Impact of realistic properties of the point spread function on classification tasks to reveal a possible distribution shift

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Abstract

Image classification is a long-standing task in computer vision with deep neural networks (DNN) producing excellent results on various challenges. However, they are required not only to perform highly accurate on benchmarks such as ImageNet, but also to robustly handle images in adverse conditions, such as modified lighting, sharpness, weather conditions and image compression. Various benchmarks aimed to measure robustness show that neural networks perform differently well under distribution shifts. While datasets such as ImageNet-C model for example common corruptions such as blur and adverse weather conditions, we argue that the properties of the optical system and the potentially resulting complex lens blur are insufficiently well studied in the literature. This study evaluates the impact of realistic optical corruptions on the ImageNet classification. The proposed complex corruption kernels are direction and wavelength dependent and include chromatic aberration, which are all to be expected in realistic scenarios such as autonomous driving applications. Our experiments on twelve different DNN models show significant differences of more than 5% in the top1 classification error, when compared to the model performances on matched ImageNet-C blur kernels.

1 Introduction

Neural networks for computer vision tasks are used in a wide range of applications and are expected to be reliable in safety-critical situations such as in autonomous driving [1, 2, 3]. Therefore, it is crucial that neural networks are able to generalize from the training distribution to unknown images and slight domain shifts. In order to test such behavior, various benchmarks have been proposed that introduce targeted corruptions [4, 5, 6, 7] or mimic common corruptions and adverse weather conditions [8, 9]. The simulation of effects such as lighting conditions, noise or image sharpness have been addressed for examples by Hendrycks et al. [8]. In [9], Kar et al. aim for more realistic modeling by proposing additional 3D corruptions such as change of field of view, camera roll or far focus.

While these papers cover a wide range of corruptions, they introduce necessary simplifications for each of them. As a result, they do not consider complex corruptions as they can result from the optical recording system. In this paper, we argue that the modeling of such realistic optical blur kernels that include chromatic aberrations and astigmatism should be considered, since they are very likely to eventually occur in practice.

Thus, we examine the effects of two complex kernel types on ImageNet and evaluate on the resulting corruptions the behavior of existing, robust and non-robust classification models, using ImageNet-C [8] as a baseline.

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Practically, the image of an object plane produced by a lens can be described using linear systems theory: If an idealized point light source is propagated through a camera's objective lens, the point function is spread to some degree on the image side. This observed intensity function is therefore called the intensity point *spread* function (PSF). In the best case, the PSF is diffraction-limited and therefore small and rotationally-symmetric. As a rule, however, the optical system is not perfectly balanced and aberrations arise. These aberrations directly affect the observed PSF. Thus, non-rotationally symmetric shapes that differ in wavelength can often occur and show the effects of e.g. Astigmatism and chromatic aberration. PSF examples are given in the appendix A. In general, the PSF varies over the image field. The superposition of all these point responses weighted with the scene's intensity yields the observed image.[10, 11] By means of simulation, such PSFs applied to an image can mimic the capture with the virtual lens model. For simplicity, we assume isoplanarity such that a single PSF represents a virtual lens, but with a focus on directional and wavelength dependence in contrast to approximate rotational symmetric blur kernels such as assumed in ImageNet-C[8].

2 Analysis of the impact of realistic PSF properties to classification

This article investigates the impact of directional and wavelength dependent PSFs at different severities. The optically motivated kernels will be called optical kernels here in contrast to the corruption kernels from ImageNet-C .

We take the defocus blur kernels from ImageNet-C and compare to them in size approximate matched optical kernels. Subsequently the image datasets (defocus blur from ImageNet-C and the proposed optical kernels) are classified by different pretrained neural networks. We compare the results for all severities of classification and image degradation. All operations are done in python and pytorch. Google Colab GPUs are used to perform the inference for the image datasets and to perform the different image dataset comparisons.

2.1 Metrics

To compare the data, different metrics are used following the dataflow from a set of PSFs to images (IMG) and classification (CLS). First, PSFs are generated, see Figure 1(left). From this, the modulation transfer function (MTF) can be generated, which is an established optical quality metric.[12, 13] The two-dimensional function is given in pairs of orthogonal slices in a particular direction, e.g. in direction of the coordinate axes or in diagonal direction. There exist different functionals derived from the MTF curve such as MTF50, which denotes the frequency value where the MTF falls to $50\,\%$, and area under the curve (AUC), which is the integral of the MTF. The metrics are meaningful, if curves of similar shape are compared to ensure for example for AUC, that the intensity is concentrated in similar frequency regions. These curves are used to match the corruption kernels and optical kernels.

The application of each PSF kernel to ImageNet yields a modified image dataset for each severity, which is compared to the unmodified ImageNet validation dataset. Every image of a modified dataset is compared to the unmodified original. These comparisons are evaluated with mean squared error (MSE) and the structural similarity index (SSIM).[14] To obtain a manageable overview, the means of these metrics are taken and are denoted as mMSE and mSSIM respectively.

These images are then fed to the different classifiers. The classifiers are assessed with the top1-error, which takes the mean of all falsely classified images. These values are then compared for the different models and for each severity.

2.2 Blur models

The corruption kernels represent the reproduced "defocus blur" corruption kernels from ImageNet-C for five severities. The generation of these kernels is a two step process: First, a disk shape is created, which is then blurred with Gaussian blur.[8] This yields approximate rotationally symmetric blur kernels, which do not depend on the color channel and model defocus.

