Robust Reinforcement Learning on State Observations with Learned Optimal Adversary

Abstract

We study the robustness of reinforcement learning (RL) with adversarially perturbed state observations, which aligns with the setting of many adversarial attacks to deep reinforcement learning (DRL) and is also important for rolling out real-world RL agent under unpredictable sensing noise. With a fixed agent policy, we demonstrate that an *optimal adversary* to perturb state observations can be found, which is guaranteed to obtain worst case agent reward. For DRL settings, this leads to a novel empirical adversarial attack to RL agents via a learned adversary that is much stronger than previous ones. To enhance the robustness of an agent, we propose a framework of alternating training with learned adversaries (ATLA), which trains an adversary online together with the agent using policy gradient following the optimal adversarial attack framework. Additionally, inspired by the analysis of state-adversarial Markov decision process (SA-MDP), we show that past states and actions (history) can be useful for learning a robust agent, and we empirically find a LSTM based policy can be more robust under adversaries. Empirical evaluation on a few continuous control environments show that ATLA achieves state-of-the-art performance under strong adversaries.

1 Introduction

Modern deep reinforcement learning agents (Mnih et al., 2015; Levine et al., 2015; Lillicrap et al., 2015; Silver et al., 2016; Fujimoto et al., 2018) typically use neuron networks as function approximators. Since the discovery of adversarial examples in image classification tasks (Szegedy et al., 2013), the vulnerabilities in DRL agents were first demonstrated in (Huang et al., 2017; Lin et al., 2017; Kos & Song, 2017) and further developed under more environments and different attack scenarios (Behzadan & Munir, 2017a; Pattanaik et al., 2018; Xiao et al., 2019). These attacks commonly add imperceptible noises into the *observations of states*, e.g., the observed environment slightly differs from true environment states. This raises concerns for using RL in safety-crucial applications such as autonomous driving (Sallab et al., 2017; Voyage, 2019); additionally, the discrepancy between ground-truth states and agent observations also contributes to the "reality gap" - an agent working well in simulated environments may fail in real environments due to noises in observations (Jakobi et al., 1995; Muratore et al., 2019), as real-world sensing contains unavoidable noise (Brooks, 1992).

We classify the weakness of a DRL agent on the perturbations of state observations into two classes: the *vulnerability in function approximators*, which typically originates from the highly non-linear and blackbox nature of neural networks; and *intrinsic weakness of policy*: even perfect features for states are extracted, a policy can still make mistakes due to an intrinsic weakness in the policy.

For example, in the deep Q networks (DQNs) for Atari games, a large convolutional neural network (CNN) is used for extracting features from input frames. To act correctly, the network must extract crucial features: e.g., for the game of Pong, the position and velocity of the ball, which can observed by visualizing convolutional layers (Hausknecht & Stone, 2015; Guo et al., 2014). Many attacks to the DQN setting add imperceptible noises (Huang et al., 2017; Lin et al., 2017; Kos & Song, 2017; Behzadan & Munir, 2017a) that exploit the vulnerability of deep neural networks so that they extract wrong features, as we have seen in adversarial examples of image classification tasks. On the other hand, the fragile function approximation is not the only source of the weakness of a RL agent - in a finite-state markov decision process (MDP), we can use a tabular form of policy and value functions so there is no function approximation error. The agent can still be vulnerable to small perturbations

(a) Path in unperturbed environment. Agent's reward = +1. The black arrows and numbers show actions and value function of the agent.

(b) Path under optimal adversary. Agent's reward = $-\infty$. The red arrows and the numbers show actions and value function of the adversary.

(c) A robust POMDP policy solved by SARSOP (Kurniawati et al., 2008) under the same adversary. This policy is history dependent.

Figure 1: The vulnerability of a RL agent does not only come from the errors in function approximators such as DNNs. We show an agent on gridworld environment trained with policy iteration with no function approximators, and its optimal policy is intrinsically not robust to perturbations of state observations. The red square and blue circle are the starting point and target (reward +1) of the agent, respectively. The green triangles are traps, with reward -1 once encountered. The Adversary is allowed to perturb the observation to adjacent states along four directions: up, down, left, and right. Adversary earns +1 at traps and -1 at the target. We set $\gamma = 0.9$ for both agent and adversary.

on observations, e.g., perturbing the observation of a state to one of its four neighbors in a gridworld-like environment can prevent an agent from reaching its goal (Figure 1). To improve the robustness of RL, we need to take measures from both aspects — a more robust function approximator, and a policy aware of perturbations in observations.

Techniques developed in enhancing the robustness of neural network (NN) classifiers can be applied to address the vulnerability in function approximators. Especially, for environments like Atari games with images as input and discrete actions as outputs, the policy network π_θ behaves similar to a classifier in test time. Thus, Fischer et al. (2019); Mirman et al. (2018a) utilized existing certified adversarial defense (Mirman et al., 2018b; Wong & Kolter, 2018; Gowal et al., 2018) approaches in supervised learning to enhance the robustness of DQN agents. Another successful approach (Zhang et al., 2020) for both Atari and high-dimensional continuous control environment regularizes the smoothness of the learned policy such that $\max_{\hat{s} \in \mathcal{B}_s} D(\pi(s), \pi(\hat{s}))$ is small for some divergence D and $\mathcal{B}(s)$ is a neighborhood around s. This maximization can be solved using a gradient method or convex relaxations of NNs (Salman et al., 2019), and then will be minimized by optimizing θ in a minimax loss function. Such an adversarial minimax regularization is in the same spirit as the ones used in some adversarial training approaches for (semi-)supervised learning, such as in TRADES (Zhang et al., 2019) and VAT (Miyato et al., 2015). However, regularizing the function approximators does not explicitly improve the intrinsic robustness of the policy.

