Identify and Remove Backdoor Neurons through Clean-Poisoned Mixture Distribution

Abstract

Convolutional neural networks (CNN) can be manipulated to perform specific behaviors when encountering a particular trigger pattern without affecting the performance on normal samples, which is referred to as backdoor attack. Backdoor attack is usually achieved by injecting a small proportion of poisoned samples into the training set, through which the victim trains a model embedded with the designated backdoor. In this work, we demonstrate that the backdoor neurons in an infected neural network have a mixture of two distributions with significantly different moments, formed by benign samples and poisoned samples, respectively. This property is shown to be attack-invariant and allows us to efficiently locate the backdoor neurons. On this basis, we make several realistic assumptions on the neuron activation distributions, and propose two backdoor neuron detection strategies based on (1) the differential entropy of the neurons, and (2) the KL divergence between the benign sample distribution and a poisoned statistics based hypothetical distribution. Experimental results show that our proposed defense strategies are both efficient and effective against various backdoor attacks.

1 Introduction

Convolutional neural networks (CNNs) have achieved tremendous success during the past few years in a wide range of areas. However, training a CNN from scratch involves a large amount of data and expensive computational cost, which is sometimes infeasible. A more practical strategy is to obtain pretrained models or utilize public datasets from a third party, which brings convenience but also raises severe security problems into the deployment of models. For example, a malicious third party may provide pretrained models embedded with a designated backdoor, such that the model will have a predefined response to some specific pattern, which is also called the *trigger*. More realistically, the attacker can inject only a small proportion of malicious data into the public dataset to mislead the trained model, which is referred to as *backdoor poisoning attacks* [25]. For instance, the malicious data can be created by patching a particular pattern into the benign data, and changing the label to the desired target. The correlation of the trigger and the specified target label will be learned by the models during the training time. In this way, the infected model will misclassify the input to the attack target when the pattern is patched, while behave normally otherwise, as shown in Figure 1.

Due to the limited understanding of CNNs, we are not clear on the formation mechanism of backdoor behaviors. However, it was empirically found that a infected model always possesses one or more neurons that have high correlation with the trigger activation, and pruning these neurons can significantly alleviate the backdoor behaviors, while retaining the model performance [42, 28, 6]. Nevertheless, how to precisely find out these backdoor neurons in a infected model is still a challenging problem, and has attracted a lot of attentions from the community.

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Figure 1: An overview of an infected learning system. The images with a white square are classified as class 0. It is an empirical observation that the backdoor behaviors are always triggered by one or more backdoor neurons. We demonstrate that the distributions of activations on these neurons are mixtures of two Gaussian-like distributions, formed by benign samples and poisoned samples, respectively.

In this work, we will take an inspection on the pre-activation distributions of infected models. In general, the activations in each neuron follow an unimodal distribution that can be approximated by a Gaussian distribution. Based on the maximum entropy property of the Gaussian distribution, these benign neurons should have relatively large entropy on their pre-activation distributions. However, in the backdoor neurons, the distribution is always bimodal and can be approximated by a mixture of two Gaussian distributions, formed by the benign data and poisoned data, respectively; see Figure 1. This kind of distribution must have a lower entropy, compared with a Gaussian distribution with the same finite variance. Thus, if we standardize the pre-activation distributions in all neurons, the backdoor neurons should possess a relatively low entropy compared with the benign neurons. We treat the low entropy neurons as outliers and potential backdoor neurons, and prune these neurons to recover the model without retraining. However, under another defense setting, in which only an infected model and a small set of benign data are provided, we may not be able to observe the bimodal distributions on the backdoor neurons since the poisoned data is absent. In this case, we can rely on the statistics on *Batch Normalization* (BN) layers. Specifically, if the infected model is trained on poisoned data, the statistics of backdoor neurons recorded in the BN layer will be significantly different from the distribution of only benign data. More importantly, the mismatch of statistics will not exist in benign neurons. Based on the neuron entropy and the statistics discrepancy, we are able to locate and prune the backdoor neurons to recover the model under two defense settings.

In summary, our contributions include:

1. We take a deep inspection on the infected model, and summarize the law of pre-activation distributions on poisoned dataset. We find that (1) the standardized entropy of backdoor neurons can be significantly lower than benign neurons, and (2) the BN statistics in infected model are mismatched with the benign sample statistics.

2. We propose to prune the potential backdoor neurons based on either the sample entropy or the statistics discrepancy, depending on the defense settings. Under certain assumptions, we claim that both the proposed indices can successfully separate the benign neurons and backdoor neurons by an appropriate threshold.

3. We conduct extensive experiments to verify our assumptions and evaluate our proposed methods, and achieve the state-of-the-art results under two different defense settings.

2   Related work

In this section, we detailedly discuss recent works in backdoor attack and defense.

2.1   Backdoor attacks

The concept of *backdoor attack* is first introduced in [14], where the adversary injects a small set of targeted label-flipped data stamped with a small and specific trigger into the training set during the DNN training, leading to a misclassification when predicting the samples with such trigger. To make the trigger pattern even more invisible to human beings, the blending strategy is used in [5]

to generate poison images, while the form of natural reflection is utilized in trigger design in [31]. The input image is perturbed in [40] to keep its content consistent with the target label such that the model better memorizes the trigger pattern, and keep it imperceptible to human beings. Moreover, the multi-target and multi-trigger attacks are proposed in [44, 33], and make the attack more flexible and covert. Recently, some sample specific trigger design strategies [27] are proposed, making the defense against such backdoor attack much harder. Generally, the above attacks can be referred as the *poisoning based backdoor attacks*.

Under some settings, the attackers can control the training process to inject the backdoor without modifying the training data, referred as the *non-poisoning based backdoor attacks*. This is achieved in [30, 36, 4] through targeted modification of the neurons' weight in a network. Such attacks will not be evaluated in our work due to its strong attack setting.