To compare such kernels with more realistic optical kernels, we use the color-dependent average PSF of a space-variant Cooke-Triplet lens model [15] as base PSF:

$$h(u, v, \lambda) = |\mathcal{F}\big\{(P(x, y) \cdot e^{-j2\pi W_\lambda(x,y,\lambda)}\big\}|^2, \tag{1}$$

where h denominates the intensity PSF acquired from a complex pupil description consisting of the pupil shape P and its phase with the real wavefront aberration W_λ.[11] For the average PSF a wavefront aberration description W_λ is available from [15] in terms of Zernike Polynomials Z_n^m [10]:

$$W_\lambda(x, y, \lambda) = \lambda \cdot \sum_{n,m} A_n^m(\lambda) \cdot Z_n^m \tag{2}$$

Each coefficient A_n^m in multiples of the wavelengths $\lambda_i \in \{0.4861\,\mu\text{m}, 0.5876\,\mu\text{m} \text{ and } 0.6563\,\mu\text{m}\}$ represents the contribution of a particular type of aberration. This allows to parameterize different aspects such as the amount of coma, astigmatism or defocus. The base PSF's wavefront aberration description therefore consists of three different sets of the first 20 Zernike-Fringe coefficients, which are then assigned to the different RGB color channels. To show directional dependence, oblique astigmatism A_2^{-2} is varied, which may also lead to chromatic aberration: The original wavefront aberration W depends on wavelength. The experimentally determined parameterization $A_2^{-2} \in \{1, 1.4, 2, 3, 3.8\}\lambda_i$ leads to optical kernels comparable to the corruption kernels both in terms of PSF metrics (MTF50, AUC, MTF curves) as well as IMG metrics (SSIM,MSE).

We also include two additional studies in appendix C for "straight" astigmatism and a closer matched version for oblique astigmatism.

3 Experiments on ImageNet

We select 12 pretrained neural networks for classification with common architectures [16] from Tab. 1. All models are pretrained on ImageNet and publicly available from pytorch vision's model zoo. We also include three models with ResNet50 architecture from the RobustBench's model zoo [7] ranked under the top-5 networks at the ImageNet leaderboard for corruptions.[7] These neural networks are robust on ImageNet-C [8] and ImageNet-3DC [9] corruptions respectively. The exact listing of the network architectures can be found in the appendix D in Tab. 1.

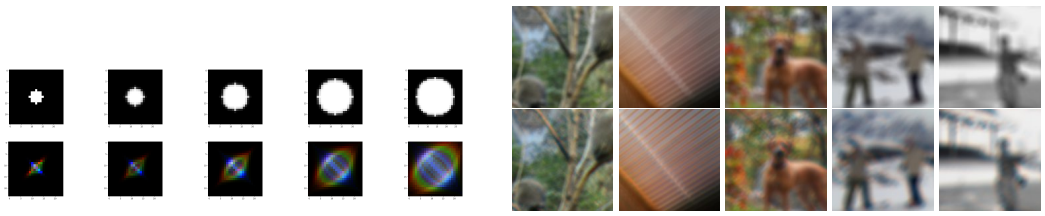
3.1 PSF comparisons

Here, the complex optical kernels shall first be compared to the optical kernels visually in Fig 1 for all severities. Visually, the severities are comparable, even though there is a dependence on the color channel, as well as a break in rotational symmetry. A criterion to quantify the similarity are also the MTF50 values in Fig. 8. The values are similar and indicate an averaged comparability between the kernels. The MTF curves for the kernels can also be found in the appendix B. Note that for the optical kernels six different curves exist, which occur because of the direction dependence and wavelength dependence, whereas the complexity of the corruption kernels can be reduced to a single MTF curve. Astigmatic behavior can be read, for example, in severity 1 in appendix B, Fig. 6 in the red and blue channels, where either the $45°$ or the $-45°$ curves proceed low. In addition, the orientations are just reversed, resulting in chromatic aberrations.

3.2 Image comparisons

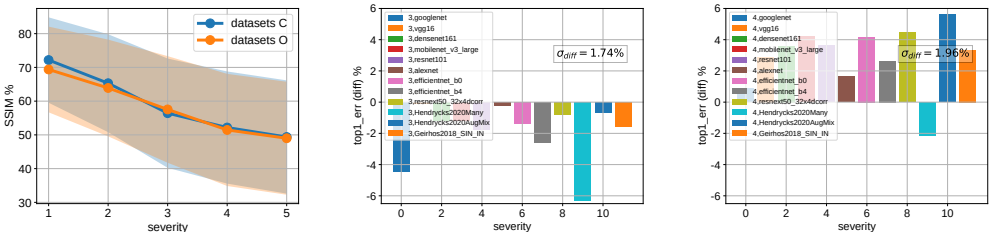
The different filter kernels are then used to convolve the images from ImageNet and yield ten datasets of 50k images each. Both, images from corruption kernels and optical kernels are saved with the same slight JPEG compression as in ImageNet-C to avoid a corruption bias between lossless and lossy image data compression and to keep the processing of 500k images manageable. The usual transformations center crop and downscale to RGB images of size 224×224 are done as preprocessing step to the bigger original ImageNet images to ensure that no additional smoothing by the scaling operation is applied to the filtered images. The image samples in Fig. 1 visualize differences in the datasets corruption datasets and optical datasets. The blur in the images increases significantly with severities. Looking at optical datasets2-4 color fringes at edges are readily visible and directional dependent blur occurs.

However, the mean values mMSE and mSSIM listed in 2 are very close to each other, which indicate similar and comparable image quality.



(a) (b) (c) (d) (e)

Figure 1: Left: PSFs representing the different "severities" 1-5 from left to right: First row visualizes the corruption kernels, the second row astigmatic optical kernels showing chromatic aberration. Right: Visual examples from the modified datasets with increasing severities: 2 (a), 3 (b-c) and 4 (d-e). The first row visualizes the effects of corruption kernels and the second of optical kernels. Read example: Chromatic aberration visible at the reddish and greenish branches (a) and at the window blind (b), while the simple kernels do not create color fringes.



(a) (b) Severity 3 (c) Severity 4

Figure 2: (a) Difference in mSSIM for all severities. The mSSIM for severities 3-5 is $\leq 1.1\,\%$. (b,c) Difference in top1-error between modified and unmodified ImageNet for corruption datasets and optical datasets. The average difference in mSSIM is below $1.1\,\%$ for severities 3-5. Classification results (b,c) with a $+$ denote worse classification for optical datasets (higher top1-error).

