DSEE: Dually Sparsity-embedded Efficient Tuning of Pre-trained Language Models

Abstract

Gigantic pre-trained models have become central to natural language processing (NLP), serving as the starting point for fine-tuning towards a range of downstream tasks. However, two pain points persist for this paradigm: (a) as the pre-trained models grow bigger (e.g., 175B parameters for GPT-3), even the fine-tuning process can be time-consuming and computationally expensive; (b) the fine-tuned model has the same size as its starting point by default, which is neither sensible due to its more specialized functionality, nor practical since many fine-tuned models will be deployed in resource-constrained environments. To address these pain points, we propose a framework for resource- and parameter-efficient fine-tuning by leveraging the sparsity prior in both weight updates and the final model weights. Our proposed framework, dubbed **D**ually **S**parsity-**E**mbedded **E**fficient Tuning (DSEE), aims to achieve two key objectives: (i) *parameter efficient fine-tuning* - by enforcing sparsity-aware weight updates on top of the pre-trained weights; and (ii) *resource-efficient inference* - by encouraging a sparse weight structure towards the final fine-tuned model. We leverage sparsity in these two directions by exploiting both unstructured and structural sparse patterns in pre-trained language models via magnitude-based pruning and ℓ_1 sparse regularization. Extensive experiments and in-depth investigations, with diverse network backbones (i.e., BERT, GPT-2, and DeBERTa) on dozens of datasets, consistently demonstrate highly impressive parameter-/training-/inference-efficiency, while maintaining competitive downstream transfer performance. For instance, our DSEE-BERT obtains about 35% inference FLOPs savings with $< 0.1\%$ trainable parameters and comparable performance to conventional fine-tuning. [1]

1 Introduction

Most recent NLP applications have been folllowing the pre-train then fine-tune paradigm, where we start from a gigantic pre-trained model and fine-tune it towards downstream tasks. Conventional *fine-tuning* works by updating all of the parameters of the pre-trained model. As the size of pre-trained models grows, updating all parameters becomes less feasible in most practical scenarios, due to the expensive memory and computational requirements. For example, $\text{BERT}_{\text{base}}$ has 110M trainable parameters, while GPT-2 has up to 1.5B and the largest version of GPT-3 has an astonishing 175B trainable parameters. As such, conventional fine-tuning of the larger models could require hundreds of GPU hours. Another downside of this paradigm is that it requires storing as many parameters, as in the large-scale pre-trained models, for each downstream task. That poses impediments to the deployment on real-world resource-constrained environments.

One solution to address the extensive resource requirement of conventional fine-tuning is model pruning (LeCun et al., 1990; Han et al., 2015a; Ren et al., 2018; He et al., 2017; Liu et al., 2017), where unnecessary weights are eliminated to shrink the model size. For example, Chen et al. (2021) leverages ℓ_1 regularization to remove insignificant attention heads and gains $35\% \sim 45\%$ training time with comparable performance. Guo et al. (2020) learns sparse task-specific "diff" vectors for various downstream fine-tuning tasks, leading to great memory savings. All these studies indicate the rise of sparsity naturally during fine-tuning a general-purpose pre-trained model, to some specialized downstream functionality. One potential interpretation, of why sparsity arises, is that different

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[1] All codes are provided in the supplement.

subsets of the parameters may be responsible for different downstream tasks and data domains (Sanh et al., 2020). However, identifying appropriate sparse pruning masks requires burdensome training of models with full weights, which can still be unaffordable for many practitioners. For example, fine-tuning a large pre-trained language model like GPT-3 for just one step consumes at least a 1.2TB of VRAM and requires 96 pieces of NVIDIA Tesla (Hu et al., 2021).

One parallel alternative is designing *parameter-efficient* fine-tuning algorithms, which aims to only optimize a small portion of weights while fixing most of the pre-trained weights during the down-stream task training step. Pioneering works along this line, which utilize adapters (Houlsby et al., 2019) or low-rank decomposition (Hu et al., 2021), can significantly reduce the number of trainable parameters while preserving good fine-tuning performance. Introducing only a small number of task-specific parameters for each new downstream task can substantially improves the memory and deployment efficiency of models as it allows us to reuse the remaining unchanged/shared parameters. However, there are two major hurdle of current parameter-efficient fine-tuning: (i) it does not yield any inference efficiency gains since the full pre-trained weights are still required to calculate outputs; and (ii) current methods assume the weight update to be either sparse (Guo et al., 2020) or low-rank (Hu et al., 2021), yet those assumptions might be oversimplified and overly restricted to allow for effective updates.

To tackle both resource- and parameter-efficiency issues of large model fine-tuning, we explicitly draw on the prior of sparsity for *both weight updates and the final weights*, and establish a *dually sparsity-embedding efficient tuning* (**DSEE**) framework. From a pre-trained model, DSEE first adopts a sparsity-aware low-rank weight update to achieve *parameter efficiency* of the fine-tuning process; and then enforces a sparse weight structure by masking to achieve *resource efficiency* of the fine-tuned model at inference time. Our contributions can be summarized as follows:

- We propose the dually sparsity-embeddeding efficient tuning (DSEE), which unifies sparsity-aware weight update and sparse final weight in fine-tuning gigantic pre-trained models. It is the first attempt towards jointly optimizing both parameter efficiency of the fine-tuning process, and the resource efficiency of the fine-tuned model.

- We exploit both unstructured and structural sparse patterns in the DSEE framework. For weight updates, we find the injected sparsity prior to greatly enhance existing parameter-efficient update schemes, and to further trim down the needed amount of trainable parameters. For the final weights, we learn well-performed sparse masks from the pre-trained weights, leading to substantial computation and memory reductions at inference.