2.2 Backdoor defenses

Training stage defense. Under such setting, the defender has access to the training process, so that they can detect and filter the poisoned data or add some restrictions to suppress the backdoor effect in training. Since the poisoned data can be regarded as outliers, different strategies are applied in [10, 12, 1, 39, 15], such as the *robust statistics* in feature space and *input perturbation techniques* to filter them out of training data. Other methods aim at suppressing the backdoor effect during training phase with strong data augmentation methods [2] [26] [35] [32] including *CutMix* [45], *Flip*, *ShrinkPad* [26], *CutOut* and *MaxUp* [13], or *differential privacy* constraints [11, 18].

Model post-processing defense. Sometimes the defenders are only given a suspicious DNN model without access to the training process or the full training set. Therefore, they must eliminate the backdoor threat with limited resources, such as a small set of clean data. A straightforward way is to reconstruct the trigger by adding adversarial perturbations to the input images, and then detoxify the model with the knowledge of reversed trigger [41]. Some try to find the relationship between backdoor behaviors and the neurons in a DNN model. Different levels of stimulation to a neuron are introduced in [29] to see how to determine the output activation change, if the model is attacked. Simple neuron pruning strategies are applied in [6] to repair the model, while adversarial perturbations are added to the neurons in [42] and precisely prunes the backdoor neurons with more limited clean data requirement and better performance. Simple redundant neuron pruning and fine-tuning are combined together in [28] to erase the backdoor effect. There are other fine-tuning based methods with the implementation of knowledge distillation [24, 17], while they may suffer from the hyper-parameter tuning and clean accuracy dropping problems due to limited prior knowledge of the attack and over-fitting on the clean set. Mode connectivity repair technique [46] is also explored to mitigate the backdoored model. Recently, the *K-Arm optimization* [38] is applied in backdoor detection, and outperforms other adversarial perturbation based methods [41, 8], helping curtail the threat of backdoor attack.

3 Preliminaries

3.1 Notations

Consider a multi-class classification problem with C classes. Let the original training set $\mathcal{D} = \{(\boldsymbol{x}_i, y_i)\}_{i=1}^{N}$ contains N i.i.d. sample images $\boldsymbol{x}_i \in \mathbb{R}^{d_c \times d_h \times d_w}$ and the corresponding labels $y_i \in \{1, 2, ..., C\}$ drawn from $\mathcal{X} \times \mathcal{Y}$. Here, we denote by d_c, d_h and d_w the number of neurons, the height and the width of images, respectively. In particular, we have $d_c = 3$ for RGB images.

As in Section 2.1, the backdoor poisoning attack involves changes to the input images and the corresponding labels on a subset $\mathcal{D}_p \subseteq \mathcal{D}$. In this work, we define the ratio $\rho = \frac{|\mathcal{D}_p|}{|\mathcal{D}|}$ as the *poisoning rate*. We denote the poisoning function to the input images as $\delta(\boldsymbol{x})$.

Consider a neural network $F(x; \theta)$ with L layers. Denote

$$F^{(l)} = f^{(l)} \circ \phi \circ f^{(l-1)} \circ \phi \circ \cdots \circ \phi \circ f^{(1)},$$

for $1 \leq l \leq L$, where $f^{(l)}$ is a linear function (*e.g.*, convolution) in the l-th layer, and ϕ is a nonlinear activation function applied element wise. In this work, we may denote $F(x; \theta)$ as $F(x)$ or F for simplicity.

We denote by $\boldsymbol{W}^{(l)} \in \mathbb{R}^{d_{c'} \times d_c \times d_h \times d_w}$ the weight tensor of a convolutional layer. To do pruning, we apply a mask $\boldsymbol{M}^{(l)} \in \{0,1\}^{d_{c'} \times d_c \times d_h \times d_w}$ starting with $\boldsymbol{M}^{(l)} = \mathbb{1}_{d_{c'} \times d_c \times d_h \times d_w}$ in each layer. Pruning neurons on the network refers to getting a collection of indices $\mathcal{I} = \{(l,k)_i\}_{i=1}^{I}$ and setting $\boldsymbol{M}_k^{(l)} = \boldsymbol{0}_{d_c \times d_h \times d_w}$ if $(l,k) \in \mathcal{I}$. The pruned network $F_{-\mathcal{I}}$ has the same architecture as F but with all the weight matrices of convolutional layers set to $\boldsymbol{W}^{(l)} \odot \boldsymbol{M}^{(l)}$, where $\odot$ denotes the Hadamard product.

3.2 Differential entropy

To measure the uncertainty of a discrete random variable Z, the *entropy* [37, 7] was defined as $H(Z) = -\sum_{z \in Z} p(z) \log p(z)$. At the same time, as an extension of entropy, the *differential entropy* was also introduced for a continuous random variable. More concretely, if Z is a continuous random variable, then it was defined as

$$h(Z) = -\int_Z p(z) \log p(z) dz. \tag{1}$$

An important fact about the differential entropy is that, among all the real-valued distributions supported on $(-\infty, \infty)$ with a specified finite variance, the Gaussian distribution maximizes the differential entropy [7]. In this work, the differential entropy (1) will be utilized to identify the distributions that are far different from a Gaussian distribution.

3.3 Backdoor neurons

It was found that there exist one or more neurons that contribute the most to the backdoor behaviors in a infected model [42, 28]. If some of or all of these neurons are pruned, the *attack success rate* will be reduced greatly [42]. In this work, to better quantify the importance of neurons to backdoor behaviors, we would like to introduce the sensitivity of neurons to the backdoor by the backdoor loss calculated before and after pruning the neuron:

$$\alpha(F, l, k) = \mathcal{L}_{\text{bd}}(F) - \mathcal{L}_{\text{bd}}(F_{-\{(l,k)\}}), \tag{2}$$

where $F_{-\{(l,k)\}}$ is the network after pruning the k-th neuron of the l-th layer. The *backdoor loss* is defined as:

$$\mathcal{L}_{\text{bd}}(f) = \mathbb{E}_{(\boldsymbol{x},y) \sim \mathcal{D}}[\mathrm{D}_{\text{CE}}(y, f(\delta(\boldsymbol{x})))],$$

where D_{CE} denotes the cross entropy loss. The backdoor loss is high when the model is infected, and will be reduced when the backdoor effect is alleviated.

