Plan Your Target and Learn Your Skills: State-Only Imitation Learning via Decoupled Policy Optimization

Abstract

State-only imitation learning (SOIL) enables agents to learn from massive demonstrations without explicit action or reward information. However, previous methods attempt to learn the implicit state-to-action mapping policy directly from state-only data, which results in ambiguity and inefficiency. In this paper, we overcome this issue by introducing hyper-policy as sets of policies that share the same state transition to characterize the optimality in SOIL. Accordingly, we propose Decoupled Policy Optimization (DPO) via explicitly decoupling the state-to-action mapping policy as a state transition predictor and an inverse dynamics model. Intuitively, we teach the agent to plan the target to go and then learn its own skills to reach. Experiments on standard benchmarks and a real-world driving dataset demonstrate the effectiveness of DPO and its potential of bridging the gap between reality and simulations of reinforcement learning.

1 Introduction

Imitation learning offers a way to train an intelligent agent from demonstrations by mimicking the expert's behaviors without constructing hand-crafted reward functions [11, 15]. The corresponding methods normally require the expert demonstrations include information of both states and actions. Unfortunately, the action information is not always accessible from many real-world demonstration resources, e.g., online video recordings of car driving or sports. Thus a natural desire to take advantage of these massive and valuable resources motivates the study of state-only imitation learning (SOIL), also known as learning from observations (LfO) [22]. Analogy to human beings, SOIL is a more intuitive way to approach imitation by only matching the expert's state sequences without having explicit knowledge of the exact actions.

A wide range of algorithms have been proposed to solve SOIL by matching the state sequence of the expert [20, 21, 23]. However, the action agnostic setting in SOIL makes it challenging to determine the optimal action because of the partial observability of the expert demonstrations that multiple policies could be chosen to match the same expert state sequence. Thus learning a state-to-action policy is implicit, leading to an less efficient modeling of the explicit information from demonstrations, and in result could cause suboptimality.

To this end, in this paper, we introduce the concept of *hyper-policy* denoting a *family* of policies that share the same state transition. Based on that, instead of recovering the expert *policy*, we characterize the optimality in SOIL by finding the expert *hyper-policy*. The proposed method is called decoupled policy optimization (DPO), which separates the policy into two modules: an expert state transition predictor that finds the optimal *hyper-policy*, followed by an inverse dynamics model that obtains the executable *policy*. Intuitively, the expert state transition predictor predicts the target, while the

inverse dynamics model enables the agent to learn its own skills to reach. DPO takes the advantage of such a decoupled structure by separately learning two kinds of data: (1) the expert state transition that is accessible in the demonstration; (2) the action to be performed which should be obtained by interacting with the environment.

To ensure the benefit of DPO, these two modules should work coherently to provide accurate foresight for targets and corresponding skills. To mitigate the difficulty, we and regularize the state transition predictor to prevent the model from predicting non-neighboring states via multi-step and cycle training style. Further, to improve the learning efficiency by encouraging the agent to reach the expert states, we augment reward and apply policy gradient to DPO with additional generative adversarial objective.

Experiments on standard benchmarking tasks show the advantage of the decoupled structure and the higher efficiency of DPO. We also evaluate DPO on a real-world driving dataset with state-only demonstrations, and the result shows that DPO can learn driving behaviors closer to human drivers when compared with baseline methods.

2 Preliminaries

Notations. We consider a γ-discounted infinite horizon Markov decision process (MDP) as a tuple $\mathcal{M} = \langle \mathcal{S}, \mathcal{A}, \mathcal{T}, \rho_0, r, \gamma \rangle$, where $\mathcal{S}$ is the set of states, $\mathcal{A}$ represents the action space, $\mathcal{T} : \mathcal{S} \times \mathcal{A} \times \mathcal{S} \to [0, 1]$ is the state transition probability distribution, $\rho_0 : \mathcal{S} \to [0, 1]$ is the distribution of the initial state s_0, and $\gamma \in [0, 1]$ is the discount factor. The agent makes decisions through a policy $\pi(a|s) : \mathcal{S} \times \mathcal{A} \to [0, 1]$ and receives rewards $r : \mathcal{S} \times \mathcal{A} \to \mathbb{R}$.