In this paper, we propose an orthogonal approach, alternating training with learned attacks (ATLA), to enhance the robustness of DRL agents. We focus on dealing with the intrinsic weakness of the policy by learning an adversary online with the agent during training time, rather than directly regularizing function approximators. Our main contributions can be summarized as:

• We follow the theory of state-adversarial Markov decision process (SA-MDP) in Zhang et al. (2020) and show how to learn an *optimal* adversary for perturbing observations. We demonstrate practical attacks under this formulation and obtain learned adversaries that are significantly stronger than previous ones.

• We propose the alternating training with learned adversaries (ATLA) framework to improve the robustness of DRL agents. The difference between our approach and previous training time attack approaches is that we use a stronger adversary, which is learned online together with the agent.

• Our analysis on SA-MDP also shows that *history* can be important for learning a robust agent. We thus propose to use a LSTM based policy in the ATLA framework and find that it is more robust than policy parameterized as regular feedforward NNs.

- We evaluate our approach empirically on four continuous control environments. We outperform explicit regularization based methods in a few environments, and our approach can also be directly combined with explicit regularizations on function approximators to achieve state-of-the-art results.

2 RELATED WORK

State-adversarial Markov decision process (SA-MDP) (Zhang et al., 2020) characterizes the decision making problem under adversarial attacks on *state observations*. Most importantly, the true state in the environment is not perturbed by the adversary under this setting; for example, perturbing pixels in an Atari environment (Huang et al., 2017; Kos & Song, 2017; Lin et al., 2017; Behzadan & Munir, 2017a) does not change the true location of an object in the game simulator. In real world settings, SA-MDP can characterize agent performance under natural or adversarial noise from sensor measurements. For example, GPS sensor readings on a car are naturally noisy, but the ground truth location of the car is not affected by the noise. Importantly, this setting is different from robust Markov decision process (RMDP) (Nilim & El Ghaoui, 2004; Iyengar, 2005), where the worst case transition probabilities of the environment are considered. "Robust reinforcement learning" in some works (Mankowitz et al., 2018; 2019) refer to this different definition of robustness in RMDP, and should not be confused with our setting of robustness against perturbations on state observations.

Several works proposed methods to learn an adversary online together with an agent. RARL (Pinto et al., 2017) proposed to train an agent and an adversary under the two-player Markov game (Littman, 1994) setting. The adversary *can* change the environment states through actions *directly applied* to environment. The goal of RARL is to improve the robustness against environment parameter changes, such as mass, length or friction. Gleave et al. (2019) discussed the learning of an adversary using reinforcement learning to attack a victim agent, by taking adversarial actions that changes the environment and consequentially change the observation of the victim agent. Both Pinto et al. (2017); Gleave et al. (2019) conduct their attack under on the two-player Markov game framework, rather than considering perturbations on state perturbations. Besides, Li et al. (2019) consider a similar Markov game setting in multi-agent RL environments. The difference between these works and ours can be clearly seen in the setting where the adversary is fixed - under the framework of (Pinto et al., 2017; Gleave et al., 2019), the learning of agent is still a MDP, but in our setting, it becomes a harder POMDP problem (Section 3.2).

Training time adversarial attacks for DRL agents by perturbing state observations have been investigated in a few works. Kos & Song (2017); Behzadan & Munir (2017b) used gradient based adversarial attack to DQN agents and put adversarial frames into replay buffer. This approach is not very successful because for Atari environments the main source of weakness is likely to come from the function approximator, so an adversarial regularization framework such as (Zhang et al., 2020; Qu et al., 2020) which directly controls the smoothness of the Q function is more effective. For lower dimensional continuous control tasks such as the MuJoCo environments, Mandlekar et al. (2017); Pattanaik et al. (2018) conducted FGSM and multi-step gradient based attack during training time; however, their main focus was on the robustness against environment parameter changes and only limited evaluation on the adversarial attack setting was conducted with relatively weak adversaries. Zhang et al. (2020) systematically tested this approach under newly proposed strong attacks in a few more environments, and found that it cannot reliably improve robustness. These training time attack approaches typically use a gradient basic attack based on a critic function. Such an attack is usually relatively weak, and not sufficient to lead to a robust policy under stronger attacks.

The robustness of RL has also been investigated from other perspectives. For example, Tessler et al. (2019) study MDPs under action perturbations; Tan et al. (2020) use adversarial training on action space to enhance agent robustness under action perturbations. These settings differ from the setting of perturbing state observations discussed in our paper.

3 METHODOLOGY

In this section, we first discuss the case where the agent policy is fixed, and then the case where the adversary is fixed in SA-MDPs. This allows us to propose an alternating training framework to improve robustness of RL agents under perturbations on state observations.

Notations and Background We use $\mathcal{S}$ and $\mathcal{A}$ to represent the state space and the action space, respectively; $\mathcal{P}(\mathcal{S})$ defines the set of all possible probability measures on $\mathcal{S}$. We define a Markov decision process (MDP) as $(\mathcal{S}, \mathcal{A}, R, p, \gamma)$, where $R : \mathcal{S} \times \mathcal{A} \times \mathcal{S} \rightarrow \mathbb{R}$ and $p : \mathcal{S} \times \mathcal{A} \rightarrow \mathcal{P}(\mathcal{S})$

are two mappings represent the reward and transition probability. The transition probability at time step t can be written as $p(s'|s,a) = \Pr(s_{t+1} = s'|s_t = s, a_t = a)$. $\gamma \in [0,1]$ is the discounting factor. We denote a stationary policy as $\pi : \mathcal{S} \rightarrow \mathcal{P}(\mathcal{A})$ which is independent of history. We denote history h_t at time t as $(s_0, a_0, \cdots, s_{t-1}, a_{t-1}, s_t)$ and $\mathcal{H}$ as the set of all histories. A history-dependent policy is defined as $\pi : \mathcal{H} \rightarrow \mathcal{P}(\mathcal{A})$. A partially observable Markov decision process (Astrom, 1965) (POMDP) can be defined as a 7-tuple $(\mathcal{S}, \mathcal{A}, \mathcal{O}, \Omega, R, p, \gamma)$ where $\mathcal{O}$ is a set of observations and Ω is a set of conditional observation probabilities $p(o|s)$. Unlike MDPs, POMDPs typically require history-dependent optimal policies.