Using the quantity define in (2), we are now able to find the neurons that are mostly correlated with the backdoor behaviors. More concretely, we first set a threshold $\tau > 0$, and then go through all the neurons to find the ones with the quantity (2) above τ. We call them the *backdoor neurons*, and denote

$$\mathcal{B}_{F,\tau} = \{(l,k) : \alpha(F, l, k) > \tau\}. \tag{3}$$

3.4 Pre-activation distribution

During the forward propagation of an input $\boldsymbol{x}$, we denote $\boldsymbol{x}^{(l)} = F^{(l)}(\boldsymbol{x}) \in \mathbb{R}^{d_c^{(l)} \times d_h^{(l)} \times d_w^{(l)}}$ as the output of the l-th layer. For the k-th neuron of the l-th layer, the *pre-activation* $\boldsymbol{\phi}_k^{(l)} = \phi(\boldsymbol{x}_k^{(l)})$ is defined as the maximum value of the k-th slice matrix of dimension $d_h^{(l)} \times d_w^{(l)}$ in $\boldsymbol{x}^{(l)}$.

It is a common assumption that, for every neuron, the pre-activations before the non-linear function follow a Gaussian distribution, if the network is randomly initialized and the number of neurons is large enough [21, 3]. In a trained network, although this assumption may not strictly hold, the pre-activation of every neuron can be still regarded as approximately following a Gaussian distribution. However, in this work, for the first time, we observe a bimodal distribution in the backdoor neurons, two components of which are formed by the benign data and poisoned data, respectively. This phenomenon is shown in Figure 2, where a typical backdoor neuron is compared with the benign neurons. It can be seen that, after the model is infected, the pre-activation distributions of benign neurons hardly change when the data is poisoned, while the pre-activation distributions of backdoor neurons become significantly different.

| (a) Benign neuron | (b) Backdoor neuron | (c) Benign neuron | (d) Backdoor neuron |

Figure 2: In (a) and (b), we compare the pre-activation distributions in backdoor neurons and benign neurons. In benign neurons, the pre-activation distributions on benign data and poisoned data are nearly the same, while in backdoor neurons, they show great difference. In (c) and (d), we plot the empirical distributions with benign samples (in blue) and the BN statistics induced Gaussians (in green). In backdoor neurons, the discrepancy between the empirical and BN induced distribution is large (all the neurons are selected from infected ResNet-18 trained on CIFAR-10, and use 1,000 images with (poisoned data) or without trigger (benign data) as the inputs).

4 Methodology

4.1 Assumptions

A primary assumption is that $|\mathcal{B}_{F,\tau}| > 0$ for a poisoned model F and a pre-defined threshold $\tau > 0$, where $\mathcal{B}_{F,\tau}$ is defined as in (3). As in Section 3.4, we also assume that the pre-activations of all neurons follow a Gaussian mixture distribution, that is:

$$\phi_k^{(l)} \sim (1-\rho)\mathcal{N}(\mu_k^{(l)}, \sigma_k^{(l)2}) + \rho\mathcal{N}(\hat{\mu}_k^{(l)}, \hat{\sigma}_k^{(l)2}), \tag{4}$$

where ρ is the poisoning rate of the dataset, $\mu_k^{(l)}$ and $\sigma_k^{(l)2}$, $\hat{\mu}_k^{(l)}$ and $\hat{\sigma}_k^{(l)2}$ are the mean and variance of $\{\phi(F^{(l)}(\boldsymbol{x})_k) : \boldsymbol{x} \sim \mathcal{X}\}$, $\{\phi(F^{(l)}(\delta(\boldsymbol{x}))_k) : \boldsymbol{x} \sim \mathcal{X}\}$, respectively.

We further assume that:

$$|\mu_k^{(l)} - \hat{\mu}_k^{(l)}| \begin{cases} < \epsilon, & \text{if } (l, k) \notin \mathcal{B}_{F,\tau}, \\ \gg \epsilon, & \text{if } (l, k) \in \mathcal{B}_{F,\tau}, \end{cases}$$

and

$$|\sigma_k^{(l)2} - \hat{\sigma}_k^{(l)2}| \begin{cases} < \epsilon^2, & \text{if } (l, k) \notin \mathcal{B}_{F,\tau}, \\ \gg \epsilon^2, & \text{if } (l, k) \in \mathcal{B}_{F,\tau}, \end{cases}$$

where $\epsilon > 0$ is a small enough value. Note that, if $|\mu_k^{(l)} - \hat{\mu}_k^{(l)}| = |\sigma_k^{(l)2} - \hat{\sigma}_k^{(l)2}| = 0$, the pre-activation follows a Gaussian distribution $\mathcal{N}(\mu_k^{(l)}, \sigma_k^{(l)2})$.

4.2 Discrepancy of differential entropy (DDE)

If the pre-activation distributions are standardized (subtracting the mean and dividing the standard deviation), the differential entropy will be maximized on the benign neuron approximately following a standard Gaussian distribution $\mathcal{N}(0, 1)$. In backdoor neurons, because of the difference of the moments on Gaussian components, the resulting mixture distributions can not be Gaussian distributions, hence the differential entropy must be smaller than $h(Z)$, where $Z \sim \mathcal{N}(0, 1)$ is the standardized Gaussian distribution. Specifically, let $\dot{\phi}_k^{(l)} = \frac{\phi_k^{(l)} - \mu_k^{(l)}}{\sigma_k^{(l)}}$ be the standardized pre-activations, then

$$h(\dot{\phi}_k^{(l)}) < h(\dot{\phi}_{k'}^{(l)}) \leq h(Z), \quad \forall k \in \mathcal{B}_{F,\tau}, k' \notin \mathcal{B}_{F,\tau}.$$

This inequality gives a guarantee that with an appropriately chosen threshold, the backdoor neurons can be well separated with the benign neurons.