- Extensive experiments demonstrate the effectiveness of our proposal across various representative pre-trained languages models, such as BERT, GPT-2, and DeBERTa; and on diverse evaluation benchmarks, such as E2E, DART, WebNLG, and GLUE. Specifically, on (E2E, Dart, WebNLG), our methods can achieve a BLUE score of $(69.75, 55.40, 46.66)$ with less than 0.1% of total trainable-parameters. On BERT, our method can save about 35% FLOPs, compared to traditional downstream fine-tuning.

2 RELATED WORK

Pre-trained language models. Transformer (Vaswani et al., 2017) is a sequence-to-sequence model that heavily uses the concept of self-attention. Later on, numerous transformer-based models have been proposed and show overwhelming performance on natural language processing (NLP) and on computer vision (CV) tasks. Devlin et al. (2019) designed BERT that pre-train deep bidirectional representations from unlabeled text and reached powerful performance. Liu et al. (2019) found that BERT were terribly undertrained and proposed RoBERTa, an enhanced training recipe for BERT which can greatly boost the performance. He et al. (2020) proposed decoding-enhanced BERT with disentangled attention (DeBERTa) that incorporates the disentangled attention mechanism and an improved mask encoder to enhance BERT and RoBERTa. More variants like XL-Net, Albert, and Electra have also been proposed in recent years (Yang et al., 2019; Lan et al., 2019; Clark et al., 2019). The series of GPT models (Radford et al., 2019; Brown et al., 2020) are later developed based on transformers decoder blocks rather than encoder blocks like BERT, which again have shown superior performance on different tasks. These large models pretrained on a large amount of unlabelled texts would need to be further fine-tuned on downstream tasks for better performance. One of the accompanying disadvantages of these pre-training models with tremendous parameter counts (e.g., 175B in GPT-3) is the unaffordable computational cost for further fine-tuning.

Pruning and Low-rank decomposition.   Pruning is a widely-used model compression technique. It can reduce the number of parameters inside models, which possibly brings training and inference efficiency. Along with weight pruning method (Han et al., 2015b) being one of the most effective methods (Gordon et al., 2020), various criterion have been proposed to select insignificant weights for pruning, such as Taylor approximation (Molchanov et al., 2019), Hessian score approximation (Hassibi & Stork, 1993), and other saliency scores such as SNIP (Lee et al., 2018), GraSP (Wang et al., 2019) and SynFlow (Tanaka et al., 2020). Several pruning methods have been commonly adapted to compress language models (McCarley et al., 2019; Gordon et al., 2020; Sanh et al., 2020; Wang et al., 2020; Chen et al., 2021). Specifically, McCarley et al. (2019) proposed to prune attention heads that had less contribution to the model. Wang et al. (2020) pruned BERT models by involving low-rank factorization and ℓ_0 regularization. Sanh et al. (2020) invented an improved version of magnitude pruning (*i.e.*, pruning based on the weight change) that can better suit the transfer learning. Chen et al. (2021) performed structural pruning on BERT via ℓ_1 sparse regularization, which reduced a large portion of parameters and decreased the training cost.

Low-rank approximation (Ye, 2005) is also vastly studied. One classical scenario is robust principle component analysis (Candès et al., 2011), which decomposes matrix into a low-rank plus a sparse component. Existing literature shows that in deep learning, the learned over-parameterized models often naturally bear approximate low-rank weight structures (Oymak et al., 2019; Yu et al., 2017). Some (Jaderberg et al., 2014; Povey et al., 2018; Sainath et al., 2013; Zhang et al., 2014; Zhao et al., 2016) have explicitly imposed the low-rank constraint during training. Wang et al. (2020); Hu et al. (2021) utilized low-rank decomposition to shrink model size and trim down the trainable parameters during fine-tuning. However to our best knowledge, integrating sparsity and low-rank structures has never been studied before for efficient fine-tuning of pre-trained language models.

Parameter-efficient adaptation.   Parameter-efficient adaptation aims at reducing the number of trainable parameters when fine-tuning the models across different downstream domains. Unlike pruning, it generates sparse update instead of building sparse models. Various approaches are invented to achieve the goal. Rebuffi et al. (2017); Houlsby et al. (2019) inserted and only trained adapters between existing layers, whose parameters is much less compared to the pretrained models. Guo et al. (2020) leveraged ℓ_0 regularization to limit the number of non-zero elements in the update vectors. Lester et al. (2021); Li & Liang (2021) introduced efficient prompt tuning which optimizes only a small continuous task-specific vector. Hu et al. (2021) proposed a low-rank decomposition-based method that can also significantly reduce the number of trainable parameters. However, fine-tuned models yielded by these methods work have the same amount of weights as the pre-trained starting point, hence they contribute no resource efficiency of the final model.

3 METHODOLOGY

In this section, we begin by describing our notations and definitions of sparsity generation and parameter-efficient fine-tuning in Section 3.1. Then, we introduce the (dually) sparsity-embedded efficient fine-tuning algorithms in Sections 3.2 and 3.3.

3.1 PRELIMINARIES

Sparsity generation and resource-efficient fine-tuning.   We adopt both unstructured and structural pruning methods to produce sparsity. When combined, they leads to resource-efficiency including memory and computation savings in both training and inference stages.

Let $\mathcal{W} \in \mathbb{R}^{m \times n}$ denote the pre-trained weight matrix. The goal of pruning is to locate a sparse binary mask $\mathcal{S} \in \{0, 1\}^{\|\mathcal{W}\|_0}$, where $\|\mathcal{W}\|_0$ is the number of weights in $\mathcal{W}$. The found mask $\mathcal{S}$ can be applied to the weights $\mathcal{W}$, and results in sparsified subnetworks with weight $\mathcal{W} \odot \mathcal{S}$. And the sparsity of the subnetwork is defined as $1 - \frac{\|\mathcal{S}\|_0}{\|\mathcal{W}\|_0}$. Note that for structurally pruned masks, we can indeed shrink the size of sparse weights by coalescing non-zero columns from the regular patterns.