To study the decision problem under adversary on state observations, we use the framework of state-adversarial Markov decision process (Zhang et al., 2020) (SA-MDP). In SA-MDP, an adversary $\nu : \mathcal{S} \rightarrow \mathcal{S}$ is introduced to perturb the input state of an agent; however, the true environment state s is unchanged (Figure 2). Formally, an SA-MDP is a 6-tuple $(\mathcal{S}, \mathcal{A}, \mathcal{B}, R, p, \gamma)$ where $\mathcal{B}$ is a mapping from a state $s \in \mathcal{S}$ to a set of states $\mathcal{B}(s) \in \mathcal{S}$. The agent sees the perturbed state $\hat{s} \sim \nu(s)$ and take the action $\pi(a|\hat{s})$ accordingly. $\mathcal{B}$ limits the power of adversary:

Figure 2: SA-MDP introduces an adversary on state observations in a MDP.

$\nu(s) \in \mathcal{B}(s)$. The goal of SA-MDP is to solve an optimal policy π^* under its optimal adversary $\nu^*(\pi^*)$; an optimal adversary is defined as an adversary $\nu^*(\pi)$ such that π achieves the lowest possible expected discounted return (or value) on all states. Zhang et al. (2020) did not give an explicit algorithm to solve SA-MDP and found that a stationary optimal policy need not exist.

3.1 Finding the optimal adversary under a fixed policy

In this section, we discuss how to find an *optimal* adversary ν for a given policy π. An optimal adversary leads to the *worst case performance* under bounded perturbation set $\mathcal{B}$, and is an absolute lower bound of the expected cumulative reward an agent can receive. It is similar to the concept of "minimal adversarial example" in supervised learning tasks. We first show how to solve the optimal adversary in MDP setting and then apply it to the DRL settings.

A technical lemma (Lemma 1) from Zhang et al. (2020) shows that, from the adversary's point of view, a fixed and stationary agent policy π and the environment dynamics can be essentially merged into an MDP with redefined dynamics and reward functions:

Lemma 1 (Zhang et al. (2020)) *Given an SA-MDP $M = (\mathcal{S}, \mathcal{A}, R, \mathcal{B}, p, \gamma)$ and a fixed and stationary policy $\pi(\cdot|\cdot)$, there exists an MDP $\hat{M} = (\mathcal{S}, \hat{\mathcal{A}}, \hat{R}, \hat{p}, \gamma)$ such that the optimal policy of $\hat{M}$ is the optimal adversary ν for SA-MDP given the fixed π, where $\hat{\mathcal{A}} = \mathcal{S}$, and*

$$\hat{R}(s, \hat{a}, s') = \begin{cases} -\frac{\sum_{a \in \mathcal{A}} \pi(a|\hat{a})p(s'|s,a)R(s,a,s')}{\sum_{a \in \mathcal{A}} \pi(a|\hat{a})p(s'|a,s)} & \text{for } s, s' \in \mathcal{S} \text{ and } \hat{a} \in \mathcal{B}(s) \subset \hat{\mathcal{A}}, \\ -M & \text{for } s, s' \in \mathcal{S} \text{ and } \hat{a} \notin \mathcal{B}(s). \text{ } M \text{ is a large constant.} \end{cases}$$

$$\hat{p}(s'|s, \hat{a}) = \sum_{a \in \mathcal{A}} \pi(a|\hat{a})p(s'|s,a) \quad \text{for } s, s' \in \mathcal{S} \text{ and } \hat{a} \in \hat{\mathcal{A}}.$$

Note that the adversary's goal is to reduce the reward earned by the agent. So $\hat{R}$ is defined as a weighted average of $-R$. After constructing the MDP $\hat{M}$, it is possible to solve an optimal agent ν of $\hat{M}$, which will be the optimal adversary on SA-MDP M given policy π. For MDPs, under mild regularity assumptions an optimal policy always exists (Puterman, 2014). In our case, the optimal policy on $\hat{M}$ corresponds to an *optimal adversary* in SA-MDP, which is the worst case perturbation for policy π. As an illustration, in Figure 1, we show a GridWorld environment. The red square is the starting point. The blue circle and green triangles are the target and traps, respectively. When the agent hits the target, it earns reward +1 and the game stops and it earns reward -1 when it encounters a trap. We set $\gamma = 0.9$ for both agent and adversary. The adversary is allowed to perturb the observation to adjacent cells along four directions: up, down, left, and right. When there is no adversary, after running policy iteration, the agent can easily reach target and earn a reward of +1, as in Figure 1. However, if we train the adversary based on Lemma 1 and apply it to the agent, we

(a) No attack
(reward **5851**)

(b) RS Attack
(reward **284**)

(c) Our Attack
(reward **−1140**)

(d) No attack
(reward **7094**)

(e) RS Attack
(reward **85**)

(f) Our Attack
(reward **−743**)

Figure 3: Our "Optimal" Attack and Robust Sarsa attack (a previous *strong* attack proposed in Zhang et al. (2020)) on Ant and HalfCheetah environments. Previous strong attacks make the agent fail and receive a small positive reward (less than 1/10 of the reward without attack). Our attack is strong enough to trick the agent into moving to the opposite direction, receiving a large *negative reward*.

are able to make the agent repeatedly encounter a trap. This leads to $-\infty$ reward for the agent and $+\infty$ reward for the adversary as shown in Figure 1b.

We now extend this Lemma 1 to the DRL setting. Since the learning of adversary is equivalent to solving an MDP, we parameterize the adversary as a neural network function and use any popular DRL algorithm to learn an "optimal" adversary. Here we quote the word "optimal" as we use function approximator to learn the agent so it's no longer optimal, but we emphasize that it follows the SA-MDP framework of solving an optimal adversary. No existing adversarial attacks follow such a theoretically guided framework. We show our algorithm in Algorithm 1. Instead of learning to produce $\hat{s} \in \mathcal{B}(s)$ directly, since $\mathcal{B}(s)$ is usually a small set nearby s (e.g., $\mathcal{B} = s' | \|s - s'\|_p \leq \epsilon$), our adversary learns a perturbation vector Δ, and we project $s + \Delta$ to $\mathcal{B}(s)$.

