movielens-1m (Harper & Konstan, 2015) and a dataset from Pinterest (Geng et al., 2015).

For each user, the last item is held out as the test set, and the second last is held out as the validation set, and the remaining as the training set. We use the validation set and training set to select the best hyper-parameters, and then re-train the model using both training and validation sets.

Each user has his own candidates pool, and it consists of the withheld item and 99 sampled negative items. During evaluation, the algorithm will score the 100 items and rank them by the score.

Two evaluation metrics are employed to measure the performance of top-N ranked items:

$$\text{HitRate@}N = \frac{1}{|\mathbb{U}|} \sum_{u \in \mathbb{U}} \delta(|\hat{\mathcal{I}}_{u,N} \cap \mathcal{I}_u| > 0), \tag{11}$$

where $\hat{\mathcal{I}}_{u,N}$ denotes the top-N ranked items for u, $\mathcal{I}_u$ is the set of testing items, and $\delta(\cdot)$ is the indicator function.

$$\text{NDCG@}N = \frac{1}{|\mathbb{U}|} \sum_{u \in \mathbb{U}} \frac{1}{\log(1 + r_u)}, \tag{12}$$

where r_u is the rank of the withheld item in the top-N items for u.

A.4.2 SEQUENTIAL MODELING WITH MULTINORMIAL DISTRIBUTION

We compare to the models implemented in ComiRec (Cen et al., 2020). ComiRec provides the codes and two preprocessed datasets: Amazon books data (Ni et al., 2019) and Taobao click data (Zhu et al., 2018). So we use the same datasets and evaluation metrics for a fair comparison.

We use HitRate@N and Recall@N to measure the accuracy. HitRate@N is defined in Eq. 11, and Recall@N is defined below:

$$\text{Recall@}N = \frac{1}{|\mathbb{U}|} \sum_{u \in \mathbb{U}} \frac{|\hat{\mathcal{I}}_{u,N} \cap \mathcal{I}_u|}{|\mathcal{I}_u|}. \tag{13}$$

Metrics 'Distinct items@N' counts the distinct items of all users' top-N recommended list, and 'Distinct cates@N' counts the distinct categories of these items. They measure the diversity of the recommendation results.

The comparing methods include the following:

- **MostPopular** recommends the most popular items to all users.

Figure 3: Comparison of the converging speed and diversity of MF modeled with Bernoulli distribution (MF) and Multinormial distribution (TR). The x-axis is the data throughput, i.e., the number of records consumed by the model, and the y-axis is the metric measured on the test data. For Movie-lens, TR is about $16\times$ times faster, and for Pinterest it is about $10\times$ times.

- **YouTube DNN** (Covington et al., 2016) is a simple and very efficient neural network model adopted in the CG stage of the large-scale industrial RS.
- **ComiRec-SA & ComiRec-DR** (Cen et al., 2020) use self-attention (Vaswani et al., 2017) or dynamic routing (Sabour et al., 2017) to explicitly incorporate users' diverse interests in the model's architecture to increase accuracy and diversity.

Figure 4: Comparison of accuracy and diversity metrics of different methods on Amazon books and Taobao data. HitRate@50 and Recall@50 measure the accuracy, and Distinct items@50 and Distinct cates@50 measure the diversity. '∗_temp' means the users and items representations u and i are l2-normalized, and then their dot product is rescaled with temperature $\tau = 0.067$. By this way, the model converges much faster to higher accuracy. As for diversity, Bi-InfoNCE surpass Uni-InfoNCE and SSM by a large margin.

Figure 5: Results of Next-n-prediction for Amazon data. The improvement of accuracy is substantial when $n <= 5$.

Figure 6: KL Divergence between two marginal distributions of items: $\hat{p}_{\text{test}}(i)$ of test data and $\hat{p}_{\text{data}}(i)$ of next-n training data. Although they are not the full distributions of u and i, to a certain extent they can reveal the discrepancy between the distributions of the training data and the test data. In Amazon data, if we increase n, the discrepancy becomes smaller, and the accuracy also increases (See Fig. 5). In Taobao data, the discrepancy gets larger when we increase n, and in experiments the accuracy does not increase.

Table 5: Statistics of the split Movielens datasets in PUMS experiments.

	# records	# movies	# users
train (w/o negative samples)	990296	3076	6040
valid	5125	1257	2698
test	4788	1257	2547

A.5 EXPERIMENT RESULTS: PUMS

There are different ways of creating the validation and test datasets, such as randomly picking 10 users for each chosen item or each group of items.

Here we choose to holdout 1% users for the practical reason: usually we mine the potential users based on the historical behaviors and then deliver advertisement to them in the future, and the implicit assumption is that the distribution of the future is close to the past, i.e., popular items in the past will be bought by more users in the future, and vice versa. So we holdout validation and test datasets in accordance with the overall distribution to emulate the practical scenario.

A.5.1 POTENTIAL USERS OF A SINGLE ITEM

We create the training, validation and test data as described in Sec. 5.2. The statistics of the resulting datasets is shown in Tab. 5.

Our evaluation metrics of accuracy are Precision@N and Recall@N:

$$\text{Precision@}N = \frac{1}{\mathbb{I}_{\text{test}}} \sum_{i \in \mathbb{I}_{\text{test}}} \frac{|\hat{\mathcal{U}}_{i,N} \cap \mathcal{U}_i|}{N},$$

where $\hat{\mathcal{U}}_{i,N}$ denotes the top-N ranked users for i and $\mathcal{U}_i$ is the set of users for the testing item i.

$$\text{Recall@}N = \frac{1}{\mathbb{I}_{\text{test}}} \sum_{i \in \mathbb{I}_{\text{test}}} \frac{|\hat{\mathcal{U}}_{i,N} \cap \mathcal{U}_i|}{|\mathcal{U}_i|}.$$

We count the distinct users of all the test items to measure the diversity.