3.2.1 Classification on ImageNet

The images from corruption datasets and optical datasets are then processed with the different neural networks for classification from Tab. 1. Again, the processing is set such that no additional transformation besides image normalization is done, because the input size is already the target size of 224×224. The classification results for 50k images each in Figs. 2b and 2c show differences of top1-errors for the selected neural networks. Looking at the mean values of the errors μ_{top1}, this bias can possibly be due to the slight variation between the kernel types: The image results show slight variations for levels 3 and 4 in mSSIM, respectively. For level 3, the mSSIM for optical datasets3 is higher ($1.11\,\%$) and for level 4, the mSSIM for corruption datasets4 is lower ($-0.720\,\%$). However, significant differences between the networks can be found within these conditions. For example, Hendrycks2020Many[17, 18], as well as in most cases GoogLeNet[19], can handle the blur of optical kernels better than that of corruption kernels (lower top1-error). Hendrycks2020AugMix[20, 18] does mostly the opposite. All severities are visualized in appendix F. Note that the differences in mSSIM, mMSE, MTF50 and AUC are for severities 1-2 greater, but the top1-error deviation is smaller for these less blurred images.

4 Conclusion

This article compares the ImageNet validation dataset in several modified versions degraded with corruption kernels from ImageNet-C and optical kernels, which are directional and wavelength dependent. Although the blur kernels are of comparable size and produce similar image datasets, some classification results differ significantly. We conclude that realistic optical corruptions should be considered in our standard benchmarks towards model robustness.

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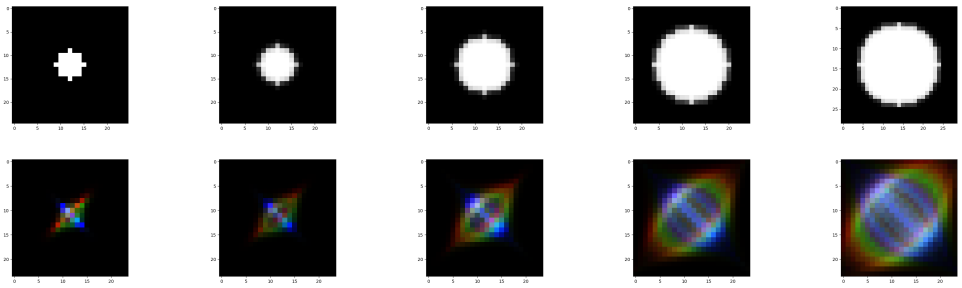
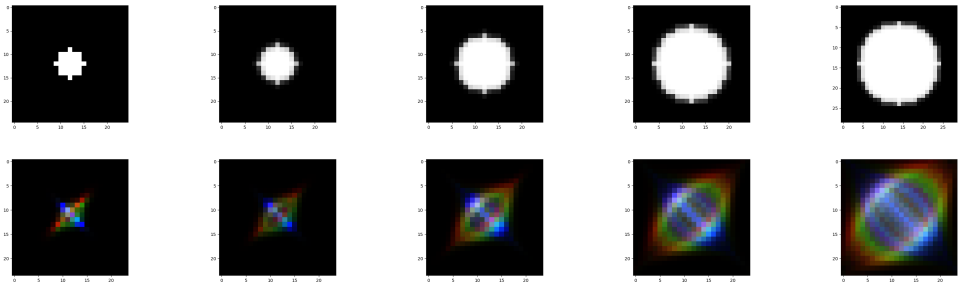
A PSFs

The different used kernels are visualized in Figs. 3, 4 and 5.



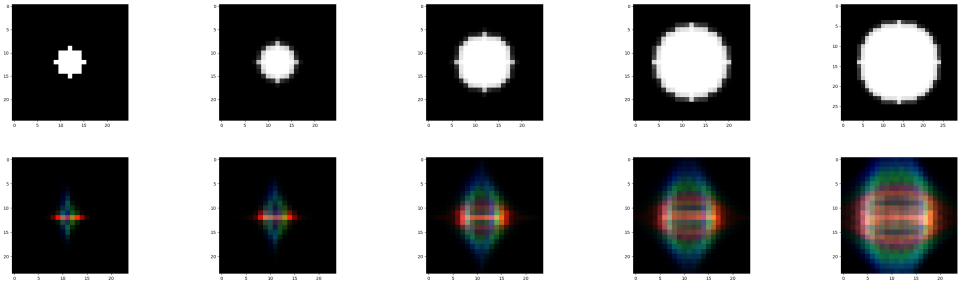
(a) (b) (c) (d) (e)

Figure 3: Average PSFs representing the different "severities" 1-5: (a-e) corruption kernels, (f-j) optical kernels with oblique astigmatism and chromatic aberrations.



(a) (b) (c) (d) (e)

Figure 4: Average PSFs representing the different "severities" 1-5: (a-e) corruption kernels, (f-j) optical kernels with oblique astigmatism and chromatic aberrations. These kernels have higher match quality and minimize mSSIM on the datasets, although visually hard to distinct from Fig. 3

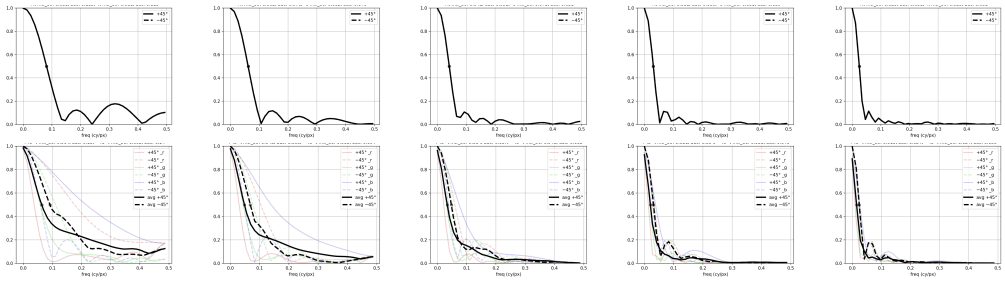


(a) (b) (c) (d) (e)

Figure 5: Average PSFs representing the different "severities" 1-5: (a-e) corruption kernels, (f-j) optical kernels with straight astigmatism and chromatic aberrations.