Parameter-efficient fine-tuning.   To leverage the knowledge from pre-trained weights $\mathcal{W}$, downstream models learn task-specific weight update $\Delta \mathcal{W}$ via fine-tuning and output predictions with weights $\mathcal{W} + \Delta \mathcal{W}$, where $\Delta \mathcal{W}$ usually has the same size of $\mathcal{W}$, and hence requiring massive resources as the size of the pre-trained model increases. The target of parameter-efficient fine-tuning is to use as fewer trainable parameters as possible to calculate $\Delta \mathcal{W}$, while maintaining competitive downstream fine-tuning performance. Previous literature reaches the goal via either sparsifying

Figure 1: The overview of our proposals. The sparse masks can have unstructured or structural patterns, which leads to training and inference efficiency. During the fine-tuning, we only train decomposed matrices $\mathcal{U}$ and $\mathcal{V}$.

weight update matrices $\Delta \mathcal{W}$ (Guo et al., 2020) or leveraging low-rank decomposed matrices to compute $\Delta \mathcal{W}$ (Hu et al., 2021).

Algorithm 1: Sparsity-Embedded Low-Rank Decomposition

Input: Pretrained weights $\mathcal{W}$, number of non-zero elements N
Output: Sparse matrices $\mathcal{S}_2$

1 Initialize $\mathcal{S}_2$ to be an empty set.
2 **for** *each self-attention projection weights w_i in $\mathcal{W}$* **do**
    /* Decomposition */
3   Perform matrix decomposition: $w_i \approx \mathcal{U}\mathcal{V} + \mathcal{S}'$ by solving the optimization problem in Eqn.1.
    /* Identify important elements to form $\mathcal{S}_2$ */
4   Perform thresholding on $\mathcal{S}'$: Keep N elements in $\mathcal{S}'$ with top magnitudes, and set the rest 0.
5   Append $\mathcal{S}'$ into $\mathcal{S}_2$.
6 **end**

Algorithm 2: DSEE

Input: Pretrained weights $\mathcal{W}$, number of non-zero elements N, desired sparsity s, loss function $\mathcal{L}$
Output: Sparse mask $\mathcal{S}_1$, matrices $\mathcal{U}, \mathcal{V}, \mathcal{S}_2$

1 Decompose $\mathcal{W}$ into $\mathcal{U}, \mathcal{V}$ and $\mathcal{S}_2$
2 (Re-)Initialization: $\mathcal{U} = 0, \mathcal{V} \sim \mathcal{N}(0, 0.02), \Omega =$ indexes of non-zero elements in $\mathcal{S}_2, \mathcal{S} = 0$
    /* I: train before pruning */
3 Train $\mathcal{U}, \mathcal{V}, \mathcal{S}$ with respect to $\mathcal{L}$ under the constraint of $P_{\Omega^C}(\mathcal{S}) = 0$.
    /* II: pruning the model */
4 Prune (1-s%) parameters in $\mathcal{W}$ globally by sorting the magnitude of $\mathcal{W} + \mathcal{U}\mathcal{V} + \mathcal{S}$, deriving the sparsity mask $\mathcal{S}_1$
    /* III: tuning after pruning */
5 Tune $\mathcal{U}, \mathcal{V}, \mathcal{S}_2$ for E epochs for recovering the performance.

3.2 Sparsity-Embedded Parameter-Efficient Fine-tuning

A recent study (Hu et al., 2021) enforces low-rank constraint to weight update tensors $\Delta \mathcal{W}$, and obtains satisfactory trade-off between parameter-efficiency and model quality. However, as revealed experimentally by (Yu et al., 2017), a part of the important information in the trained weights will also scatter outside the low-rank subspace, creating sparse "residuals". Inspired by these observations, we investigate a new sparsity-aware low-rank subspace of $\Delta \mathcal{W}$, and introduce the first component of our proposal in Figure 1, i.e., sparsity-embedded parameter-efficient fine-tuning.

Specifically, we identify a sparse subspace Ω, that we can project our update matrices $\Delta \mathcal{W}$ to. The update matrix is then decomposed into two components: a low-rank part which is represented by the multiplication of two low-rank matrices $\mathcal{U} \in \mathbb{R}^{m \times r}$ and $\mathcal{V} \in \mathbb{R}^{r \times n}$, and a sparse residual

$$\mathcal{S}_2 = \mathcal{P}_\Omega(\Delta \mathcal{W}), \text{ where } \mathcal{P}_\Omega(\Delta \mathcal{W}) = \begin{cases} s_{i,j}, & (i,j) \in \Omega \\ 0, & (i,j) \in \Omega^C \end{cases}, \; i = 1, 2, \ldots, m, \; j = 1, 2, \ldots, n.$$

As illustrated in Figure 1, the update matrix $\Delta \mathcal{W}$ can be approximated by $\mathcal{U}\mathcal{V} + \mathcal{S}_2$, in which the $\mathcal{U}, \mathcal{V}$, and the non-zero element of $\mathcal{S}_2$ are learnable parameters while Ω is fixed once determined.

Compared to the full fine-tuning schemes has $m \times n$ individual trainable parameters, our method only has $(m + n) \times r + \text{card}(\Omega)$. If r is smaller than $\frac{m \times n}{m+n} < \min\{m, n\}$, which is a loose bound, our method is capable of substantially reducing trainable parameters for downstream fine-tuning.