The first advantage of attacking a policy in this way is that it is *strong* - as we allow to optimize the adversary in an online loop of interactions with the agent policy and environment, and keep improving the adversary with a goal of receiving as less reward as possible. It is strong because it follows the theoretical framework of finding an optimal adversary, rather than using any heuristic to generate a perturbation. Empirically, in the cases demonstrated in Figure 3, previous strong attacks (e.g., Robust Sarsa attack) can successfully fail an agent and make it stop moving and receive a small positive reward; our learned attack can trick the agent into *moving toward the opposite direction of the goal* and receive a large negative reward. We also find that this attack can further reduce the reward of robustly trained agents, like SA-PPO (Zhang et al., 2020).

The second advantage of this attack is that it requires no gradient access to the policy itself; in fact, it treats the agent as part of the environment and only needs to run it in a blackbox. Previous attacks (e.g., Lin et al. (2017); Pattanaik et al. (2018); Xiao et al. (2019)) are mostly gradient based approach and need to access the values or gradients to a policy or value function. Even without access to gradients, the overall learning process is still just a MDP and we can apply any popular modern DRL methods to learn the adversary.

3.2 FINDING THE OPTIMAL POLICY UNDER A FIXED ADVERSARY

We now investigate SA-MDP when we fix the adversary ν and find an optimal policy. In Lemma 2, we show that this case SA-MDP becomes a POMDP:

Lemma 2 (Optimal policy under fixed adversary) *Given an SA-MDP* $M = (\mathcal{S}, \mathcal{A}, \mathcal{B}, R, p, \gamma)$ *and a fixed and stationary adversary* $\nu(a|s)$*, there exists a POMDP* $\bar{M} = (\mathcal{S}, \mathcal{A}, \mathcal{O}, \Omega, R, p, \gamma)$ *such that the optimal policy of* $\bar{M}$ *is the optimal policy* π *for SA-MDP given the fixed* ν*, where*

$$\mathcal{O} = \bigcup_{s \in \mathcal{S}} \{s' | s' \in supp(\nu(\cdot|s))\}, \qquad p(o_t = s' | s_t = s) = \nu(\hat{s}_t = s' | s_t = s) \qquad (1)$$

To prove Lemma 2, we construct the a POMDP with the observations defined on the support of all $\nu(s), s \in \mathcal{S}$ and the observation process is exactly the process of generating an adversarially perturbed state $\hat{s}$. This POMDP is functionally identical to the original SA-MDP when ν is fixed. This lemma unveils the connection between POMDP and SA-MDP: SA-MDP can be seen as a version of "robust" POMDP where the policy needs to be robust under a set of observational processes (adversaries). SA-MDP is different from robust POMDP (RPOMDP) (Osogami, 2015; Rasouli & Saghafian, 2018), which optimizes for the worst case environment transitions.

Algorithm 1 Learning an "optimal" adversary for perturbations on state observations

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Input: Policy $\pi(s)$ under attack, number of iterations N_{iter}, batch size B, perturbation set $\mathcal{B}(s)$
1: initialize adversary $\nu_\phi(s)$ parameterized by a neural network with parameters ϕ,
2: **for** $i = 1$ to N_{iter} **do**
3:     $\mathcal{D} \leftarrow Adv\_Traj(\nu_\phi, \pi, B)$ # collection of samples (for simplicity we ignore episodes here)
4:     $\phi \leftarrow \text{PolicyOptimizer}(\mathcal{D}, \phi)$
5: **end for**

Function $Adv\_Traj(\nu_\phi, \pi, B)$:
6: $s \leftarrow s_0$ # Initial state
7: $\mathcal{D} \leftarrow \emptyset$
8: **for** $b = 1$ to B **do**
9:     $\Delta \leftarrow \nu_\phi(s), \hat{s} \leftarrow \text{Proj}_{\mathcal{B}}(s)(s + \Delta)$ # projection will be a clipping for ℓ_∞ norm set $\mathcal{B}(s)$
10:     $a \leftarrow \pi(\hat{s})$
11:     obtain reward r, next state s' from environment given action a
12:     $\mathcal{D} \leftarrow \mathcal{D} \cup (s, \Delta, -r, s')$ # state, action, reward and next state for the adversary
13:     $s \leftarrow s'$
14: **end for**
15: **return** $\mathcal{D}$

As a proof of concept, we use a modern POMDP solver, SARSOP (Kurniawati et al., 2008) to solve the GridWorld environment in Figure 1 to find a policy that can defeat the adversary. The POMDP solver produces a finite state controller (FSC) with 8 states (FSC is an efficient representation of history dependent policies). This FSC policy can almost eliminate the impact of the adversary and receive close to perfect reward, as shown in Figure 1c.

Unfortunately, unlike MDPs, it is quite challenging to solve an optimal policy for POMDPs; state-of-the-art solvers (Bai et al., 2014; Sunberg & Kochenderfer, 2017) can only work on relatively simple environments which are much smaller than those used in modern DRL. Thus, we do not aim to solve the optimal policy. For the DRL setting, we follow (Wierstra et al., 2007) to use recurrent policy gradient theorem on POMDPs and use LSTM as function approximators for the value and policy networks. For example, for proximal policy gradient (PPO) we can use the loss function

$$L(\theta) = \mathbb{E}_{h_t}\left[r_{h_t}(\theta)A_{h_t}, \text{clip}(r_{h_t}(\theta), 1 - \epsilon, 1 + \epsilon)A_{h_t}\right], \text{where} r_{h_t}(\theta) = \frac{\pi_\theta(a_t|h_t)}{\pi_{\theta_{\text{old}}}(a_t|h_t)} \tag{2}$$

where $h_t = \{\hat{s}_0, a_0, \cdots, \hat{s}_t\}$ contains all history of states (perturbed states in our setting) and actions and A_{h_t} is a baseline advantage function also modeled using a LSTM. A LSTM or recurrent policy network has been used in the DRL setting in a few other works (Hausknecht & Stone, 2015; Azizzadenesheli et al., 2018), but our focus is to improve agent robustness rather than learning a policy purely for POMDPs. In our empirical evaluation, we will compare feedforward and LSTM policies under our ATLA framework.