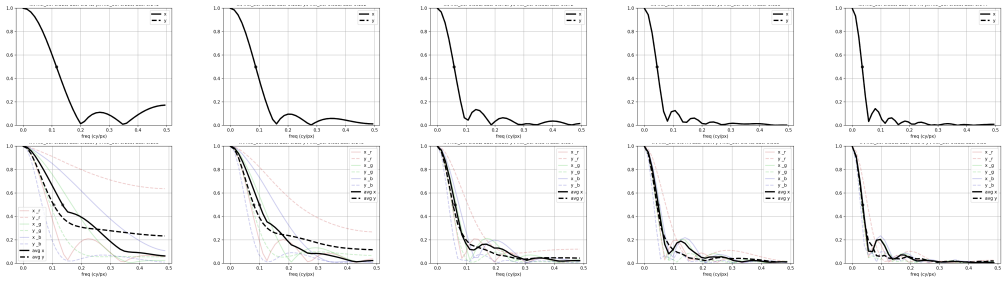
B MTF curves

Here, the direction in coordinate axes is denoted with (x, y) and the diagonal direction is denoted with $\pm 45°$. Note that sometimes curves for the optical kernels in different directions proceed differently. This astigmatic behaviour is color channel dependent and therefore creates chromatic aberrations.



(a) (b) (c) (d) (e)

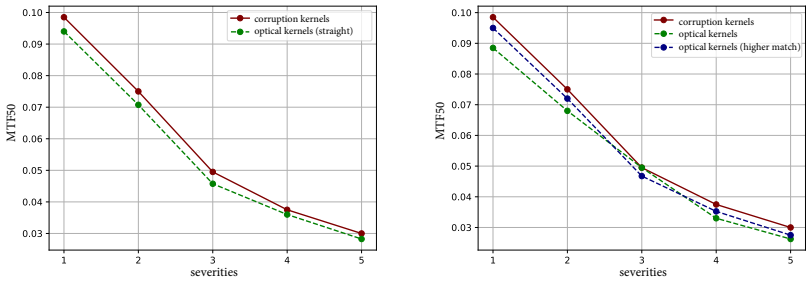
Figure 6: MTF slices from PSFs for severities (1-5, a-e): First row corruption kernels, second row optical kernels with oblique astigmatism from Fig. 3



(a) (b) (c) (d) (e)

Figure 7: MTF slices from PSFs for severities (1-5, a-e): First row corruption kernels, second row optical kernels with straight astigmatism (0°,90°) from Fig. 5

B.1 Aggregated MTF metrics - differences for MTF50



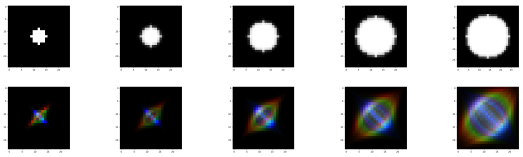
(a) (b)

Figure 8: MTF50 values for all severities and the different studies: (a) visualizes corruption kernels vs. optical kernels with straight astigmatism from Fig. 5 and (b) displays the optical kernels from Fig. 3 and 4. Each point is acquired by averaging color, orientation and direction to get a single MTF from the above MTF curves from Figs. 7 and 6. From this resulting MTF the MTF50 value is taken. We also show the MTF50 values from curves with minimum mSSIM on the datasets.

C Additional studies for different optical kernels

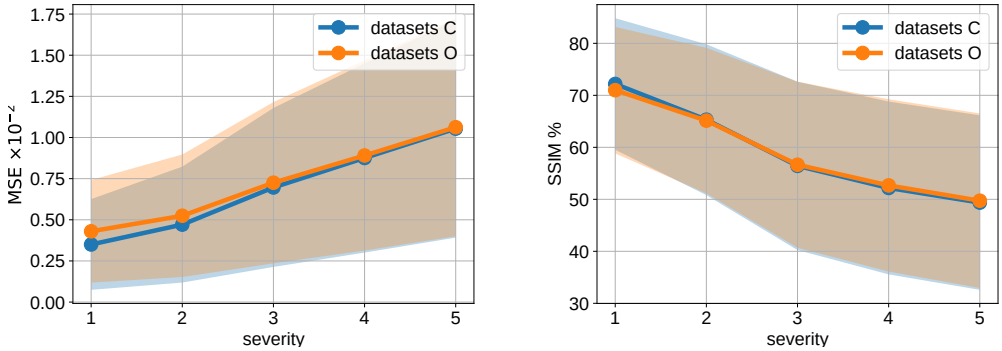
C.1 Oblique astigmatism (higher match quality)

We provide here a version with closer match in mSSIM, mMSE, MTF50 and AUC for all severities with the parameterization $A_2^{-2} \in \{0.9, 1.3, 2.1, 2.8, 3.6\}\lambda_i$. The mSSIM for severities 3-5 is below $0.5\,\%$, but although significantly smaller differences occur compared to Fig. 14 still the DNNs can handle the blur types differently well, which indicates a distribution shift. Lower severities tend to be more robust to changes in mSSIM and the improved match quality has little effect.