The next question is how to find appropriate Ω. Motivated by (Candès et al., 2011), we formulate our sparsity-aware decomposition as the following optimization problem:

$$\min_{\mathcal{U},\mathcal{V},\mathcal{S}_2} \quad \frac{1}{2}\|\mathcal{W} - \mathcal{U}\mathcal{V} - \mathcal{S}_2\|_{\mathbf{F}}^2$$
$$\text{s.t. } \text{rank}(\mathcal{U}) \leq r, \text{ rank}(\mathcal{V}) \leq r, \text{ card}(\mathcal{S}_2) \leq c, \tag{1}$$

where $\text{rank}(\cdot)$ indicates the rank and $\text{card}(\cdot)$ indicates the cardinality of a matrix. Here we derive Ω from pre-trained weights $\mathcal{W}$, which is different with previous low-rank techniques for model compression since we perform prior-training decomposition and can not access $\Delta\mathcal{W}$ before fine-tuning. In this way, we actually assume that $\Delta\mathcal{W}$ shares a similar crucial subspace Ω with $\mathcal{W}$ (Sun et al., 2018). We uses the GreBsmo algorithm (Zhou & Tao, 2013) to solve this optimization problem. This method adopts a similar idea as random projection and can solve the optimization problem rapidly.

Algorithm 1 summarizes the detailed procedure of our proposal. We first decompose the pretrained weights $\mathcal{W}$ into three matrices: $\mathcal{U}$, $\mathcal{V}$ and $\mathcal{S}_2$. $\mathcal{U}$ and $\mathcal{V}$ are matrices of low-rank and $\mathcal{S}_2$ is a sparse matrix. After the decomposition, we re-initialize $\mathcal{U}$ and $\mathcal{V}$ to be of shape $\mathbb{R}^{m \times r}$ and $\mathbb{R}^{r \times n}$. The initial values for $\mathcal{U}$ are set to 0, and the initial values for $\mathcal{V}$ will follow a normal distribution as Hu et al. (2021) did. We do not use the decomposed value inside $\mathcal{S}_2$, but only the index of non-zero elements. We collect the indexes of non-zero elements into Ω, and reset the values of $\mathcal{S}_2$ back to 0. During the update, we only update the elements of $\mathcal{S}_2$ whose indexes are in Ω.

3.3 Dually Sparsity-Embedded Efficient Tuning (DSEE)

Besides parameter-efficiency, resource-efficiency is another major goal of our proposed framework. Sparsity-embedded low-rank weight updates, alone, does not necessarily lead to computational cost reductions, since it works together with the dense pre-trained weights and the massive computation during forward processes is inevitable. To achieve both resource- and parameter-efficiency, we also promote a sparse weight structure to the final fine-tuned model, as demonstrated by the sparse mask $\mathcal{S}_1$ in Figure 1. Our DSEE explores both unstructured/structural sparsity patterns as follows.

▷ **Pruning with unstructured sparse masks.** Unstructured sparse mask is the most widely used mask since it usually produces almost undamaged performance compared to its dense counterpart (Han et al., 2015a). It applies fine-grained manipulation on each individual model weight, while the generated irregular sparse masks bring limited hardware speedup (Wen et al., 2016). Specifically, based on the weight matrix $\mathcal{W}$, a sparse mask $\mathcal{S}_1$ can be calculated with various approaches either heuristic or optimization-based. We adopt the one-shot magnitude pruning (Han et al., 2015a) in DSEE, due to its simplicity and competitive performance.

In our context, we create the sparse pattern $\mathcal{S}_1$ from $\mathcal{W} + \mathcal{U}\mathcal{V}$: first, it sorts the magnitude (i.e., absolute value) of individual weights and removes parameters with bottom $1 - k\%$ magnitude. Second, we further tune the value of the low-rank update matrices for a few epochs, which is important to keep the performance as stated in Han et al. (2015b). Third, the sparse mask $\mathcal{S}_1$ that we derive will be applied on the pretrained weights only and do not affect the output from the update matrices, as $\mathcal{W} \odot \mathcal{S}_1 + \mathcal{U}\mathcal{V}$. For a input sample x, the output is calculated by $(\mathcal{W} \odot \mathcal{S}_1 + \mathcal{U}\mathcal{V})x = \mathcal{W} \odot \mathcal{S}_1 x + \mathcal{U}\mathcal{V}x$, where the first term $\mathcal{W} \odot \mathcal{S}_1 x$ brings significant resource-efficiency.

▷ **Pruning with structured sparse masks.** The second method exploits structural sparse masks, whose regular patterns are more hardware friendly yet have worse performance than unstructured masks. Our DESST considers ℓ_1 sparse regularization (Liu et al., 2017; Chen et al., 2021) to craft high-quality structural subnetworks. More precisely, motivated by Chen et al. (2021), we introduce learnable coefficients ξ before each attention head module, and append a ℓ_1 sparse penalty on ξ to the original loss. Detailed formulations are depicted as below:

We add trainable coefficients c before attention heads. The parameters c are optimized together with the decomposed matrices, *i.e.*, $\mathcal{U}, \mathcal{V}$ and $\mathcal{S}_2$. An extra term $\lambda\|c\|_1$ will be added to the training loss for sparse regularization. The value of λ are set to 1e-4. After training, we prune the attention

heads that have the lowest contribution to the model (*i.e.,* lowest c). We use a layer-wise pruning scheme that prune a same proportion of heads in each attention layer. After pruning, several epochs of tuning are run to recover the performance of the pruned model. The size of update matrices will change after structured pruning, so we also need to change the dimension of $\mathcal{U}$ and $\mathcal{V}$. Specifically, we change the size of $\mathcal{V}$ from $\mathbb{R}^{r \times n}$ to $\mathbb{R}^{r \times [n \times s]}$ where s is the pruning ratio of the corresponding self-attention layer and $[x]$ is the biggest integer that is not greater than x. The size of $\mathcal{S}_2$ is shrank accordingly.