4.3 Mismatched BN statistics (MBNS)

BN layer involves using the statistics of a mini-batch to normalize the data in each layer for each neuron. It is known to be able to smooth the optimization landscape, and has gradually become a

default setting of neural networks [19]. When inference, BN uses the fixed statistics obtained by averaging the sample statistics of mini-batches during training time, including the mean and the variance. If the model is trained on a poisoned dataset, BN will record the mean and the variance of the poison-benign mixed data. Note that the mean and variance here are not defined on the pre-activations $\phi_k^{(l)}$, but on $x_k^{(l)}$. Based on the above discussions, we know that the poisoned samples (especially the pre-activations) on the backdoor neurons follow a different distribution from the benign samples. The recorded statistics during training are actually that of the mixture distribution. Hence, we can expect that the BN statistics of a trained backdoor neural network are biased. If we are able to access a small set of benign data, we can calculate an approximation of the true statistics on benign data. Then we calculate the *Kullback-Leibler* (KL) divergence [9] between the sample distribution and the BN induced distribution as the measurement of the bias. By assuming both of the distributions follow Gaussian distributions, we have a closed form solution:

$$\mathrm{D}_{\mathrm{KL}}(\mathcal{N}_{\mathrm{sample}}^{(l)}, \mathcal{N}_{\mathrm{BN}}^{(l)})_k = \log \frac{\tilde{\sigma}_k^{(l)}}{\bar{\sigma}_k^{(l)}} + \frac{\bar{\sigma}_k^{(l)2} + (\bar{\mu}_k^{(l)} - \tilde{\mu}_k^{(l)})^2}{2\tilde{\sigma}_k^{(l)2}} - \frac{1}{2},$$

where $\bar{\mu}_k^{(l)}$ and $\bar{\sigma}_k^{(l)2}$ are the statistics obtained from benign samples, $\tilde{\mu}_k^{(l)2}$ and $\tilde{\sigma}_k^{(l)}$ are the BN statistics. The backdoor neurons should have abnormally large KL divergences, as illustrated in Figure 2(c).

4.4 Overview of the two pruning strategies

In Section 3.4, we reveal the discrepancy between the pre-activation distributions in the backdoor neurons and that in the benign neurons. This enables fast detecting the neurons that are more related to the backdoor behaviours. The index we choose to detect the abnormal neurons depends on what kind of data we are able to access.

Mixture training data In this case, the victim is given a poisoned training dataset with a specified poisoning rate ρ. Our goal is to obtain a benign model based on the poisoned dataset. To achieve this, we first train an infected model F on the poisoned dataset. The resulting model should have a certain number of backdoor neurons based on empirical observation and the assumption. Since $\rho > 0$ for the dataset, all the neurons follow Gaussian mixture distributions, and we have $h(\dot{\boldsymbol{x}}_k^{(l)}) < h(\dot{\boldsymbol{x}}_{k'}^{(l)})$ for all $k \in \mathcal{B}_{F,\tau}, k' \notin \mathcal{B}_{F,\tau}$. This implies that with an appropriate threshold τ_h^*, we can perfectly separate the benign neurons and backdoor neurons, which can be formulated as:

$$\exists \tau_h^*, \quad h(\dot{\boldsymbol{x}}_k^{(l)}) < \tau_h^*, \quad \forall k \in \mathcal{B}_{F,\tau},$$
$$h(\dot{\boldsymbol{x}}_{k'}^{(l)}) > \tau_h^*, \quad \forall k' \notin \mathcal{B}_{F,\tau}.$$

Setting the threshold τ_h^* is crucial to the solution, and it is a trade-off between the accuracy on benign samples and that on the backdoored samples. Note that $|\mathcal{B}_{F,\tau}^{(l)}| << d_c^{(l)}$. We can treat the low entropy neurons as outliers in each layer, and set different thresholds for different layers. Specifically, let $h^{(l)} = [h(x_1^{(l)}), h(x_2^{(l)}), \ldots, h(x_{d_c^{(l)}}^{(l)})]^T \in \mathbb{R}^{d_c^{(l)}}$ be a vector of sample entropy of the l-th layer calculated from the poisoned dataset. Then we set $\tau_h^{(l)} = \bar{h}^{(l)} - u_h \cdot s_h^{(l)}$, where $\bar{h}^{(l)} = \frac{1}{d_c^{(l)}} \sum_{k=1}^{d_c^{(l)}} h_k^{(l)}$ and $s_h^{(l)} = \sqrt{\frac{1}{d_c^{(l)}} \sum_{k=1}^{d_c^{(l)}} (h_k^{(l)} - \bar{h}^{(l)})^2}$ are the mean and standard deviation of $h^{(l)}$, u_h is a hyperparameter controlling how low the threshold is. Then we have a set of indices of potential backdoor neurons $\mathcal{I}_h = \{(l, k) : h_k^{(l)} < \tau_h^{(l)}\}$. Finally, we prune the infected model F using $\mathcal{I}_h$, which result in a final model $F_{-\mathcal{I}_h}$.

Benign training data This is the case that the victim is given a trained poisoned model F with a small set of benign data. Our goal is to utilize the benign data to clean up the poisoned model and eliminate the backdoor threat. Similar to the pruning process based on differential entropy, we first construct a vector of KL divergences of all neurons for each layer $K^{(l)} = [K_1^{(l)}, K_2^{(l)}, \ldots, K_{d_c^{(l)}}^{(l)}]^T \in \mathbb{R}^{d_c^{(l)}}$ according to equation (5). We set $\tau_K^{(l)} = \bar{K}^{(l)} - u_K \cdot s_K^{(l)}$, where $\bar{K}^{(l)} = \frac{1}{d_c^{(l)}} \sum_{k=1}^{d_c^{(l)}} K_k^{(l)}$ and $s_K^{(l)} = \sqrt{\frac{1}{d_c^{(l)}} \sum_{k=1}^{d_c^{(l)}} (K_k^{(l)} - \bar{K}^{(l)})^2}$ are the mean and standard deviation of $K^{(l)}$, u_K is a

229 hyperparameter. The set of selected neurons is $\mathcal{I}_K = \{(l,k) : K_k^{(l)} < \tau_K^{(l)}\}$ and the pruned model
230 can be represented as $F_{-\mathcal{I}_K}$. Note that u_K is the **only** hyperparameter of our methods, and is usually
231 set to 3.