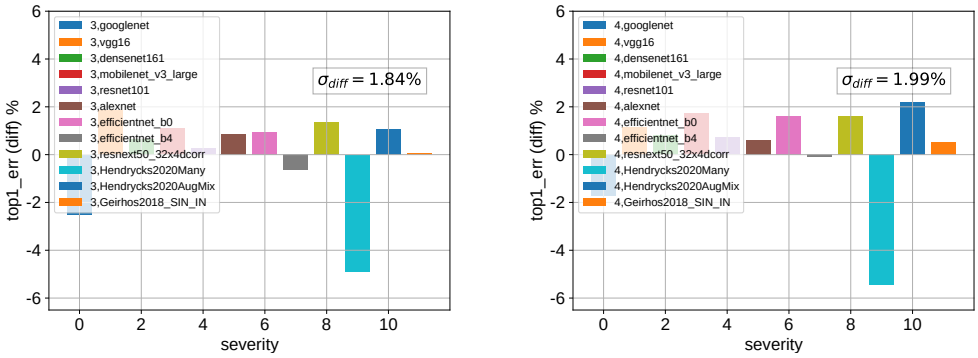
(a) (b) (c) (d) (e)

Figure 9: Average PSFs representing the different "severities" 1-5. First row: corruption kernels with higher match quality, second row: optical kernels with chromatic aberrations.



(a) (b)

Figure 10: Average MSE (a) and SSIM (b) between corrupted image database and unmodified original.

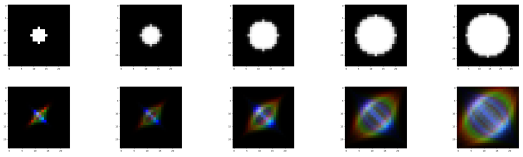


(a) Severity 3 (b) Severity 4

Figure 11: Deviation in top1-error for all neural networks and severities 3 and 4. "+" means that optical datasets have higher top1-error than corruption datasets.

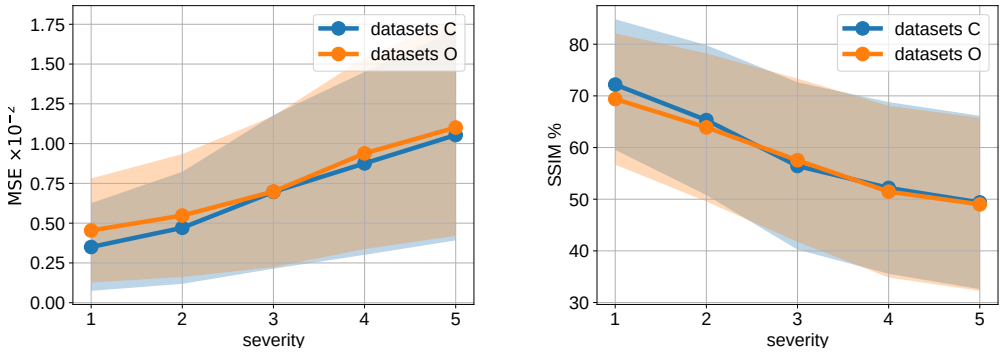
C.2 Oblique astigmatism

We include here the study on oblique astigmatic optical kernels as used in the main article. The size of the kernels in Fig. 3 look very similar to Fig. 4, but create a slightly larger mSSIM $\leq 1.1\,\%$ for severities 3-5.



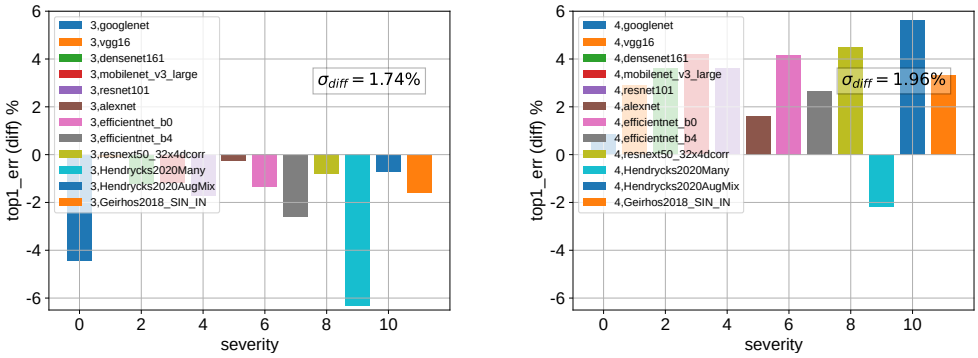
(a) (b) (c) (d) (e)

Figure 12: Average PSFs representing the different "severities" 1-5. First row: corruption kernels, second row: optical kernels with chromatic aberrations.



(a) (b)

Figure 13: Average MSE (a) and SSIM (b) between corrupted image database and unmodified original.

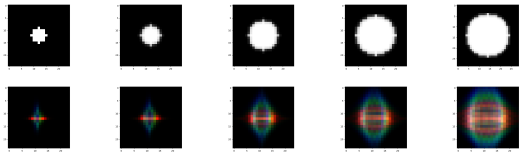


(a) Severity 3 (b) Severity 4

Figure 14: Deviation in top1-error for all neural networks and severities 3 and 4. "+" means that optical datasets have higher top1-error than corruption datasets.

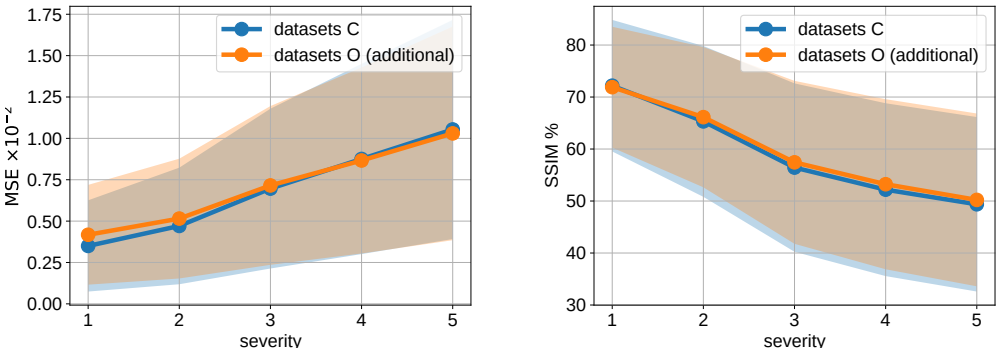
C.3 Straight astigmatism

This study shows the effect of the parameterization of straight astigmatism $A_2^{+2} \in \{1.0, 1.4, 2.2, 2.8, 3.6\}\lambda_i$, which leads to comparable results as in Fig. 11.