Figure 7: Comparison of the convergence speed between MF and TR. The x-axis is in log scale. We can see that TR can obtain better results much faster.

A.5.2 POTENTIAL USERS OF A GROUP OF ITEMS

For a given genre, we define the popularity of its movies in this way: we first rank the movies based on the number of users who have watched them, and then we pick the top/middle/bottom 10% movies as different groups. So we obtained 54 groups from 18 genres.

A.6   EQUIVALENCE BETWEEN BERNOULLI DISTRIBUTION AND MULTINORMIAL DISTRIBUTION ON MODELING JOINT PROBABILITY

Here we show that by properly choosing the training data distribution, $\phi_\theta(u, i)$ in Eq. 2 is actually approaching the conditional distribution $p(i|u)$ or $p(u|i)$, or joint distribution $p(u, i)$.

Our derivation is inspired by Noise Contrastive Estimation (Gutmann & Hyvärinen, 2010).

In the modeling with Bernoulli distribution, we have two sets of samples, $\mathbb{X}$ and $\mathbb{Y}$. $\mathbb{X}$ is the set of positive samples and $\mathbb{Y}$ is the set of negative samples randomly sampled based on a certain distribution $p_n(\cdot)$.

Assume $\mathbb{X} = \{\boldsymbol{x}_1, \boldsymbol{x}_2, ..., \boldsymbol{x}_L\}$ contains L samples, and $\mathbb{Y} = \{\boldsymbol{y}_1, \boldsymbol{y}_2, ..., \boldsymbol{y}_T\}$ contains T samples, and $\mathbb{Z} = \mathbb{X} \cup \mathbb{Y} = \{\boldsymbol{z}_1, \boldsymbol{z}_2, ..., \boldsymbol{z}_{L+T}\}$ contains all the $L+T$ samples. Here $\boldsymbol{x}_l := (u, i)$, $\boldsymbol{y}_t := (u, i)$ and $\boldsymbol{z}_j := (u, i)$, where $u \in \mathbb{U}$ and $i \in \mathbb{I}$. We assign each sample $\boldsymbol{z}_j$ a binary class C_j: $C_j = 1$ if $\boldsymbol{z}_j$ comes from $\mathbb{X}$, and $C_j = 0$ if $\boldsymbol{z}_j$ is from $\mathbb{Y}$.

We assume the joint probability of positive samples in $\mathbb{X}$ is parameterized by θ is $p_{\text{model}}(u, i; \theta) = p_{\text{model}}(\boldsymbol{z}; \theta)$. So we have the conditional probabilities:

$$p(\boldsymbol{z}|C = 1; \theta) = p_{\text{model}}(\boldsymbol{z}; \theta) \qquad p(\boldsymbol{z}|C = 0; \theta) = p_n(\boldsymbol{z}). \tag{14}$$

The posterior probabilities are:

$$p(C = 1|\boldsymbol{z}; \theta) = \frac{p_{\text{model}}(\boldsymbol{z}; \theta)P(C = 1)}{p_{\text{model}}(\boldsymbol{z}; \theta)P(C = 1) + p_n(\boldsymbol{z})P(C = 0)} = \frac{1}{1 + \exp(-G(\boldsymbol{z}; \theta))}, \tag{15}$$

where

$$G(\boldsymbol{z}; \theta) = \log \frac{p_{\text{model}}(\boldsymbol{z}; \theta)P(C = 1)}{p_n(\boldsymbol{z})P(C = 0)}, \tag{16}$$

and we also have

$$p(C = 0|\boldsymbol{z}; \theta) = \frac{1}{1 + \exp(G(\boldsymbol{z}; \theta))}.$$

So the log-likelihood is:

$$l(\theta) = \sum_{j=1}^{L+T} C_j \log P(C_j = 1|\boldsymbol{z}_j; \theta) + (1 - C_j) \log P(C_j = 0|\boldsymbol{z}_j; \theta).$$

Through optimizing the binary classification using samples in $\mathbb{Z}$ and the corresponding binary classes C, we are actually recovering the MF with Bernoulli distribution defined in Sec. 3.2.1. The dot product $\phi_\theta(u, i)$ will converge to $G(\boldsymbol{z}; \theta)$ in Eq. 16:

$$\phi_\theta(u, i) \to \log \frac{p_{\text{model}}(\boldsymbol{z}; \theta)P(C = 1)}{p_n(\boldsymbol{z})P(C = 0)}. \tag{17}$$

Different negative sampling strategies will lead to very different optimal $\phi_\theta(u, i)$. For example, if we randomly sample n items for each positive (u, i) pair to form negative samples with the u, then we have $p_n(\boldsymbol{z}) = p_n(u, i) = \hat{p}_{\text{data}}(u) \cdot 1/K$, where $\hat{p}_{\text{data}}(u)$ is the empirical marginal probability of the positive samples. Substitute $p_n(\boldsymbol{z})$ into Eq. 17, we have

$$\phi_\theta(u, i) \approx \log \frac{p_{\text{model}}(u, i; \theta)}{\hat{p}_{\text{data}}(u)} + C \approx \log p_{\text{model}}(i|u; \theta) + C.$$

Similarly, if we randomly sample n users for each positive (u, i) pair to form negative samples with the i, then $\phi_\theta(u, i)$ will converge to the conditional probability $\log p_{\text{model}}(u|i; \theta)$. And if the negative samples are randomly sampled from all users and items globally, then $\phi_\theta(u, i)$ will converge to the joint probability $\log p_{\text{model}}(u, i; \theta)$.

Therefore, we show that MF with Bernoulli distribution and Multinormial distribution can be equivalent if we choose the proper negative sampling strategies.