5 Experiments

5.1 Implementation details

Datasets   In this section, the experiments are conducted on two influential benchmarks, CIFAR-10
[22] and Tiny-ImageNet [23]. We use 90% of the data set for training, the rest of the data is used for
validating or recovering the poisoned model.

Models   We use ResNet-18 [16] as the baseline model to evaluate our proposed method, and
compare it with other methods. We train the network for 150 epochs on CIFAR-10 and 100 epochs
on Tiny-ImageNet with SGD optimizer. The initial learning rate is set to 0.1 and the momentum is
set to 0.9. We adopt the cosine learning rate scheduler to adjust the learning rate. The batch size
is set to 128 by default. We set the threshold hyperparameter u_h/u_k to 3 on CIFAR-10 and 4 on
Tiny-ImageNet by default.

Attacks   Our experiments are based on both the classical and the most advanced attack strategies,
including the *BadNet* [14], *Clean Label Attack* (CLA) [40], *Reflection Backdoor* (Refool) [31],
Warping-based poisoned Networks [34], *Blended backdoor attack* (Blended) [5], *Input-aware back-
door attack* (IAB) [33] and *Sample Specific Backdoor Attack* (SSBA) [27]. For BadNets, we test
both the *All-to-All* (A2A) attack and *All-to-One* (A2O) attack, *i.e.*, the attack target labels are set to
$y_t = (y+1) \bmod C$, or one particular label $y_t = C_t$, respectively. The target for A2O attacks of all
the attack strategies is set to class 0. The triggers for BadNets and CLA are set to randomly generated
patterns with size 3×3 for CIFAR-10 and 5×5 for Tiny-ImageNet. The poisoning rate is set to 10%
by default. Note that, due to the image size restraint, SSBA is only performed on Tiny-Imagenet.

Defenses   We conduct experiments under two defense settings, one of which allows the defender to
access the poisoned training set, while the other only has a small clean data set. Both the defense
goals are to obtain a clean model without backdoor behaviours. We compare our approaches with the
l_∞ *pruning* [6], *fine-tuning* (FT), *fine-pruning* (FP) [28] and *neural attentional distillation* (NAD)
[24]. The number of benign samples allowed to access is set to 500 (1%) for CIFAR-10 and 5000
(5%) for Tiny-ImageNet by default.

Evaluation metrics   In this work, we use the *attack clean accuracy* (ACC) and *attack success rate*
(ASR) to evaluate the effectiveness of different methods. The ACC for a given model F is defined as:

$$\mathrm{ACC}(F, \mathcal{D}_{\text{test}}) = \sum_{(\boldsymbol{x},y) \in \mathcal{D}_{\text{test}}} \mathbb{I}\{\arg\max(F(\boldsymbol{x})) = y\},$$

where $\mathbb{I}$ is the *indicator function*. The ASR is defined as:

$$\mathrm{ASR}(F, \mathcal{D}_{\text{test}}) = \sum_{(\boldsymbol{x},y) \in \mathcal{D}_{\text{test}}, y \neq y_t} \mathbb{I}\{\arg\max(F(\delta(\boldsymbol{x}))) = y_t\},$$

where y_t is the attack target label. The ACC measures the model performance on benign samples,
while the ASR reflects the degree of backdoor behavior retainment in the model. Given an infected
model, our goal is to reduce the ASR, while keeping the ACC from dropping too much.

5.2 Experimental results

CIFAR-10   We show the results on CIFAR-10 in Table 1. The recently proposed NAD and ANP
performs significantly better than other defense methods, reducing the ASR to a very low level with a
slight drop on ACC. However, they also have a significant drop ($3 \sim 4\%$) on ACC when defending
CLA, which is the most robust backdoor attack in our experiments, and ANP even failed when
defending BadNets(A2A). Nevertheless, both of our methods successfully eliminate the backdoor
(ASR $< 1\%$) with negligible loss on ACC. We even observe a little rise on ACC when defending

Table 1: Experimental results of the proposed approaches against different attacks compared with other defense methods in CIFAR-10[22].

Attacks	BadNets (A2O)		BadNets (A2A)		CLA		WaNet		Blended		Refool		IAB	
	ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR
Origin	93.86	100.00	94.60	93.89	94.99	98.83	94.11	99.67	94.17	99.62	94.24	98.40	93.87	97.91
FT	92.22	2.16	92.03	60.76	92.88	95.73	92.93	9.37	93.9	90.27	91.68	17.78	91.78	9.52
FP	92.18	2.97	91.75	66.82	92.60	99.36	92.07	1.03	70.92	90.92	92.36	75.98	87.04	16.13
l_∞	92.12	100.00	93.67	6.67	92.75	98.76	93.48	99.74	86.99	99.77	91.19	98.47	88.37	88.48
NAD	93.36	2.43	92.18	2.06	91.36	15.31	93.08	3.05	92.72	1.61	91.64	6.74	92.11	19.45
ANP	93.47	3.53	90.29	86.22	91.13	11.76	**94.12**	**0.51**	93.66	5.03	91.71	26.96	**93.52**	10.61
DDE (Ours)	**93.88**	**0.86**	**94.49**	**0.61**	**94.42**	**0.91**	93.79	2.80	93.67	**2.24**	93.35	8.90	93.17	0.94
MBNS (Ours)	93.60	1.60	94.25	0.72	94.14	7.03	94.05	3.39	**94.17**	2.71	**93.69**	**6.48**	93.15	**0.64**

Table 2: Experimental results of the proposed approaches against different attacks compared with other defense methods in Tiny-ImageNet[23].