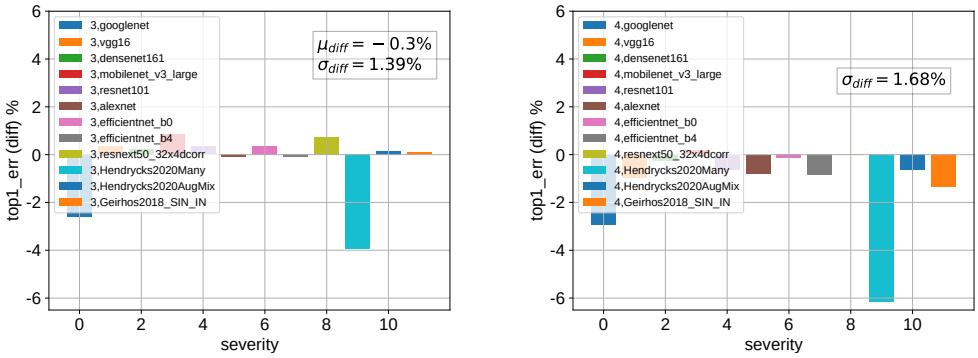
(a) (b) (c) (d) (e)

Figure 15: Average PSFs representing the different "severities" 1-5. First row: corruption kernels, second row: optical kernels with chromatic aberrations.



(a) (b)

Figure 16: Average MSE (a) and SSIM (b) between corrupted image database and unmodified original.



(a) Severity 3 (b) Severity 4

Figure 17: Deviation in top1-error for all neural networks and severities 3 and 4. "+" means that optical datasets have higher top1-error than corruption datasets. Difference in mSSIM $\leq 1\,\%$.

D Additional tables

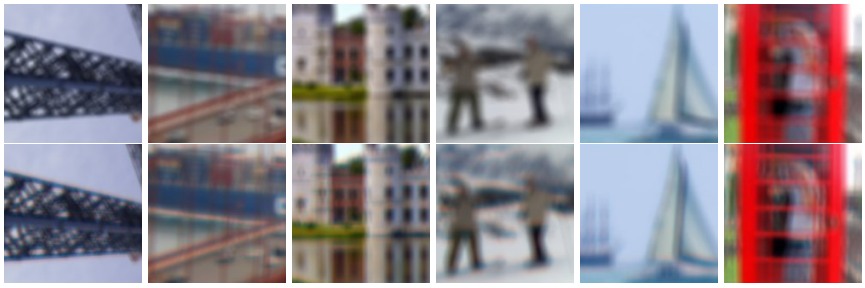
Table 1: Selection of pretrained models from pytorch vision and RobustBench model zoos with corresponding number of trainable parameters. The selected neural networks from RobustBench use a Resnet50.

Name	Number of Parameters $[\times 10^6]$	Name	Number of Parameters $[\times 10^6]$
VGG16	138.4	ResNeXt50	25.0
AlexNet	61.1	EfficientNet_B4	19.3
ResNet101	44.5	GoogLeNet	6.6
DenseNet161	28.7	MobileNet_v3	5.5
Resnet50	25.6	EfficientNet_B0	5.3

E Additional image examples

(a) (b) (c) (d) (e) (f)

Figure 18: All images are zoomed in. First row corruption datasets, second row optical datasets. Severity 3 (a-c): Chromatic aberration visible at the airplanes wheels, the dog's face, the window blind and the boat's mast. Note also the diagonal astigmatism. Severity 5: (d-e) visible chromatic aberration at the fish scales as orange stripes, the eagle, and as color fringe at the baby's hair.

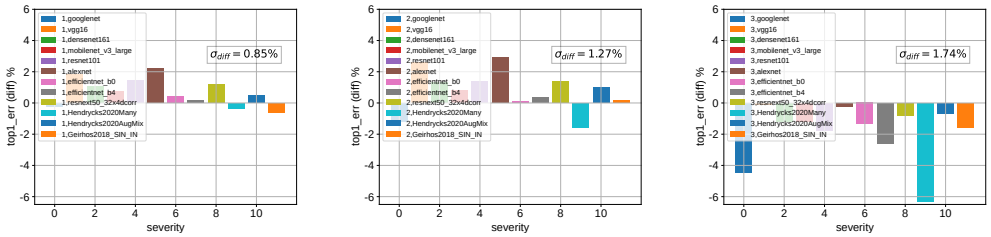


(a) (b) (c) (d) (e) (f)

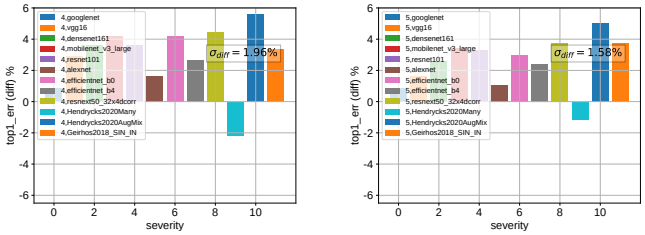
Figure 19: First row corruption datasets, second row optical datasets (straight). Severity 3 (a-c): Chromatic aberration visible at the airplanes wheels, the dog's face, the window blind and the boat's mast. Note also the diagonal astigmatism. Severity 5: (d-e) visible chromatic aberration at the fish scales as orange stripes, the eagle, and as color fringe at the baby's hair.

F Classification results for all severities

Below the classification results are plotted for the two studies.