3.3 ALTERNATING TRAINING WITH LEARNED ADVERSARIES (ATLA)

As we have discussed in Section 3.1, we can solve an optimal adversary given any fixed policy. In our ATLA framework, we train such an adversary online with the agent: we first keep the agent and optimize the adversary; the adversary is also parameterized as a neural network. Then we keep the adversary and optimize the agent. Both adversary and agent can be updated using a policy gradient algorithm such as PPO. We show our full algorithm in Algorithm 2.

Our algorithm is designed to use a strong and learned adversary that tries to find intrinsic weakness of the policy, and to obtain a good reward the policy must learn to defeat such an adversary. In other words, it attempts to solve the SA-MDP problem directly rather than relying on explicit regularization on the function approximator like the approach in (Zhang et al., 2020). In our empirical evaluation, we show that such regularization can be unhelpful in some environments and harmful for performance when evaluating the agent without attacks.

The difference between our approach and previous training time attack approaches such as in (Pattanaik et al., 2018) is that we use a stronger adversary, learned online with the agent. Our empirical evaluation finds that using such an adversary in training time allows the agent to learn a robust policy generalized to different types of strong adversarial attacks during test time. Additionally, it is

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Algorithm 2 Alternating Training with Learned Adversaries (ATLA)

Input: Environment $\mathcal{E}$, number of iterations N_{iter}, and batch size B.
1: Initialize the agent's actor network $\pi(a|\hat{s})$ with parameters θ.
2: Initialize the adversary's actor network $\nu(\hat{s}|s)$ with parameters ϕ.
3: **for** $i = 1$ to N_{iter} **do**
4:     **for** $j = 1$ to N_π **do**
5:         Run π_θ with fixed ν_ϕ to collect a set of trajectories $\mathcal{D} := \{(\hat{s}_t^{k,j}, a_t^{k,j}, r_t^{k,j}, \hat{s}_{t+1}^{k,j})\}\big|_{k=1}^{B}$.
6:         $\theta \leftarrow$ PolicyOptimizer$(\mathcal{D}, \theta)$
7:     **end for**
8:     **for** $j = 1$ to N_ν **do**
9:         $\mathcal{D} \leftarrow Adv\_Traj(\nu_\phi, \pi_\theta, B)$ # Adv_Traj defined in Algorithm 1
10:         $\phi \leftarrow$ PolicyOptimizer$(\mathcal{D}, \phi)$
11:     **end for**
12: **end for**

Table 1: Average rewards $\pm$ standard deviation over 50 episodes on PPO and SA-PPO models. We report natural rewards (no attacks) and rewards under four adversarial attacks in Zhang et al. (2020) and our "optimal" attack. In each row we bold the best (lowest) attack reward over all five attacks. "Optimal" attack is better than other attacks in all environments, sometimes by a large margin.

Env.	ℓ_∞ norm perturbation budget ϵ	Method	Natural Reward	Attack Reward				
				Critic	Random	MAD	RS	"Optimal"
Hopper	0.075	PPO	2554±853	1464 ±523	2101±793	1410± 655	794±238	**373± 9**
		SA-PPO	2234± 668	3789± 15	2710± 801	2652± 835	1130 ±42	**751± 465**
Walker2d	0.05	PPO	3460 ± 1170	3424 ± 1295	3007 ± 1200	2869 ± 1271	1336 ± 654	**454±16**
		SA-PPO	4775± 591	4875± 30	4867± 39	3668± 1789	3808± 138	**1723± 1555**
Ant	0.15	PPO	5485 ± 1160	4934± 1022	5261± 1005	1759± 828	268 ±227	**-872 ± 436**
		SA-PPO	5067± 695	4805 ± 128	4986 ±452	4662 ±522	3412 ±1755	**2511 ± 1117**
HalfCheetah	0.15	PPO	7112± 113	5761±119	5486 ± 1378	1836± 866	489± 758	**-637± 267**
		SA-PPO	3635± 21	3589± 21	3619± 18	3624± 23	3283± 20	**3036 ±17**

important to distinguish between the original state s and the perturbed state $\hat{s}$. We find that using s instead of $\hat{s}$ to train the advantage function and policy of the agent leads to worse performance, as it does not follow the theoretical framework of SA-MDP.

4 EXPERIMENTS

"Optimal" attack on DRL agents In section 3.1 we show that it is possible to cast the optimal adversary finding problem as an MDP problem. In practice, the environment dynamics are unknown but model-free RL methods can be used to approximately find this optimal adversary. In this section, we use PPO to train an adversary on 4 MuJoCo continuous control environments. In Table 1 we present results on attacking vanilla PPO and robustly trained SA-PPO (Zhang et al., 2020) models. As a comparison, we also report the attack reward of four other baseline attacks, the same as in (Zhang et al., 2020): critic attack is based on (Pattanaik et al., 2018); random attack adds uniform random noise to state observation; MAD (maximal action difference) attack maximizes the differences in action under perturbed state; RS (robust sarsa) attack is based on training robust action-value functions and was the strongest attack reported in (Zhang et al., 2020). For all attacks in this paper we consider $\mathcal{B}(s)$ as a ℓ_∞ norm ball around s with radius ϵ, set similarly as in (Zhang et al., 2020). During testing, we run the models without attacks as well as under attacks for 50 episodes and report the mean and standard deviation of the reward. In Table 1 our "optimal" attack achieves noticeably lower rewards than all the other four attacks. We illustrate a few examples of attacks in Figure 3. For each method, we train with the best hyper-parameters for at least five times and choose the median model for this experiment. For RS and "optimal" attacks, we report the best (lowest) attack reward obtained from different hyper-parameters.