4 EXPERIMENT RESULTS

Datasets and models. We use three classical pre-trained language models in our experiments: BERT$_{\text{BASE}}$ (Devlin et al., 2019), GPT-2 (Radford et al., 2019), and DeBERTa-large (He et al., 2020), which have 12/24/24 layers with hidden size of 768/1024/1024 and 110/354/380M trainable parameters, respectively. For BERT and DeBERTa, we evaluate our method on the GLUE benchmarks (Wang et al., 2018). For GPT-2, we use E2E (Novikova et al., 2017), WebNLG (Gardent et al., 2017), and DART (Nan et al., 2021) for evaluations.

Training and evaluation details. For BERT and DeBERTa, we follow the default settings in Wolf et al. (2019); Devlin et al. (2019). We use a linear learning rate decay scheduler with no warm-up and the AdamW (Loshchilov & Hutter, 2017) optimizer for downstream training. The batch size for BERT and DeBERTa is 32, 8 per GPU. We train 3 epochs to search the sparse mask $\mathcal{S}_1$, and continue to tune the model for 3 epochs to converge. For GPT-2, we follow the same hyperparameters as in Hu et al. (2021). The learning rate is 2e-4, and the training batch size is 2. We train the model for 5 epochs to search for the mask, and further tune the pruned model for 2 epochs.

Evaluation Metrics. For tasks on BERT and DeBERTa, we use accuracy in the evaluation by default, which is also the conventional setting in the NLP community. This includes accuracy, Matthew's Correlation and Pearson's r. On GPT-2, we use BLEU (Papineni et al., 2002), METEOR (Denkowski & Lavie, 2014), TER (Snover et al., 2006) and NIST (Doddington, 2002) as our evaluation metrics. To evaluate the efficiency of models, we use number of trainable parameters to measure the parameter efficiency, use Sparsity in Pretrained Weights to measure the resource efficiency, and FLOPs to evaluate the computational efficiency.

Baselines. On BERT and DeBERTa, we conduct comparisons with the following baseline methods: ❶ Fine-tune: directly fine-tunes the full model; ❷ EarlyBERT (Chen et al., 2021); ❸ BERT Ticket Tickets (Chen et al., 2020); ❹ OMP: prune the fine-tuned weights and fine-tune again afterwards; and ❺ LoRA (Hu et al., 2021). We also report the Huggingface's fine-tuning results.

On GPT-2, we conduct comprehensive comparisons with multiple baseline methods: ❶ Adapters (Houlsby et al., 2019): insert adapters after linear layers; ❷ FT-Top2: fine-tune the top 2 layers only; ❸: Prefix: prefix tuning introduced by (Li & Liang, 2021); and ❹ LoRA: low-rank decomposition, which assumes $\Delta \mathcal{W} = \mathcal{U}\mathcal{V}$; most results are directly cited from Hu et al. (2021).

4.1 EFFICIENT TUNING WITH DSEE

Parameter-efficiency with sparse masks. To verify that simple low-rank adaptation has limitations, we compare its performance with the performance of our sparsity-embedded efficient fine-tuning. Table 1 shows that on MNLI, SST-2, CoLA, and STS-B, assuming $\Delta \mathcal{W} = \mathcal{U}\mathcal{V}$ only, has limitation. Adding a small proportion of parameters (only 3072 trainable parameters) can bring performance

Table 1: Performance comparison with BERT$_{\text{BASE}}$ on SST-2, MNLI, CoLA, and STS-B.

Dataset	# Trainable Parameters	SST-2	MNLI	CoLA	STS-B
Metric	-	Acc	Acc	Corr.	Pearson's r
Fine-tune	109.9M	92.32	82.12	0.570	0.890
$\Delta \mathcal{W} = \mathcal{U}\mathcal{V}$	589.8K	92.09	80.79	0.575	0.891
$\Delta \mathcal{W} = \mathcal{U}\mathcal{V}$	294.9K	92.09	80.49	0.580	0.892
$\Delta \mathcal{W} = \mathcal{U}\mathcal{V} + \mathcal{S}_2$	298.0K	92.78	80.64	0.588	0.895

boost to the model. Specifically, under the rank $r = 8$, the metrics increases (0.69/0.13/0.008/0.003) on SST-2/MNLI/CoLA/STS-B, respectively. Moreover, using only approximately half of the number of trainable parameters, our method can achieve comparable parameters compared to LoRA. Table 2 shows the performance on GPT-2. For all three tasks, our method can achieve comparable results with only about half of the trainable parameters with LoRA with rank equals to 4, and achieve substantial performance gain compared to LoRA with rank equals to 2. On WebNLG, our method

even achieve a higher BLEU score, 55.56 versus 55.29, with only half of the model's size. Such phenomenon indicates that adding a sparse matrix on the basis of low-rank decomposition can make substantial improvements.

Table 2: Performance comparison on GPT-2. Results of direct fine-tuning are cited from Hu et al. (2021). We compare different efficient fine-tuning settings. Results of $r = 4$ is directly taken from (Hu et al., 2021).

Dataset	# Trainable Parameters	E2E			WebNLG			DART		
Metric	-	BLEU	MET	NIST	BLEU	MET	TER	BLEU	MET	TER
Fine-tune	354.92M	68.2	46.2	8.62	47.60	0.39	0.50	46.0	0.39	0.46
$\Delta W = \mathcal{U}\mathcal{V}$	0.39M	70.4	46.9	8.84	55.29	0.4143	0.3938	48.23	0.392	0.469
$\Delta W = \mathcal{U}\mathcal{V}$	0.20M	69.2	45.9	8.74	55.23	0.4134	0.3957	46.49	0.387	0.477
$\Delta W = \mathcal{U}\mathcal{V} + \mathcal{S}_2$	0.20M	69.8	46.5	8.79	55.56	0.4132	0.3916	47.08	0.390	0.472

Resource- and parameter-efficiency with sparse masks. We report the performance of DSEE, including both the number of trainable parameters and the sparsity in pretrained weights. We use an unstructured sparsity of 50%, and structured sparsity of 25% and 33%, which is equal to pruning 1/4 and 1/3 heads from each attention head. Moreover, we prune each of the intermediate layers using a structured sparsity of 40% as in (Chen et al., 2021). For $\text{BERT}_{\text{BASE}}$ and DeBERTa-large, we set the r (the low-rank dimension) to be 16, and N (the number of non-zero elements in $\mathcal{S}_2$) to be 64. For GPT, we set r to be 2 in DSEE and 4 in LoRA. The choice of N remains 64.