Occupancy Measure. The concept of occupancy measure (OM) [8] is proposed to characterize the statistical properties of a certain policy interacting with an MDP. Specifically, the state OM is defined as the time-discounted cumulative stationary density over the states under a given policy π: $\rho_\pi(s) = \sum_{t=0}^{\infty} \gamma^t P(s_t = s|\pi)$. Following such a definition we can define different OM:

a) State-action OM: $\rho_\pi(s, a) = \pi(a|s)\rho_\pi(s)$

b) State transition OM: $\rho_\pi(s, s') = \int_{\mathcal{A}} \rho_\pi(s, a)\mathcal{T}(s'|s, a)\,\mathrm{d}a$

c) Joint OM: $\rho_\pi(s, a, s') = \rho_\pi(s, a)\mathcal{T}(s'|s, a)$

Imitation Learning from State-Only Demonstrations. Imitation learning (IL) [11] studies the task of learning from demonstrations (LfD), which aims to learn a policy from expert demonstrations without getting access to the reward signals. The expert demonstrations typically consist of expert state-action pairs. General IL objective minimizes the state-action OM discrepancy:

$$\pi^* = \arg\min_\pi \mathbb{E}_{s \sim \rho_\pi^s} \left[\ell\left(\pi_E(\cdot|s), \pi(\cdot|s)\right) \right] = \arg\min_\pi \ell\left(\rho_{\pi_E}(s, a), \rho_\pi(s, a)\right) , \tag{1}$$

where ℓ denotes some distance metric. For example, GAIL [8] chooses to minimize the JS divergence $\mathrm{D_{JS}}(\rho_{\pi_E}(s, a)\|\rho_\pi(s, a))$, and AIRL [3] utilizes the KL divergence $\mathrm{D_{KL}}(\rho_{\pi_E}(s, a)\|\rho_\pi(s, a))$ instead. However, for the scenario studied in this paper, the action information is absent in state-only demonstrations, known as state-only imitation learning (SOIL) or learning from observations (LfO) problems, where the action spaces between the expert and the agent can even be different. Such challenges prevent applying typical IL solutions. An existing method for this problem is to indirectly optimize the discrepancy of the state transition OM without modeling the state transition [21]:

$$\pi^* = \arg\min_\pi [\ell\left(\rho_{\pi_E}(s, s'), \rho_\pi(s, s')\right)] . \tag{2}$$

However, the solution to this problem is ambiguous since there is no one-to-one correspondence between $\rho(s, s')$ and π as we will show in the following section. As such, the optimality of SOIL should be reconsidered.

3 Methodology

3.1 Characterizing the Optimality in SOIL

In standard IL tasks, when the expert actions are accessible in demonstrations, perfectly imitating the expert policy corresponds to matching the state-action OM due to the one-to-one correspondence

between π and ρ_π [8, 19]. However, such correspondence is not applicable for the state transition OM in SOIL.

Proposition 1. *Suppose Π is the policy space and $\mathcal{P} = \{\rho : \rho \geq 0\}$ is a feasible set of OM, then a policy $\pi \in \Pi$ corresponds to one state transition OM $\rho_\pi \in \mathcal{P}$. However, a state transition OM $\rho \in \mathcal{P}$ can correspond to more than one policy in Π.*

The proof can be found in Appendix B. As a result, if we choose to optimize a state-to-action mapping policy, then the optimal solution to Eq. (2) is ambiguous that may have more than one answer. This could cause training instability and lead to sub-optimal policies. Besides, since the action information is latent in the expert demonstration, a state-to-action mapping function may be too implicit for matching the state sequence. In that case, we must find a one-to-one corresponding solution to solve SOIL explicitly and efficiently. Before continuing, we introduce the definition of a *hyper-policy*.

Definition 1. *A hyper-policy Ω is a set of policies such that for any $\pi_1, \pi_2 \in \Omega$, we have $\rho_{\pi_1}(s, s') = \rho_{\pi_2}(s, s')$.*

Then by definition, we know there is a one-to-one correspondence between the hyper-policy Ω and the state transition OM $\rho_\Omega(s, s')$. Similar to the normal state-to-action mapping policy, a hyper-policy Ω can be regarded as a state-to-state mapping function $h_\Omega(s'|s)$ which predicts the state transition such that for any $\pi \in \Omega$:

$$h_\Omega(s'|s) = \frac{\rho_\Omega(s, s')}{\int_{\tilde{s}} \rho_\Omega(s, \tilde{s}) \, d\tilde{s}} = \int_a \pi(a|s) \mathcal{T}(s'|s, a) \, da . \tag{3}$$