Evaluation of ATLA In this experiment, we study the effectiveness of our proposed ATLA method. Specifically, we use PPO as our policy optimizer. For policy networks, we have two different structures: the original fully connected (MLP) structure, and an LSTM structure which takes historical observations. The LSTMs are trained using backpropagation through time for up to 100 steps. In Table 2 we include the following methods for comparisons:

- PPO (vanilla) and PPO (LSTM): PPO with a feedforward NN or LSTM as the policy network.

- SA-PPO: the state-of-the-art approach for improving the robustness of DRL in continous control environments, using a smooth policy regularization solved convex relaxations of NNs.

Table 2: Average rewards $\pm$ standard deviation over 50 episodes on ATLA models and baselines. We report natural rewards (no attacks) and the best (lowest) attack rewards among five types of adversarial attacks, including four attacks used in Zhang et al. (2020) (Critic, Random, MAD, and RS) and our "optimal" attack. For each environment, we bold the most robust model. Since both RS attack and our "optimal" attack are parameterized attacks, the "best attack" columns represent the worst case agent performance *under hundreds of adversaries*. See Appendix A.1 for more details.

Env.	State Dimension	ℓ_∞ norm perturbation budget ϵ	Method	Natural Reward	Best Attack
Hopper	11	0.075	PPO (vanilla)	2554±853	373± 9
			SA-PPO	2234± 668	751± 465
			ATLA-PPO (MLP)	2559 ± 958	976± 40
			PPO (LSTM)	3060± 639.3	784± 48
			ATLA-PPO (LSTM)	3487± 452	1224± 191
			ATLA-PPO (LSTM) +SA Reg	3291± 600	**1455± 248**
Walker2d	17	0.05	PPO (vanilla)	3460 ± 1170	454±16
			SA-PPO	4775± 591	1723± 1555
			ATLA-PPO (MLP)	3138 ± 1061	2213± 915
			PPO (LSTM)	2785± 1121	1259± 937
			ATLA-PPO (LSTM)	3920± 129	3219 ± 1132
			ATLA-PPO (LSTM) +SA Reg	3842± 475	**3239± 894**
Ant	111	0.15	PPO (vanilla)	5485 ± 1160	-872 ± 436
			SA-PPO	5067± 695	2511 ± 1117
			ATLA-PPO (MLP)	4894± 123	33±327
			PPO (LSTM)	5696 ± 165	-513 ± 104
			ATLA-PPO (LSTM)	5612± 130	716± 256
			ATLA-PPO (LSTM) +SA Reg	5393±139	**3759± 112**
HalfCheetah	17	0.15	PPO (vanilla)	7112± 113	-637± 267
			SA-PPO	3635± 21	3036 ±17
			ATLA-PPO (MLP)	5417± 49	2170± 2097
			PPO (LSTM)	5609± 98	-886± 30
			ATLA-PPO (LSTM)	5766 ± 109	2485± 1488
			ATLA-PPO (LSTM) +SA Reg	6300± 261	**4806± 603**

• ATLA-PPO (MLP) and ATLA-PPO (LSTM): Our proposed method trained with a feedforward NN (MLP) or LSTM as the policy network. The agent and adversary are trained using PPO with independent value and policy networks. For simplicity, we set $N_\pi = N_\nu = 1$ in all settings.

• ATLA-PPO (LSTM) +SA reg: Based on ATLA-PPO (LSTM), but with an extra adversarial smoothness constraint similar to those in SA-PPO. We use a 2-step stochastic gradient Langevin dynamics (SGLD) to solve the minimax loss, as convex relaxations of LSTMs are expensive.

For each model, we report its "natural reward" (without attacks) and best attack reward in Table 2. The best attack reward is the *lowest* reward achieved by all five types attacks in Table 1, including our new "optimal" attack (these include hundreds of adversaries for attacking a single agent, see Appendix A.1 for more details). For reproducibility, for each setup we train at least 5 (up to 21) agents, attack all of them and report the one with *median* robustness. We include detailed hyperparameters in A.4. In Table 2 we can see that vanilla PPO with MLP or LSTM are not robust. Using LSTM along does not make the policy more robust. However both ATLA-PPO (LSTM) and ATLA-PPO (MLP) can significantly improve agent robustness, and LSTM tends to be more robust, validating our findings in Section 3.2. ATLA-PPO (LSTM) is better than SA-PPO on Hopper and Walker2d; for higher dimensional environments like Ant, a robust function approximator regularization in SA-PPO is quite effective. Our ATLA approach that also includes this regularization (ATLA-PPO

Figure 4: The performance under the strongest attack for SA-PPO Hopper with different regularization κ. Even we increase regularization, it cannot outperform our ATLA agents.

+SA Reg) outperforms other baselines, as this combination improves both the intrinsic robustness of policy and the robustness of function approximator.

A robust functional approximator can be insufficient For some environments, SA-PPO method has its limitations - even using an increasingly larger regularization parameter κ (which controls how robust the function approximator needs to be), we still cannot reach the same performance as our ATLA agent (Figure 4). Additionally, when a large regularization is used, agent performance becomes much worse. In Figure 4, under the largest $\kappa = 1.0$, the natural reward (1436 ± 96) is much lower than other agents reported in Table 2.

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A APPENDIX

A.1 FULL RESULTS OF ALL ENVIRONMENTS UNDER DIFFERENT TYPES OF ATTACKS

In Table 2, we only include the best attack rewards (lowest rewards over all attacks). In Table 3 we list the rewards under each specific attack. Note that, Robust Sarsa (RS) attack and our "optimal" policy attack both have hyperparameters. For RS attack we use the same set of 30 different settings of hyperparameters to train a robust value function to attack the network. The reported RS attack result for each agent is the strongest one over the 30 trained value functions. For our "optimal" policy attack, the hyperparameters are PPO training parameters for the adversary (including the learning rate of the adversary policy network, learning rate of the adversary value network, the entropy regularization parameter and the ratio clip ϵ for PPO). We use a grid search of these hyperparameters to train an adversary that is as strong as possible, resulting in 100 to 200 adversaries produced for each agent. The reported optimal attack rewards is the lowest reward among all trained adversaries. Under this comprehensive adversarial evaluation, each agent is tested using hundreds of adversaries and the strongest adversary determines the true robustness of an agent.