Attacks	BadNets (A2O)		CLA		WaNet		Refool		Blended		IAB		SSBA	
	ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR
Origin	61.36	97.38	65.61	56.58	61.47	99.98	53.26	80.61	62.85	99.83	61.4	98.28	66.51	99.78
FT	46.93	99.84	61.19	63.20	54.28	99.96	47.09	91.77	56.83	29.12	52.39	99.1	52.39	33.19
FP	35.41	99.48	62.30	39.05	53.65	100.00	42.10	86.62	59.59	99.76	52.67	98.47	53.36	31.96
l_∞	53.13	90.39	59.15	23.12	42.01	99.84	46.84	81.19	56.33	99.85	54.81	86.97	49.35	99.98
NAD	44.20	90.13	62.80	17.35	53.40	99.98	51.06	70.63	57.35	55.6	53.32	98.85	52.52	25.08
ANP	53.85	4.02	59.69	3.64	54.82	86.98	50.67	**0.21**	**62.49**	0.61	61.39	4.67	60.98	1.01
DDE (Ours)	60.68	**0.86**	64.47	0.1	60.53	0.02	51.29	17.07	60.67	**0.69**	61.26	**0.60**	64.2	0.11
MBNS (Ours)	**61.60**	1.60	**64.86**	**0.05**	**61.58**	**0.01**	**52.41**	23.79	60.77	0.85	**61.30**	**0.60**	**64.64**	**0.01**

BadNets by DDE. This phenomenon demonstrates that backdoor neurons may hurt the ACC in some way, and thus the ACC will rise when the backdoor neurons are precisely pruned. Overall, our methods achieve the most advanced defense results.

Tiny-ImageNet Tiny-ImageNet is a larger scale dataset with higher resolution images, and it is harder to defend against the attacks performed on it. Note that the A2A attack is absent, since we cannot successfully perform the attack due to the large number of its classes (up to 200). Our experimental results show that all of the defense methods suffer from the performance degradation compared with the results in CIFAR-10, and they fail to defend against WaNet with a large ACC drop but even unchanged ASR, especially the ANP and l_∞ defense. This phenomenon shows that the principles for finding backdoor neurons of both ANP and l_∞ don't work in such case. Nevertheless, our methods totally remove the backdoor and the ACC are not even affected, which indicates that our methods can precisely locate the backdoor neurons even on such large scale dataset.

5.3 Ablation study

To be fair, we compare MBNS with other re-training based methods using 500 benign samples in Section 5.2. However, MBNS doesn't require re-training the model, since the samples are just used for detecting the distribution discrepancy. Therefore, the required samples can be much less than 500. We now discuss the limit of MBNS and study how the number of samples affects the effectiveness of MBNS. We train BadNets, CLA, Refool and Blended on CIFAR-10 with $\rho = 10\%$, and use 10 to 500 benign samples to recover the model using MBNS. We record the changes of ACC and ASR with respect to the number of benign samples. The results are shown in Section 5.3. The influence of number of samples to our methods comes from the randomness on estimating moments. As the number of samples grows, the randomness is reduced and MBNS has more stable performance, but the average performances are not improved, except for Refool. Compared with other attacks, Refool clearly needs more samples to reduce the ASR. The reason may be that the mixture distribution in Refool has closer moments and is harder to distinguish. Besides, we surprisingly find that MBNS can recover BadNets, CLA and Blended using only 10 benign samples. The additional results on DDE are shown in Section 7.

We also conduct experiments to show the high correlation between the backdoor neurons and our proposed evaluation metrics, the results are shown in Section 7

Figure 3: This figure shows the influence of samples used for MBNS.

Figure 4: This figure shows the performance of our proposed DDE and MBNS with different hyperparameter against badnet on CIFAR-10 with ResNet-18.

6 Discussion

The proposed methods are superior to other existing defense methods in the following three aspects:

Better performance   As demonstrated in Section 5, both of the proposed methods achieve state-of-the-art results. Moreover, according to the ablation study, the proposed MBNS can successfully defend most of the attacks within 10 benign samples, which shows the amazing effectiveness of our proposed methods.

Higher efficiency   The proposed methods are also highly efficient. We record the running time of several defense methods on 500 CIFAR-10 images with ResNet-18, and show the results in Table 3. It can be seen that both of the proposed methods require less time than the baseline defense methods. Since both methods require scanning on each neuron once, the computational complexity scale linearly with the number of the neurons in the neural network. Therefore, the efficiency of our methods is promised.

Table 3: The overall running time of different defense methods on 500 CIFAR-10 images with ResNet-18.

Defense Method	FT	FP	NAD	ANP	DDE (ours)	MBNS (ours)
Runing Time (sec.)	12.35s	$14.59s$	$22.08s$	$25.68s$	$10.69s$	**0.39s**

More robust to hyperparameter choosing   One of the most general problems in backdoor defense is the choice of hyperparameters. Under realistic settings, the defenders can only perform defenses without any prior knowledge about poison data, including poisoning rate and examples of poisoned data. So the defenders should carefully tune the hyperparameters, or the ACC and ASR can change suddenly even under small fluctuations of those hyperparameters. In comparison, both of the proposed pruning strategies only require one universal hyperparameter u. Moreover, they show reliable consistency against different attacks in the same dataset, only vary from different datasets, which is inevitable. Besides, we leave a wide range of parameters to choose, so that the ACC remains high while the ASR is controlled to a very small number, as shown in Section 5.3.

7 Conclusion

In this work, we take a deep inspection on the pre-activation distributions of each layer, and study their characteristics in a poisoned model. We find that the distributions of benign data and poisoned data on these neurons are both Gaussian but extraordinarily different in their moments. The mixture distributions have low entropy compared with that of the benign neurons. This property makes it possible for the defender to efficiently detect the abnormal neurons based on the sample entropy, when the poisoned dataset can be accessed. Moreover, when the defender has only a small set of benign data, we propose to detect the abnormal neurons based on the inconsistency of the BN statistics on poisoned dataset and the sample statistics on the given benign dataset. We then do pruning on these potential backdoor neurons using the proposed two detection methods to recover the model. The

experiments show that the proposed defending strategies can efficiently locate the backdoor neurons, and greatly reduce the backdoor threat with negligible loss on clean accuracy. Our approach based on the pre-activation distributions achieves superior results compared with all other defense methods under various attacks on both datasets, empirically showing that the distribution property may be both dataset-invariant and attack-invariant. The results shed lights on the field of backdoor defense, and can be a guidance for designing more robust backdoor attacks.