Proposition 2. *Suppose the state transition predictor is defined as in Eq. (3) and Γ is its space, $\mathcal{P} = \{\rho : \rho \geq 0\}$, then a hyper-policy state transition predictor $h_\Omega \in \Gamma$ corresponds to one state transition OM $\rho_\Omega \in \mathcal{P}$; and a state transition OM $\rho \in \mathcal{P}$ only corresponds to one hyper-policy state transition predictor such that $h_\rho = \rho(s, s') / \int_{\tilde{s}} \rho(s, \tilde{s}) \, d\tilde{s}$.*

Therefore, we find a one-to-one correspondence between the optimization term $\rho(s, s')$ and a practical target $h_\Omega(s'|s)$, which indicates that we do not have to infer the expert actions under state-only demonstrations but only need to recover the state transition predictor of the hyper-policy Ω_E:

$$\arg\min_\Omega [\ell \left(\rho_{\Omega_E}(s, s'), \rho_\Omega(s, s') \right)] = \arg\min_{h_\Omega} \mathbb{E}_{s \sim \Omega} [\ell \left(h_{\Omega_E}(s'|s), h_\Omega(s'|s) \right)] . \tag{4}$$

However, SOIL still requires to learn a policy to interact with the MDP environment to match the state transition OM of the expert. This is achievable since we do not have to recover the expert policy π_E exactly but can learn any policy $\pi \in \Omega_E$ according to Eq. (4).

3.2 Policy Decoupling

To construct an unambiguous objective for SOIL, we define hyper-policy and solve the problem by finding the state transition predictor of the expert hyper-policy. Intuitively, this tells the agent the *target* that the expert will reach without informing any feasible *skill* that require the agent to learn itself. Therefore, to recover a $\pi \in \Omega_E$, we can construct an inverse dynamics such that

$$\pi = \underbrace{\mathcal{T}_\pi^{-1}}_{\text{Inverse dynamics}} (\underbrace{\mathcal{T}(\pi_E)}_{\text{Expert state transition predictor}}) . \tag{5}$$

Formally, the expert policy can be decoupled as

$$\pi_E(a|s) = \int_{s'} \mathcal{T}(s'|s, a) \pi_E(a|s) \, ds' = \int_{s'} \frac{\rho_{\pi_E}(s, a, s')}{\rho_{\pi_E}(s)} \, ds' = \int_{s'} \frac{\rho_{\pi_E}(s, s') I_{\pi_E}(a|s, s')}{\rho_{\pi_E}(s)} \, ds'$$
$$= \int_{s'} h_{\pi_E}(s'|s) I_{\pi_E}(a|s, s') \, ds' . \tag{6}$$

Notice that both the state transition predictor h and the inverse dynamics model is policy dependent. Nevertheless, recall that the optimality in SOIL only requires us to recover $\pi \in \Omega_E$, we do not have to learn about I_{π_E} but just one feasible path $I(a|s, s')$. Then a policy can be actually recovered by

$$\pi \in \Omega_E = \mathbb{E}_{\underbrace{s' \sim h_{\Omega_E}(s'|s)}_{\text{target}}} \left[\underbrace{I(a|s, s')}_{\text{skill}} \right] . \tag{7}$$

117 Here the inverse dynamics model I offers an
118 arbitrary *skill* to reach the expected *target* state
119 provided by the state transition predictor h. In
120 fact, it does not depend on the hyper-policy Ω_E
121 and a sampling policy $\pi_{\mathcal{B}}$ to construct $I = I_{\pi_{\mathcal{B}}}$.
122 We only need mild requirements for $\pi_{\mathcal{B}}$ that it
123 should cover the support of $\rho_{\Omega_E}(s, s')$ so that I
124 can be learned to provide an effective action to
125 achieve the target state. In both experiments and
126 theoretical analysis we show that this require-
127 ment alleviates the dependence on the inverse
128 dynamics. Furthermore, if the environment and
129 the expert are all deterministic (which is usu-
130 ally the case in real-world scenarios such as

Figure 1: The architecture of Decoupled Policy Optimization (DPO), which consists of an expert state transition predictor (to plan where to go) followed by an inverse dynamics model (to decide how to reach).