Table 3: Average rewards $\pm$ standard deviation over 50 episodes on five baselines and SA-PPO. We report natural rewards (no attacks) and rewards under five adversarial attacks, including four attacks proposed in Zhang et al. (2020) (Critic, Random, MAD, and RS) and the optimal attack proposed in this paper. In each row we bold the best (lowest) attack reward over all five attacks.

Env.	ℓ_∞ norm perturbation budget ϵ	Method	Natural Reward	Attack Reward					Best Attack
				Critic	Random	MAD	RS	"Optimal"	
Hopper	0.075	PPO (vanilla)	2554±853	1464 ±523	2101±793	1410± 655	794±238	**373± 9**	373
		SA-PPO	2234± 668	3789± 15	2710± 801	2652± 835	1130 ±42	**751± 465**	751
		ATLA-PPO (MLP)	2559 ± 958	3497± 556	2153± 882	1679±676	2329± 870	**976± 40**	976
		PPO (LSTM)	3060± 639.3	2705± 986	2410± 786	2397± 905	811± 74	**784± 48**	784
		ATLA-PPO (LSTM)	3487± 452	3524± 550	3474± 401	3081± 754	1567± 347	**1224± 191**	1224
		ATLA-PPO (LSTM)+ SA Reg	3291± 600	2073± 824	3165 ± 576	2814± 725	2244± 618	**1455± 248**	1455
Walker2d	0.05	PPO (vanilla)	3460 ± 1170	3424 ± 1295	3007 ± 1200	2869 ± 1271	1336 ± 654	**454±16**	454
		SA-PPO	4775± 591	4875± 30	4867± 39	3668± 1789	3808± 138	**1723± 1555**	1723
		ATLA-PPO (MLP)	3138 ± 1061	3243± 1004	3384 ± 1056	2596± 1005	3367± 1020	**2213± 915**	2213
		PPO (LSTM)	2785± 1121	2730± 1082	2578 ± 1007	2471± 1109	**1259± 937**	1523± 869	1259
		ATLA-PPO (LSTM)	3920± 129	3915± 274	3779 ± 541	3963 ± 36	**3219 ± 1132**	3463± 1016	3219
		ATLA-PPO (LSTM) +SA Reg	3842± 475	3884± 132	3927± 368	3836± 492	**3239± 894**	3676± 602	3239
Ant	0.15	PPO (vanilla)	5485 ± 1160	4934± 1022	5261± 1005	1759± 828	268 ±227	**-872 ± 436**	-872
		SA-PPO	5067± 695	4805 ± 128	4986 ±452	4662 ±522	3412 ±1755	**2511 ± 1117**	2511
		ATLA-PPO (MLP)	4894± 123	4427± 104	4760 ± 108	1891± 885	1857± 567	**33±327**	33
		PPO (LSTM)	5696 ± 165	5519 ± 114	5475 ± 691	1069 ± 382	**-513 ± 104**	716± 256	-513
		ATLA-PPO (LSTM)	5612± 130	5196 ± 134	5390 ± 704	3903 ± 217	1096 ± 329	**716± 256**	716
		ATLA-PPO (LSTM) +SA Reg	5393 ±139	5295± 165	5366± 104	5240± 170	4136± 149	**3759± 112**	3759
HalfCheetah	0.15	PPO (vanilla)	7112± 113	5761±119	5486 ± 1378	1836± 866	489± 758	**-637± 267**	-637
		SA-PPO	3635± 21	3589± 21	3619± 18	3624± 23	3283± 20	**3036 ±17**	3036
		ATLA-PPO (MLP)	5417± 49	5134± 38	5388 ± 34	4623 ±1146	2709± 80	**2170± 2097**	2170
		PPO (LSTM)	5609± 98	4294± 112	5395± 158	4768± 106	2899 ± 2006	**-886± 30**	-886
		ATLA-PPO (LSTM)	5766 ± 109	4008± 1031	5685 ± 107	4807± 154	3458± 1338	**2485± 1488**	2485
		ATLA-PPO (LSTM) +SA Reg	6300± 261	5991± 209	6164±603	5790± 174	**4806± 603**	4971± 357	4806

A.2 NETWORK STRUCTURE

For fully connected networks, we use the same network as in (Zhang et al., 2020), which contains 2 hidden layers with 64 hidden neurons each layer, for both policy and value networks, for both the agent and the adversary. For LSTM agents, we use a single layer LSTM with 64 hidden neurons, along with an input embedding layer projecting state dimension to 64 and an output layer projecting 64 to output dimension. For LSTM agents, when conducting the "optimal" attack, we also use a LSTM network for the adversary to ensure the adversary is powerful enough.

A.3 HYPERPARAMETER FOR THE LEARNING-BASED "OPTIMAL" ATTACK

Our "optimal" attacks uses policy gradient methods to learn the optimal adversary during agent testing, and each learning process involves the selection of hyperparameters. Specifically, the hyperparameters include the learning rates of the adversary's policy and value networks, the entropy coefficient, and the annealing of the learning rate. To reduce search space, for ATLA models, the learning rates of the testing phase adversary's policy and value networks are chosen ranging from 0.3X to 3X of the learning rates of adversary's policy and value networks used in training. For other models trained without an adversary, the learning rates of the testing phase adversary's policy and value networks are chosen ranging from 0.3X to 3X of the learning rates of the agent's policy and value networks. We tested both linearly annealed learning rate and non-annealing learning

rate. The adversary's entropy coefficient is chosen form 0 and 0.003. The final results reported in all tables are the best (lowest) reward achieved by the "optimal" attacks among all hyperparameter configurations. Typically this includes around 100 to 200 different adversaries trained with different hyperparameters. This guarantees the strength of this attack and allows a comprehensive evaluation of the robustness of all agents.