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A   Implementation Details of Performed Backdoor Attacks and Defenses

In this part, we provide more detailed information about the state-of-art attacks and defenses applied in our work. The examples of poisoned images are shown in Appendix A.

(a) Original image   (b) BadNets   (c) Blended

(d) Refool   (e) CLA   (f) IAB

Figure 5: Examples of the poisoned data on CIFAR-10.

(a) Original image   (b) SSBA

Figure 6: Examples of the poisoned data on Tiny-ImageNet

The hyperparameter we used in our DDE and MBNS is 3 in CIFAR-10 and 4 in Tiny-ImageNet. The parameters in other defenses is set as default.

B   Additional Experimental Results of Different Poisoning Rate

Poisoning rate is considered important in the proposed methods, since smaller poisoning rate will make the mixture distributions less distinguishable from unimodal distributions. In DDE, decreasing poisoning rate will increase the entropy of the backdoor neurons, and it will be harder to precisely

detect them. In MBNS, the smaller poisoning rate makes the BN statistics closer to the true benign statistics. Hence, it is important to study the influence of poisoning rate on the performance of the proposed methods. We set the poisoning rate to 1%, 5% and 10% for all attacks and show the results in Table 4. Note that CLA fails to attack the model when the poisoning rate is set to 1%. In most cases, their performances retain a high level. Nevertheless, there are severe degradation against CLA and Refool. Specifically, the ASR of CLA and Refool remain over 10% after pruning using DDE and MBNS. However, we use default hyperparameter, i.e., $u_h = 3$ and $u_K = 3$ here. By further decreasing the pruning threshold, we can reduce both ASR to less than 5%. Overall, MBNS is more robust against attacks of small poisoning rate.

Table 4: Experimental results of the proposed approaches against different attacks compared with other defense methods in CIFAR-10[22].

ρ	Stage	BadNets (A2O)		BadNets (A2A)		CLA		WaNet		Blended		Refool		IAB	
		ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR
1%	Origin	95.03	99.94	94.75	88.57	88.96	4.73	94.76	46.82	94.17	99.62	93.08	99.59	93.22	64.00
	DDE	94.82	0.91	94.17	0.73	87.96	0.65	93.67	14.17	94.46	2.29	91.77	24.08	92.73	5.21
	MBNS	92.22	2.16	93.16	7.99	88.03	0.84	94.64	1.24	92.89	2.44	90.99	21.22	93.17	4.19
5%	Origin	94.29	99.99	94.26	92.78	95.53	92.23	94.00	94.55	94.53	81.33	94.35	97.98	92.70	65.50
	DDE	93.83	0.83	93.67	0.70	94.43	15.91	92.73	10.13	94.44	5.49	92.75	4.51	92.29	1.83
	MBNS	93.61	0.67	93.99	5.64	94.65	12.06	94.17	1.78	93.37	9.21	92.30	2.08	92.74	2.14
10%	Origin	93.89	100.00	94.60	93.89	94.99	98.83	94.11	99.67	94.17	99.63	94.24	98.40	93.87	97.91
	DDE	93.88	0.86	94.49	0.61	94.42	0.91	93.79	2.80	93.67	2.24	93.35	8.90	93.17	0.94
	MBNS	93.60	1.60	94.25	0.72	94.14	7.03	94.05	3.39	94.17	2.71	93.69	6.48	93.15	0.64

C Additional Experimental Results on Wide-ResNet

To study the generalization of the proposed defense methods over different architectures, we conduct experiments on WideResNet-28-1, which is also a commonly used model in backdoor community. The results are shown in Appendix C.

Attacks	Backdoored		DDE		MBNS	
	ACC	ASR	ACC	ASR	ACC	ASR
BadNets (A2O)	91.62	99.99	90.30	1.71	91.37	1.61
BadNets (A2A)	92.53	92.03	91.50	0.90	91.43	1.56
CLA	92.81	80.14	91.55	10.24	91.91	4.30
Refool	91.53	97.28	91.11	0.74	90.29	2.87
WaNet	91.78	91.92	92.28	0.67	91.84	0.56
Blended	91.65	99.78	91.59	6.40	91.59	1.52
IAB	90.32	88.08	90.97	1.87	90.74	1.86

D Analysis of Correlation Between Backdoor Neurons and Pruned Neurons

In section Section 3.3, we have demonstrated the definition of sensitivity of neurons to backdoor in Equation (2), which is the difference of backdoor loss before and after being pruned. It is important to ensure that our methods precisely detect those backdoor neurons with high sensitivity. Here, we make scatter plots of the backdoor sensitivity of the neurons and their differential entropy and KL divergence in some typical layers. The detailed scatter figures are shown in Figure 7. The results indicate that both DDE and MBNS choose the neurons with high sensitivity. Especially for BadNets, the highest sensitivity of one single neuron is extremely large and its differential entropy and KL divergence stay away from average. The overall results demonstrate a strong correlation between the neuron sensitivity to backdoor and the proposed indices.

E Performance on Low-quality Data

Our methods require extra data and rely on its distribution to detoxify the backdoor model, so it's natural to consider a worse case that we can only get low-quality dataset with some distortion in it. To further show the effectiveness of our proposed methods, we utilize multiple data augmentation tricks

| (a) BadNets (DDE) | (b) BadNets (MBNS) | (c) Blended (DDE) | (d) Blended (MBNS) |
| (e) WaNet (DDE) | (f) WaNet (MBNS) | (g) Refool (DDE) | (h) Refool (MBNS) |

Figure 7: Scatter plots of backdoor sensitivity of mid-layer neurons to backdoor and the corresponding differential entropy and KL divergence indices.

| (a) Original image | (b) CJ | (c) SAP | (d) PW | (e) Snow |

Figure 8: Examples of the perturbed data.

to create out-of-distribution data on CIFAR-10 while performing defenses against BadNets (A2O) attack, including color jitter with 90 degree rotation (CJ) from torchvision, CoarseSaltandPepper (SAP), PolarWarping (PW), Snowflakes (Snow) from [20]. To be specific, the parameters of CJ are set to be [0.5, 0.5, 0.5, 0.5]; 30% of the pixels in SAP are replaced replaced by salt/pepper noise mask which has 1% to 10% the size of the input image; the translate percent in PW is set to be ± 0.2; the snow size of Snow is (0.2, 0.5) and its speed is (0.01, 0.05). Samples of those perturbed images are shown in Appendix E. Now we replace 10% of the DDE and MBNS used data into those perturbed out-of-distribution data, and see the performance of our methods. The experimental results are shown in Table 5, which illustrates that even if some low-quality data are mixed into the data they use, our methods can still successfully locate the backdoor neurons and delete them while maintaining high clean accuracy.