131 robotics), the state transition is a single-point distribution (or known as the Dirac delta function), and
132 we can simply model h as a deterministic function. By decoupling the state-to-action mapping policy
133 function as a state-to-state mapping function (the transition predictor) with a state-pair-to-action
134 mapping function (the inverse dynamics model), we can mimic the expert policy from state-only
135 demonstrations by optimizing these two modules. The whole architecture is illustrated in Fig. 1.

136 **State Transition Predictor** In practice, we construct a parameterized expert state transition predic-
137 tor h_ψ which predicts the subsequent state of the expert taking the input as a current state $\hat{s}' = h_\psi(s)$.

138 The state transition predictor models the explicit information of the expert, and it should be learned
139 from the demonstration data only. Thence, we implement Eq. (4) as a KL divergence minimization:

$$\min_\psi \mathbb{E}_{(s,s')\sim\Omega_E}[\mathrm{D_{KL}}(h_{\Omega_E}(s'|s)\|h_\psi(s'|s))] , \tag{8}$$

140 which can be optimized in a supervised manner. Specifically, we sample state transitions (s, s') from
141 the expert demonstrations $\mathcal{D}$ and optimize the L2 loss:

$$\mathcal{L}_\psi^h = \mathbb{E}_{(s,s')\sim\mathcal{D}}\left[\|s' - h_\psi(s)\|^2\right] . \tag{9}$$

142 **Inverse Dynamics Model** Knowing where to go is not enough since the agent has to interact with
143 the environment to reach the target. This can be achieved via an inverse dynamics model, which
144 predicts the action within two consecutive states. Formally, let the ϕ-parameterized inverse dynamics
145 model I_ϕ take input the state pair and predict the feasible action to achieve the state transition:
146 $\hat{a} = I_\phi(s, s')$. Intuitively, we want the inverse dynamics to learn from possible transitions sampled
147 by the agent. Recall that we only need the support of learned $I(a|s, s')$ of the sampling policy covers
148 the support of the expert hyper-policy, from which we can infer at least one possible decision. Hence,
149 we can optimize the KL divergence between the inverse dynamics of a sampling policy $\pi_{\mathcal{B}}$ and I_ϕ:

$$\min_\phi \mathbb{E}_{(s,s')\sim\pi_{\mathcal{B}}}[\mathrm{D_{KL}}(I_{\pi_{\mathcal{B}}}(a|s, s')\|I_\phi(a|s, s'))] , \tag{10}$$

150 and we can choose to optimize L2 loss in a supervised manner by sampling from the replay buffer $\mathcal{B}$:

$$\mathcal{L}_\phi^I = \mathbb{E}_{(s,a,s')\sim\mathcal{B}}\left[\|a - I_\phi(s, s')\|^2\right] . \tag{11}$$

151 In our implementation, both the state predictor and the inverse dynamics can be constructed as
152 Gaussian distributions similar to a normal stochastic policy, thus encouraging the exploration.

3.3 Tackling Compounding Error Challenges

154 In our formulation, we have decoupled the state-to-action mapping policy as a state-to-state mapping
155 function and a state-pair-to-action mapping function. Unfortunately, compounding error problems
156 exists such that the agent cannot reach where it plans go due to the fitting errors of these two parts.

157 **Theorem 1** (Error Bound of DPO)**.** *Consider a deterministic environment whose transition function*
158 $\mathcal{T}(s, a)$ *is deterministic and L-Lipschitz. Assume the ground-truth state transition $h_{\Omega_E}(s)$ is deter-*
159 *ministic, and for each policy $\pi \in \Pi$, its inverse dynamics I_π is also deterministic and C-Lipschitz.*
160 *Then for any state s, the distance between the desired state s'_E and reaching state s' sampled by the*
161 *decoupled policy is bounded by*

$$\|s' - s'_E\| \le LC\|h_{\Omega_E}(s) - h_\psi(s)\| + L\|I_{\pi_{\mathcal{B}}}(s, \hat{s}') - I_\phi(s, \hat{s}')\| , \tag{12}$$

162 *where $\pi_{\mathcal{B}}$ is a sampling policy that covers the state transition support of the expert hyper-policy and*
163 $\hat{s}' = h_{\psi}(s)$ *is the predicted next state.*

164 The proof can be found in Appendix B, where we also
165 induce a similar error bound for rollout with a state-
166 to-action policy as BCO [20] to show the advantage
167 of the decoupled structure. From Theorem 1 we
168 know that the compounding error can be enlarged due
169 to each part's fitting error, where the first term can
170 explain the error of predicted states and the second
171 indicates whether the agent can reach where it plans
172 to. To alleviate the error, we further propose regularization on these two modules.