A.4 HYPERPARAMETERS FOR ATLA PERFORMANCE EVALUATION

Hyperparameters for PPO (vanilla)   For the Walker2d and Hopper environment, we use the same set of hyperparameters as in (Zhang et al., 2020); the hyperparameters were originally from (Engstrom et al., 2020) and found using a grid search experiment. We found that this set of hyperparameters work well. For HalfCheetah and Ant environment, we use a grid search of hyperparameters, including the learning rate of the policy network, learning rate of the value network and the entropy bonus coefficient. For Hopper, Walker2d and HalfCheetah environments, we train for 2 million steps (2 million environment interactions). For Ant, we train for 10 million steps. Training for longer may slightly improve agent performance under no attacks, but has no impact for performance under strong adversarial attacks.

Hyperparameters for PPO (LSTM)   For PPO (LSTM), we conduct a smaller scale hyperparameter search. We search hyperparameter values that are close to the optimal ones found for the PPO vanilla model. We train these LSTM agents for the same steps as those in vanilla PPO.

Hyperparameters for SA-PPO   We use the same value for all hyperparameters as in vanilla PPO except SA-PPO's extra κ for the strength of SA-PPO regularization. For κ, we choose from 1×10^{-6} to 1. We train models with each κ at least five times and choose the κ value whose median model has the highest worst-case reward under all attacks.

Hyperparameters for ATLA-PPO   For ATLA-PPO, we have hyperparameters for both agent and adversary. We keep all agent hyperparameters the same as those in vanilla MLP/LSTM agents, except for the entropy bonus coefficient. We find that sometimes we need a larger entropy bonus coefficient in ATLA to allow sufficient exploration of the agent, as learning with an adversary is harder than learning in attack-free environments. For the adversary, we run a small-scale hyperparameter search on the learning rate of adversary policy and value networks, and the entropy bonus coefficient for the adversary. To reduce the number of hyperparameters for searching, we use values close to those of the agent. We set $N_\nu = N_\pi = 1$ in all experiments and did not tune this hyperparameter. For ATLA, we train 5 million steps for Hopper, Walker and HalfCheetah and 10 million steps for Ant. We find that similar to the observations in (Madry et al., 2018), training with an adversary typically requires more steps to converge, however in all our environments the training does reliably converge.

Model selection   For each setup, we repeat the experiments using the same set of hyperparameters for at least 5 times, and at most 21 times for some high variance settings. We then attack all the models using random, critic, MAD and RS attacks. We use the lowest reward among all attacks as a metric to rank those models. Then, we select the model with *median* robustness as our final model. This final model is then attacked using the "optimal" attack to further reduce its reward. The numbers we report in Table 2 are not from the best runs, but the runs with median robustness. This is done to improve reproducibility as RL training process can have high variance.

Table 4: Hyperparameters for all environments and settings. For vanilla environments, we use the hyperparameters from Zhang et al. (2020) and Engstrom et al. (2020) if they are available for that environment (Hopper and Walker2d). Other environments' hyperparameter for the vanilla PPO model is found by a grid search. For SA-PPO and ATLA-PPO (MLP), the same set of hyperparameters as in the vanilla models are used, except that for SA-PPO we tune the parameter κ and for ATLA-PPO (MLP) we tune the entropy bonus coefficients as well as learning rates for the adversary. For LSTM models, we first tune the vanilla LSTM PPO models and find the best learning rates, keep using them in all LSTM based models.

Env.	model	policy lr	val lr	entropy coeff.	κ	adv. policy lr	adv. val lr	adv. entropy coeff.
Hopper	PPO(vanilla)	3e-4	2.5e-4	0	–	–	–	–
	SA-PPO	3e-4	2.5e-4	0	0.03	–	–	–
	ATLA-PPO (MLP)	3e-4	2.5e-4	0.01	–	0.001	0.0001	0.001
	PPO (LSTM)	1e-3	3e-4	0.0	–	–	–	–
	ATLA-PPO (LSTM)	1e-3	3e-4	0.01	–	0.01	0.01	0.001
	ATLA-PPO (LSTM)+ SA Reg	1e-3	3e-4	0.01	0.3	0.003	0.01	0.003
Walker2d	PPO(vanilla)	4e-4	3e-4	0	–	–	–	–
	SA-PPO	4e-4	3e-4	0	–	–	–	–
	ATLA-PPO (MLP)	4e-4	3e-4	0.0003	–	0.0001	0.0001	0.002
	PPO (LSTM)	1e-3	3e-2	0	–	–	–	–
	ATLA-PPO (LSTM)	1e-3	3e-2	0.001	–	0.0003	0.03	0
	ATLA-PPO (LSTM)+ SA Reg	1e-3	3e-2	0.001	0.3	0.003	0.03	0.001
Ant	PPO(vanilla)	5e-5	1e-5	0	–	–	–	–
	SA-PPO	5e-5	1e-5	0	3e-3	–	–	–
	ATLA-PPO (MLP)	5e-5	1e-5	3e-4	–	1e-05	3e-06	0
	PPO (LSTM)	3e-4	3e-4	0	–	–	–	–
	ATLA-PPO (LSTM)	3e-4	3e-4	0.0003	–	0.0003	0.0001	0.0003
	ATLA-PPO (LSTM)+ SA Reg	3e-4	3e-4	0.003	0.1	0.0003	3e-05	3e-05
HalfCheetah	PPO(vanilla)	3e-4	1e-4	0	–	–	–	–
	SA-PPO	3e-4	1e-4	0.1	–	–	–	–
	ATLA-PPO (MLP)	3e-4	1e-4	0.0003	–	0.001	0.0003	0.003
	PPO (LSTM)	1e-3	3e-4	0	–	–	–	–
	ATLA-PPO (LSTM)	1e-3	3e-4	0.0003	–	0.003	0.001	0
	ATLA-PPO (LSTM)+ SA Reg	1e-3	3e-4	0	0.03	0.003	0.003	0.0003