Table 5: Experimental Results of the proposed methods using low-quality datasets.

Attacks	Origin		CJ		SAP		PW		Snow	
	ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR
DDE	93.88	0.86	93.62	0.88	93.19	0.86	93.65	0.82	93.23	0.93
MBNS	93.60	1.60	93.56	1.52	91.17	1.58	92.62	0.96	90.99	0.95

F Exploration of Potential Adaptive Attacks

In this section, we explore some potential adaptive attacks against the proposed methods.

F.1 BN Re-parameterization against MBNS

The MBNS pruning strategy rely on the correct information from the BN statistics. However, this information can be changed by a defense-aware attacker using re-parameterization techniques.

Specifically, consider a BN operation performed on each neuron by:

$$\tilde{\mathrm{BN}}^{(l)}(\boldsymbol{x}_k^{(l)})_{\tilde{\gamma}_k^{(l)},\tilde{\beta}_k^{(l)}} = \tilde{\gamma}_k^{(l)} \frac{\boldsymbol{x}_k^{(l)} - \tilde{\mu}_k^{(l)}}{\tilde{\sigma}_k^{(l)}} + \tilde{\beta}_k^{(l)}$$

$$= \frac{\tilde{\gamma}_k^{(l)}}{\tilde{\sigma}_k^{(l)}} \boldsymbol{x}_k^{(l)} + (\tilde{\beta}_k^{(l)} - \frac{\tilde{\mu}_k^{(l)}}{\tilde{\sigma}_k^{(l)}}).$$

The attacker can calculate the sample statistics denoting $\mu_k^{(l)}$ and $\sigma_k^{(l)}$ from benign data, and assign new weights and bias by:

$$\gamma_k^{(l)} = \frac{\sigma_k^{(l)}}{\tilde{\sigma}_k^{(l)}} \tilde{\gamma}_k^{(l)}$$

$$\beta_k^{(l)} = \tilde{\beta}_k^{(l)} - \frac{\tilde{\mu}_k^{(l)}}{\tilde{\sigma}_k^{(l)}} + \frac{\mu_k^{(l)}}{\sigma_k^{(l)}}$$

In this way, the whole linear transformation remains unchanged, but the BN statistics become consistent with that of the benign data, which makes the backdoor neurons unable to be detected by the proposed MBNS.

| Attacks | $\lambda = 1$ | | $\lambda = 0.1$ | | $\lambda = 0.01$ | | $\lambda = 0.001$ | |
	ACC	ASR	ACC	ASR	ACC	ASR	ACC	ASR
Origin	NaN	NaN	NaN	NaN	95.11	100.00	93.41	75.30
DDE	—	—	—	—	93.63	9.23	93.35	0.63
MBNS	—	—	—	—	94.15	0.32	93.82	0.24

Table 6: Experimental results on regularization-based adaptive attack.

F.2 Regularization-based Adaptive Attacks

Both of the two methods rely on the discrepancy of the benign distribution and poisoned distribution. Hence, we wonder whether DDE and MBNS still work if the attacker try to regularize the distribution to minimize the discrepancy. Hence, we use BadNets as an example to perform the adaptive attack with an additional objective:

$$\mathcal{L}_{adaptive} = \mathbb{E}_{(\boldsymbol{x},y)\sim\mathcal{D}}[\mathrm{D}_{\mathrm{CE}}(y, f(\delta(\boldsymbol{x})))] + \lambda \sum_{1 \le k \le K} \sum_{1 \le l \le L} \mathbb{E}_{\boldsymbol{x}\sim\mathcal{X}}[(\phi_k^{(l)} - \hat{\phi}_k^{(l)})^2], \qquad (5)$$

where $\phi_k^{(l)}$ and $\hat{\phi}_k^{(l)}$ denote the pre-activations of benign and poisoned samples in the kth neuron of the lth layer. The goal of the second term is to minimize the discrepancy between the benign distribution and the poisoned distribution with a trade-off hyperparameter λ. We select λ from [1.000, 0.100, 0.010, 0.001] and train four models and do pruning using DDE and MBNS, the results are shown in Table 6. We find that too large λ makes the objective not trainable, hence collapse the training process. This may because it is not realistic to distinguish benign and poisoned samples while making their distribution indistinguishable. After down weighting λ, the model is able to be trained normally. However, we find DDE and MBNS are still able to remove the backdoor without influence too much on the clean accuracy.

A recently proposed method[43] also regularizes the distribution discrepancy between benign samples and poisoned samples by maximum mean discrepancy (MMD), which is a direct attack against our defense. We test our method on it and find it still works. Specifically, the original ACC and ASR are 87.51%, 98.48%, respectively. The ACC and ASR after pruning by DDE is 86.34%, 3.26% and ACC and ASR for MBNS is 86.93%, 6.15%, respectively.

G   Additional Experimental Results for the Choice of Hyperparameter

In this section, we provide ablation study on the choice of the threshold hyperparameter u_h/u_k. As shown in Figure 9, both DDE and MBNS gives promising defending results against most tested attacks on CIFAR 10 when u_h/u_k is around 3. Besides, the robustness of the hyperparameter is supported by the wide choice of available u_h/u_k that lead to acceptable results.

Figure 9: The performance of proposed DDE and MBNS with different hyperparameter u_h/u_k against all the tested attacks on ResNet-18.