Table 3 summarizes the performance on $\text{BERT}_{\text{BASE}}$. On $\text{BERT}_{\text{BASE}}$, Our DSEE method can: ❶ achieve parameter-efficiency at high level and retain the performance on various downstream tasks. On $\text{BERT}_{\text{BASE}}$, with only about 600K trainable parameters ($110/0.5 \approx 200\times$ smaller than the full model), DSEE can achieve comparable performance on all GLUE tasks. ❷ DSEE can achieve resource-efficiency in the final models. Using either unstructured or structured sparse masks can reach our goal of reducing the number of parameters in the pretrained weights without sacrificing much performance. At the sparsity level of 50%, unstructured DSEE can achieve an accuracy of 90.46% on QNLI, surpassing the baseline of fine-tuning, whose result is 90.15%. At the sparsity level of 25%, the structured DSEE can have performance gains ranging from 0.46% to 2.22% except QQP and QNLI. At the sparsity level of 33%, the performance gains range from 0.11% to 2.04% except QQP and QNLI. ❸ Compared to other baselines, *e.g.,* EarlyBERT and BERT Tickets, our method benefits from parameter efficiency, which updates the weights more efficiently. These observations validate the effectiveness of our DSEE method.

We also calculate FLOs on $\text{BERT}_{\text{BASE}}$ and the STS-B dataset. Directly fine-tuning the $\text{BERT}_{\text{BASE}}$ on STS-B for 3 epochs takes a FLOPs of 1.13505×10^{15}, while LoRA takes a FLOPs of 1.14287×10^{15}, which is 0.69% higher than directly fine-tuning. On the contrary, the structured DSEE takes a FLOPs of 7.47633×10^{14} at the sparsity of 25%, and 7.1601×10^{14} at the sparsity of 33%, which is 34.61$ and 37.38% lower than the FLOPs taken by LoRA. Note that we cannot save FLOPs when training the models with DSEE, but we can achieve computational efficiency when using the trained models for inference.

Table 3: $\text{BERT}_{\text{BASE}}$ performance on GLUE benchmarks. The star sign (*) in the sparsity column indicates that it represents structured sparsity.

Methods	# Trainable Parameters	Sparsity in Pretrained Weights	Dataset							
			CoLA	STS-B	MNLI	QQP	QNLI	MRPC	RTE	SST-2
Fine-tune	110M	0%	57.02	88.97	82.12	91.01	90.15	85.29	70.40	92.32
EarlyBERT	110M	33%	41	-	79.97	89.44	89.86	80.39	61.01	90.94
BERT Tickets	110M	{50%,50%,70%,90%,70%,50%,60%,60%}	54.5	88.4	82.4	90.2	89.1	85.2	66.2	92.1
OMP	$\sim$ 55M	50%	56.17	88.66	81.97	90.72	89.80	82.84	70.04	92.18
LoRA	589.8K	0%	58.58	89.10	80.79	86.43	88.16	86.27	71.48	92.09
DSEE	592.9K	50%	56.74	88.77	81.41	87.21	90.46	85.05	70.04	90.83
DSEE	592.9K	25%*	59.01	89.90	84.34	90.99	90.94	86.76	71.84	92.78
DSEE	592.9K	33%*	57.79	89.93	84.16	90.78	91.09	87.25	71.48	92.43

Table 4 summarizes the performance on GPT-2, which shares the similar trend. DSEE can achieve $1000\times$ reduction in trainable parameters and $2\times$ reduction in the final fine-tuned model size with no loss in downstream task performance compared to conventional finetuning. When compared to LoRA, DSEE can retain the same level of the number of trainable parameters and downstream task performance, while showing a $2\times$ reduction in the final fine-tuned model size.

Table 4: GPT-2 medium performance on E2E, WebNLG and DART. LoRA[†]: reproduced results.

Methods	# Trainable Parameters	Sparsity in Pretrained Weights	E2E			WebNLG			DART		
Metric	-	-	BLEU	MET	NIST	BLEU	MET	TER	BLEU	MET	TER
Fine-tune[2]	354.92M	0%	68.2	0.462	8.62	47.6	0.39	0.50	46.0	0.39	0.46
Adapters	11.48M	0%	68.9	0.461	8.71	55.2	0.41	0.39	45.4	0.38	0.46
FT-Top2	25.19M	0%	68.1	0.460	8.59	33.5	0.26	0.75	38.1	0.34	0.56
Prefix	0.35M	0%	69.7	0.461	8.81	54.4	0.41	0.41	45.7	0.38	0.46
LoRA	0.39M	0%	70.4	0.468	8.85	55.3	0.41	0.39	47.5	0.39	0.45
LoRA[†]	0.39M	0%	70.06	0.467	8.84	55.29	0.4143	0.3938	48.23	0.392	0.469
DSEE	0.17M	30%	69.33	0.465	8.73	55.78	0.4163	0.3921	47.21	0.390	0.471
DSEE	0.17M	50%	69.75	0.469	8.78	55.40	0.4124	0.3935	46.66	0.389	0.471

Table 6: Performance comparison on BERT$_{\mathrm{BASE}}$ with different masks embedded.