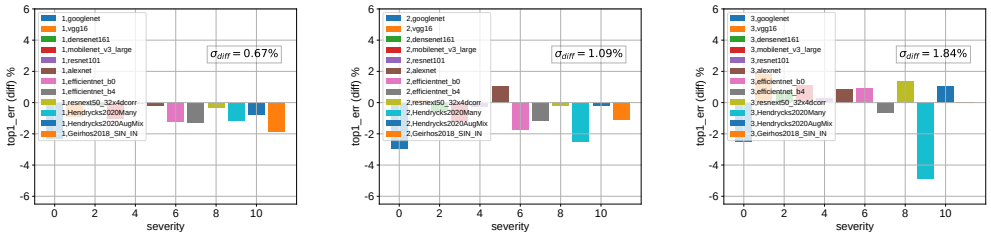
(a) Severity 1 (b) Severity 2 (c) Severity 3



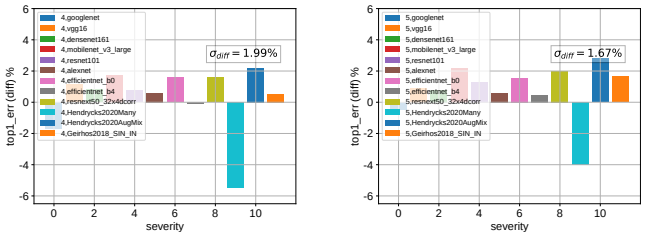
(d) Severity 4 (e) Severity 5

Figure 20: Classification results, difference in top1-error in percentage points: Comparison of optical datasets and corruption datasets for severities 1-5 from (a-e). Difference in mSSIM $\leq 1.1\,\%$ for severities 3-5.

F.1 Classification results for all severities for additional studies

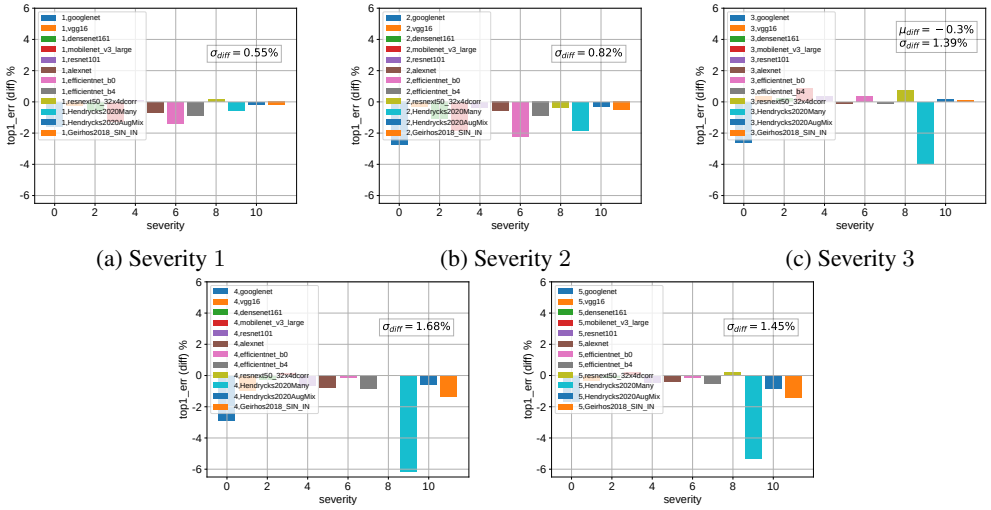


(a) Severity 1 (b) Severity 2 (c) Severity 3



(d) Severity 4 (e) Severity 5

Figure 21: Classification results, difference in top1-error in percentage points: Comparison of optical datasets and corruption datasets using optical kernels *with higher match quality* for severities 1-5 from (a-e). Difference in mSSIM $\leq 0.5\,\%$ for severities 3-5.

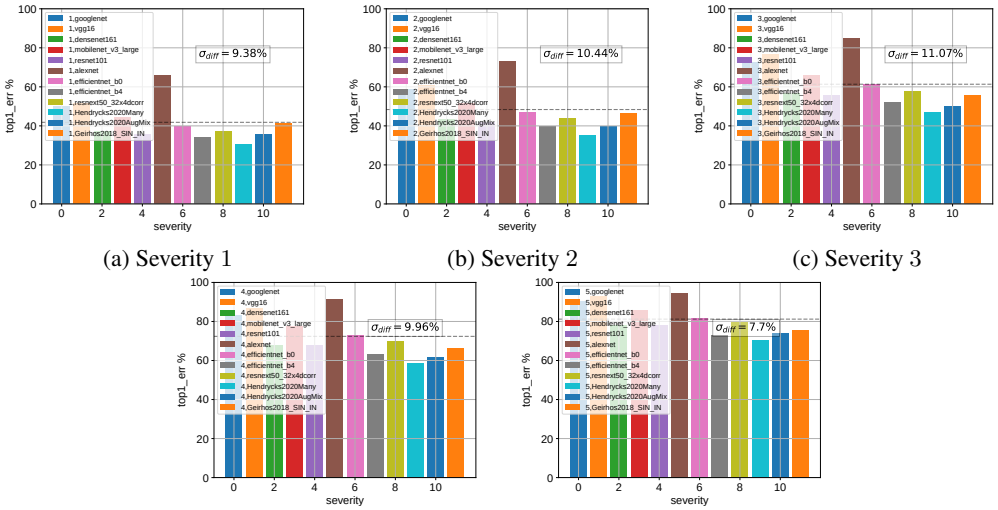


(a) Severity 1 (b) Severity 2 (c) Severity 3

(d) Severity 4 (e) Severity 5

Figure 22: Classification results, difference in top1-error in percentage points: Comparison of optical datasets with straight astigmatism and corruption datasets for severities 1-5 from (a-e). Difference in mSSIM $\leq 1\,\%$.