Figure 2: Multi-step optimization. Given an expert state s_E, h_{ψ} predicts the next possible state $\hat{s}'^1$, which is further fed to a target network $h_{\psi'}$ to predict the following sequence. The total loss computes the MSE loss along the state sequence.

3.3.1 Regularization on Target Planning

174 One major problem is that the state transition predictor may suggest non-neighboring states instead
175 of predicting one-step reachable states. To overcome this, we draw inspiration from Asadi et al. [1]
176 and Edwards et al. [2], and regularize state transition predictor to prevent the model from predicting
177 non-neighboring states via multi-step and cycle training style.

178 **Multi-Step Optimization** We first explain the details of the multi-step optimization objective. This
179 idea is motivated by Asadi et al. [1], which optimizes a multi-step outcome by executing a sequence
180 of actions in the dynamics model. Here we optimize the state sequence instead. As shown in Fig. 2,
181 given an expert state s_E, h_{ψ} predicts the next possible state $\hat{s}'$ that the expert will reach; the predicted
182 state is then fed into the predictor to output the predicted two-step state $\hat{s}''$. As such, the multi-step
183 training loss is the L2 loss computed along the k-step outcome sequence:

$$\mathcal{L}_{\psi}^{h,\text{ms}} = \mathbb{E}_{(s,\{s_E'^i\}_{i=1}^k)\sim\mathcal{D}} \left[\|s_E'^1 - h_{\psi}(s)\|^2 + \sum_{i=2}^{k} \|s_E'^i - h_{\psi'}(s'^{i-1})\|^2 \right]. \quad (13)$$

184 Intuitively, such a regularization makes the state prediction
185 $\hat{s}'$ close to the expert state distribution in order to make
186 accurate long step predictions. It is worth noting that the
187 gradient of the cascade state transition predictors should
188 be dropped since we already have an accurate input at each
189 time step, and for each training step, we only update the
190 first one. We use a target network $h_{\psi'}$ in practice.

191 **Cycle Training Style** Another way to regularize the
192 transition predictor's output to a neighboring state is to
193 keep an additional function to ensure the cycle consistency,
194 which is also regarded as an important technique in [2].
195 In particular, as illustrated in Fig. 3, given an expert state
196 s_E, we take the predicted state $\hat{s}'$ and s_E into the inverse
197 dynamics and get the action a, then we train an additional forward dynamics model M_{ω} to simulate
198 one step rollout that takes the input (s_E, a) and gets a forward next state $\tilde{s}'$:

Figure 3: Cycle training style. Given an expert state s_E, $I_{\phi}(s, s')$ takes input the predicted state $\hat{s}'$ and s_E to get the execution action a, then an additional forward dynamics model M_{ω} is used to simulated one step rollout using (s_E, a) and get a forward next state $\tilde{s}'$. The total loss computes the MSE loss between the two predicted states.

$$\begin{aligned} \mathcal{L}_{\omega}^M &= \mathbb{E}_{(s,a,s')\sim\mathcal{B}} \left[\|s' - M_{\omega}(s,a)\|^2 \right] \\ \mathcal{L}_{\psi}^{h,\text{cycle}} &= \mathbb{E}_{(s,s')\sim\mathcal{D}} \left[\|s' - h_{\psi}(s)\|^2 + \|h(s) - M_{\omega}(s, I_{\phi}(s,s'))\|^2 \right]. \end{aligned} \quad (14)$$

199 In other words, the cycle training scheme provides a regularization on h_{ψ} to make predictions
200 consistent with the forward dynamics model.

3.3.2 Efficient Skills Learning via Decoupled Policy Gradient

202 In previous sections, we have mentioned that learning to reach a specific place requires the data-
203 collecting policy to cover the support of the expert hyper-policy. This is directly achievable on simple
204 low-dimensional tasks, but it may not be easily satisfied in high-dimensional continuous environments.
205 To this end, we encourage the agent to approach those state transitions from the expert's hyper-policy

Ω_E by minimizing the JS divergence of the state transition occupancy using a state-to-action mapping policy $D_{JS}\left(\rho_{\pi_E}(s, s'), \rho_\pi(s, s')\right)$. This can be done by producing informative rewards via GAN-like methods [8, 21], and updating the decoupled policy with policy gradients (PG).