Methods	# Trainable Parameters	Sparsity in Pretrained Weights	Dataset			
			SST-2	MNLI	CoLA	STS-B
Metric	-	-	Acc	Acc	Corr.	Pearson's r
Fine-tune	110M	0%	92.32	82.12	57.02	88.97
$\mathcal{W} \odot \mathcal{S}_1$	55M	50%	91.28	81.97	56.17	88.66
$\mathcal{W} \odot \mathcal{S}_1 + \mathcal{U}\mathcal{V}$	294K	50%	90.66	81.13	56.64	88.41
$\mathcal{W} + \mathcal{U}\mathcal{V} + \mathcal{S}_2$	295K	0%	92.43	80.99	58.60	89.31
$\mathcal{W} \odot \mathcal{S}_1 + \mathcal{U}\mathcal{V} + \mathcal{S}_2$	295K	50%	90.83	81.41	56.74	88.77

Finally we validate our method on DeBERTa. The results are displayed in Table 5. We use four datasets, SST-2, MNLI, CoLA and STS-B. The four datasets have greatly varied sizes, which can be representatives of the GLUE benchmark. DeBERTa is a larger model so applying low-rank decomposition with our hyperparameters cannot reach the performance of fine-tuning. Comparing to LoRA, our method reaches a higher performance on downstream tasks, albeit it needs a slightly more training epochs. The main advantage of DSEE compares to LoRA is that, the burden on resources such as storing the pretrained weights are relieved. Although there is a slight extra cost for search the sparse mask $\mathcal{S}_1$, it can be amortized by the efficiency gained in the future inference.

4.2 UNDERSTANDING DSEE

The position of embedded sparsity plays a crucial important role in our proposed DSEE. For instance, applying sparse masks to the pre-trained weights or weight updates produces resource- and parameter-efficiency. Precisely, we compare four different methods

Table 5: DeBERTa-large performance on CoLA, MNLI, MRPC and RTE.

Methods	# Trainable Parameters	Sparsity in Pretrained Weights	Dataset			
			CoLA	MNLI	MRPC	RTE
LoRA	786.4K	0%	63.36	88.90	90.44	75.09
DSEE	789.5K	30%	67.35	90.58	90.20	77.98
DSEE	789.5K	50%	63.82	90.03	89.71	74.73

on BERT$_{\mathrm{BASE}}$: one-shot magnitude weight pruning ($\mathcal{W} \odot \mathcal{S}_1$), two DSEE's variants ($\mathcal{W} \odot \mathcal{S}_1 + \mathcal{U}\mathcal{V}$) and $\mathcal{W} + \mathcal{U}\mathcal{V} + \mathcal{S}_2$), DSEE ($\mathcal{W} \odot \mathcal{S}_1 + \mathcal{U}\mathcal{V} + \mathcal{S}_2$). The results are collected in Table 6. We can see that: ❶ NO embedded sparsity into the pretrained weights yields overall best performance. This is intuitive since the valuable knowledge learned from massive pretraining data is intact and not removed. ❷ Embedding sparsity into the pretrained weights harms only little to no performance. A similar conclusion is drawn by Chen et al. (2020) which validated that a pruned model can have similar performance as the dense model. ❸ Using sparsity-embed efficient fine-tuning with the sparse pre-trained weights can also preserve performance, as well as achieving parameter efficiency.

4.3 ABLATION AND VISUALIZATION

Different methods to generate sparse matrix $\mathcal{S}_2$ In this section, we compare the performance of BERT$_{\mathrm{BASE}}$ using different methods to generate the sparse matrix $\mathcal{S}_2$ and the corresponding space Ω. Except the aforementioned matrix decomposition method, we try to (1) randomly sample indexes into Ω; and (2) directly select the indexes of elements of highest magnitude of $\mathcal{W}$ into Ω. In Figure 2 we can see that using the matrix decomposition method has the highest metric overall. It is also noteworthy that sparse matrices generated by other methods will sometimes harm the performance.

Another factor is the number of non-zero elements inside $\mathcal{S}_2$. More non-zero elements in $\mathcal{S}_2$ reduce the parameter efficiency, while less non-zero elements increase the efficiency but may not be much beneficial to the accuracy or other metrics. Figure 2 also shows the relationship between number of non-zero elements in $\mathcal{S}_2$ and the performance on fine-tuned model on SST-2. From the graph we can

see that, using an N of 64 seems to have the most stable results compared to other choices. Another important information we can derive from the figure is that, higher number of non-zero elements in the $\mathcal{S}_2$ does not guarantee a better performance.

Ablation of # ranks. The rank of low-rank decomposition r is crucial to the transfer learning performance. A small r will result in lower representation ability, and a large r will bring more parameters and reduce the parameter efficiency. To find the best value, we conduct experiments with different ranks r on four datasets, SST-2, MNLI, CoLA and STS-B. The results are displayed in Figure 3. We add quadratic trend lines in the graph along with the discrete points to smooth

Figure 2: *Left*: Different method for generating $\mathcal{S}_2$ in $BERT_{Base}$. *Right*: Different number of non-zero elements in $\mathcal{S}_2$. Empty: no non-zero element in $\mathcal{S}_2$. Decompose: matrix decomposition method aforementioned. Magnitude: picking elements with highest magnitude. Random: random matrix.

the results. We can draw two conclusions from the graphs: ❶ Overall, the final performance is positively correlated with the number of trainable parameters; however on some tasks (MNLI, CoLA) higher number of parameters (namely, the r for $\mathcal{U}$ and $\mathcal{V}$) will lead to lower performance. ❷ With a sparse matrix embedded, the performance of the trained models can be improved within a range of trainable parameters. On SST-2 and CoLA, the applicable range seems to be $10\times^{4.5} \sim 10\times^6$. On STS-B, our method can consistently outperform the performance of using low-rank decomposition only. For MNLI the two methods behave similarly while our method is slightly better.