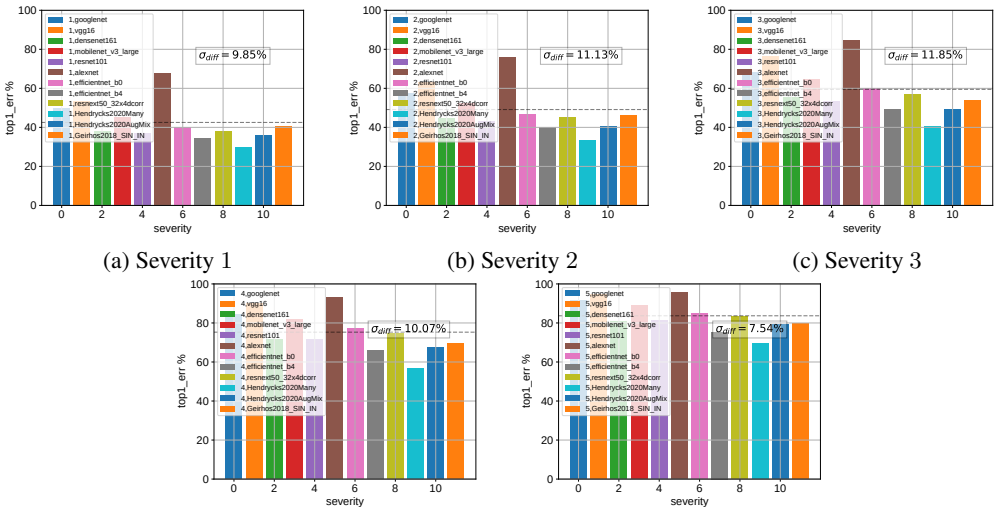
F.2 Absolute results on the different modified dataset versions



(a) Severity 1 (b) Severity 2 (c) Severity 3

(d) Severity 4 (e) Severity 5

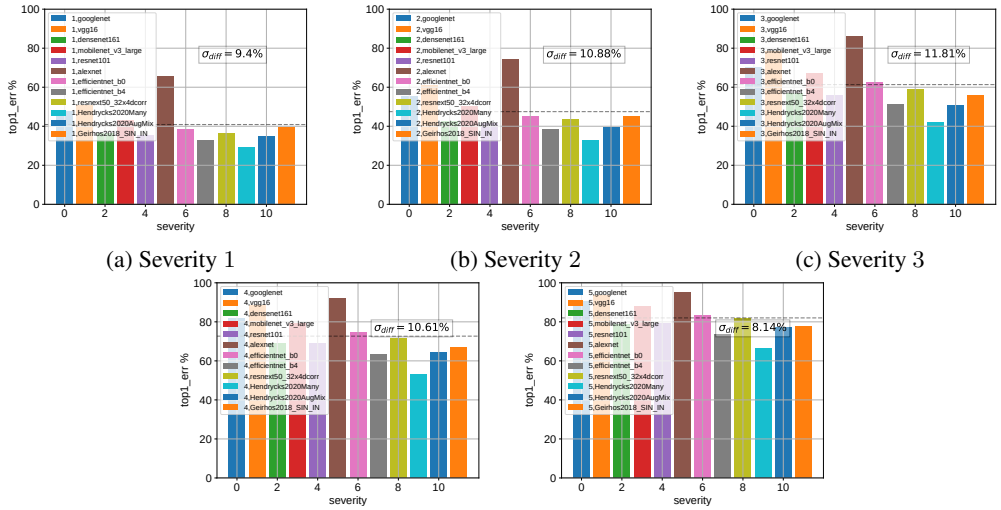
Figure 23: Classification results: Top1-error for corruption kernels for severities 1-5 from (a-e).



(a) Severity 1 (b) Severity 2 (c) Severity 3

(d) Severity 4 (e) Severity 5

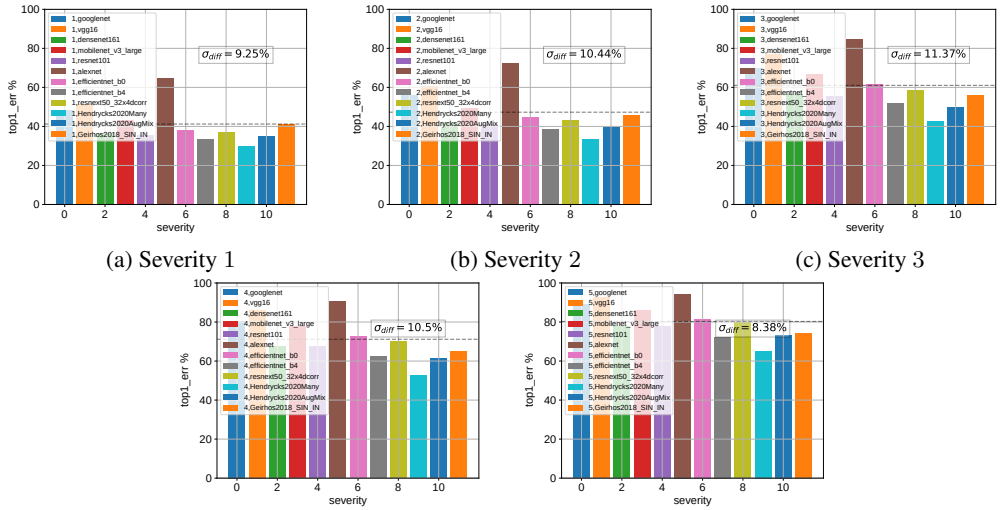
Figure 24: Classification results: Top1-error for optical kernels (oblique astigmatism) from Fig. 3 for severities 1-5 from (a-e). Difference in mSSIM $\leq$ for 1.1 % for severities 3-5.



(a) Severity 1 (b) Severity 2 (c) Severity 3

(d) Severity 4 (e) Severity 5

Figure 25: Classification results: Top1-error in percentage points: optical datasets with optical kernels from Fig. 4 *with higher match quality* for severities 1-5 from (a-e). Difference in mSSIM $\leq 0.5\,\%$ for severities 3-5.



(a) Severity 1 (b) Severity 2 (c) Severity 3

(d) Severity 4 (e) Severity 5

Figure 26: Classification results: Top1-error in percentage points for optical datasets with straight astigmatism from Fig. 5 for severities 1-5 from (a-e). Difference in mSSIM $\leq 1\,\%$.