Figure 3: Performance comparison of two decomposition methods under different ranks. We add quadratic trend lines for better visualization quality.

Ablation of sparsity. Although creating sparsity in pre-trained weights $\mathcal{W}$ does not change the number of trainable parameters of models, the different levels of sparsity control the number of non-zero elements and thereby influence the representation ability. We conduct experiments on BERT with different sparsity. The sparsity levels range from 10% to 60%. The results are in Figure A5. From the figures we can draw conclusions: ❶ DSEE out-performs magnitude pruning at low sparsity ($< 50\%$) with respect to the performance on downstream tasks. ❷ DSEE surpasses vanilla magnitude pruning with respect to the number of parameters. For each self-attention layer, using vanilla magnitude pruning needs to train all the weights while DSEE only needs to update the two low-rank matrices.

Figure 4: Weight change distributions.

Visualizations. Figure 4 shows the distribution of weight change. From the graph we can see that most weights are located around 0. Such phenomenon indicates that a naturally sparsity exists within the update matrices, motivating us to explore sparse structures along with matrix decomposition.

5 CONCLUSION

This paper draws the prior of sparsity and establishes the DSEE framework. It is the first attempt towards jointly optimizing both parameter efficiency of the fine-tuning process, and the resource efficiency of the fine-tuned model. On state-of-the-art large-scale language models (e.g., BERT, GPT, and DeBERTa) and across dozens of datasets, DSEE consistently demonstrates highly impressive parameter, training, and inference efficiency, in addition to preserving a competitive downstream transfer performance. Our future work targets extending DSEE to the finetuning of large-scale computer vision and/or multi-modal pre-trained models.

6 REPRODUCIBILITY CHECKLIST

To ensure reproducibility, we use the Machine Learning Reproducibility Checklist v2.0, Apr. 7 2020 (Pineau et al., 2021). An earlier version of this checklist (v1.2) was used for NeurIPS 2019 (Pineau et al., 2021).

- For all **models** and **algorithms** presented,
  - **A clear description of the mathematical settings, algorithm, and/or model.** We clearly describe all of the settings, formulations, and algorithms in Section 4.
  - **A clear explanation of any assumptions.** We do not make assumptions.
  - **An analysis of the complexity (time, space, sample size) of any algorithm.** We do not make the analysis.
- For any **theoretical claim**,
  - **A clear statement of the claim.** We do not make theoretical claims.
  - **A complete proof of the claim.** We do not make theoretical claims.
- For all **datasets** used, check if you include:
  - **The relevant statistics, such as number of examples.** N/A.
  - **The details of train/validation/test splits.** We follow conventional settings.
  - **An explanation of any data that were excluded, and all pre-processing step.** We did not exclude any data or perform any pre-processing.
  - **A link to a downloadable version of the dataset or simulation environment.** Most of our datasets and pretrained models can be retrieve from `https:// huggingface.co/`.
  - **For new data collected,a complete description of the data collection process, such as instructions to annotators and methods for quality control.** We do not collect or release new datasets.
- For all shared **code** related to this work, check if you include:
  - **Specification of dependencies.** We will give installation instructions in the README of our repository.
  - **Training code.** The training code is available in our repository.
  - **Evaluation code.** The evaluation code will be available in our repository.
  - **(Pre-)trained model(s).** We do not release any pre-trained models. The code to run all experiments in our work can be found in the GitHub repository.
  - **README file includes table of results accompanied by precise command to run to produce those results.** We will include a README with detailed instructions to reproduce all of our experimental results.
- For all reported **experimental results**, check if you include:
  - **The range of hyper-parameters considered, method to select the best hyper-parameter configuration, and specification of all hyper-parameters used to generate results.** We provide all details of the hyper-parameter tuning in Section 4 and A1.
  - **The exact number of training and evaluation runs.** We only run each experiment one time.
  - **A clear definition of the specific measure or statistics used to report results.** We use the classification accuracy on test-set, which is defined in Section 4.
  - **A description of results with central tendency (e.g. mean) & variation (e.g. error bars).** We do not include these results.
  - **The average runtime for each result, or estimated energy cost.** We report FLOPs.
  - **A description of the computing infrastructure used.** All detailed descriptions are presented in Section A1.

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A1 MORE IMPLEMENTATION DETAILS

We report the setting of other hyperparameters of our experiments, such as learning rate, in Table A7. The device we used for experiments are various, including NVIDIA GeForce GTX 1080 Ti, GeForce RTX 2080 Ti, Titan RTX, RTX and A6000.

Architecture	Method	Parameters	Dataset							
			MNLI	QNLI	QQP	SST-2	CoLA	MRPC	RTE	STS-B
BERT$_{BASE}$	Fine-tune	Learning Rate					5e-5			
BERT$_{BASE}$	DSEE (before pruning)	Learning Rate	5e-5	5e-5	5e-5	2e-4	1e-3	8e-4	1e-3	8e-4
BERT$_{BASE}$	DSEE (after pruning)	Learning Rate	5e-5	5e-5	5e-5	5e-5	1e-3	5e-4	5e-4	5e-4
DeBERTa-large	LoRA & DSEE (before pruning)	Learning Rate	1e-5				1e-3	8e-4	8e-5	
DeBERTa-large	DSEE (after pruning)	Learning Rate	1e-5				5e-5	8e-4	6e-5	

Table A7: Hyper-parameters we used on different dataset. BERT$_{BASE}$.

A2 MORE EXPERIMENT RESULTS

Ablation of Sparsity To study the relationship between sparsity of unstructured pruning and the behavior of our DSEE, we conduct an ablation study on various datasets in GLUE benchmarks. The results are shown in Figure A5

Figure A5: DSEE performance compared to vanilla magnitude pruning at different sparsity. Magnitude Pruning: vanilla magnitude pruning which tunes $\mathcal{W}$ directly.