In detail, we construct a parameterized discriminator $D_\omega(s, s')$ to compute the reward $r(s, a) \triangleq r(s, s')$ as $\log D_\omega(s, s')$ and the decoupled policy served as the generator. In addition, since we decouple the policy as two parameterized modules, i.e., a state transition predictor and an inverse dynamics model, then by chain rule, the PG for the decoupled policy can be accomplished by

$$\begin{aligned}
\nabla \mathcal{L}^\pi_{\phi, \psi} &= \mathbb{E}_\pi\left[Q(s, a) \nabla_{\phi, \psi} \log \pi_{\phi, \psi}(a|s)\right] \\
&= \mathbb{E}_\pi\left[Q(s, a) \int_{s'} \left(\nabla_\psi \log h_\psi(s'|s) + \nabla_\phi \log I_\phi(a|s, s')\right) \mathrm{d}s'\right] ,
\end{aligned} \tag{15}$$

where Q is the state-action value function; the first term is the gradient for updating the state transition predictor; and the second term is for the inverse dynamics model. Thus, the optimization for both the state transition predictor and the inverse dynamics can augment the supervised objectives with any PG-based learning algorithms (e.g., TRPO, PPO, SAC). As the training proceeds, the agent will sample more transition data around Ω_E, and thus the support of the sampling policy will progressively cover the support of $\rho_{\Omega E}(s, s')$.

3.4 Overall Algorithm

By combining the idea of generative adversarial training, we obtain our final algorithms, composed with three essential parts: the state transition predictor h used for predicting the possible future states sampled by the expert; the inverse dynamics model I used for inferring the possible actions conditioned on two adjacent states; and the discriminator D used for offering intermediate reward signals for training the decoupled policy $\pi = I(h)$. The overall objective of DPO is

$$\mathcal{L}^{\pi, h, I}_{\phi, \psi} = \lambda_G \mathcal{L}^\pi_{\phi, \psi} + \lambda_h \mathcal{L}^h_\psi + \lambda_I \mathcal{L}^I_\phi , \tag{16}$$

where λ_G, λ_h and λ_I are hyperparameters for trading off the training among each loss. In practice, we try less than ten combinations for these parameters as shown in Appendix C.3, and we directly optimize $\mathcal{L}^\pi_{\phi, \psi}$ instead of iterative training. The detailed algorithm is summarized in Appendix A. Besides, it is worth noting that both the inverse dynamics model and the state transition predictor can be pre-trained, where we optimize $\mathcal{L}^h_\psi$ using the state-only demonstration and optimize $\mathcal{L}^I_\phi$ using samples collected by a randomized agent.

4 Related Work

State-only imitation learning (SOIL) endows the agent with the ability to learn from expert states. Although lack the expert decision information, most of the previous works still optimize a state-to-action mapping policy to match the state transition distribution of the expert. For example, Torabi et al. [20]

Table 1: Comparison between different methods.

Method	Inverse Dynamics	State Predictor	Decoupled Policy	Task
BCO [20]	✓	✗	✗	SOIL
GAIfO [21]	✗	✗	✗	SOIL
IDDM [23]	✗	✗	✗	SOIL
OPOLO [25]	✓	✗	✗	SOIL
PID-GAIL [9]	✗	✗	✓	IL
QSS [2]	✓	✓	✓	RL
SAIL [14]	✓	✓	✗	IL
DPO (Ours)	✓	✓	✓	SOIL

used a model-based approach to apply behavioral cloning to state-only demonstrations, while Torabi et al. [21] employed a similar structure to GAIL to match the distribution of state transitions. Yang et al. [23] analyzed the optimization gap between SOIL and naive IL and introduced a mutual information term to narrow it. Huang et al. [9] applied SOIL on autonomous driving tasks by decoupling the policy into a neural decision module and a non-differentiable execution module in a hierarchical way.

Our work decouples the state-to-action policy into two modules. However, both the inverse dynamics model and the state transition predictor have been widely used by many previous works on RL and IL tasks. For instance, Torabi et al. [20] and Guo et al. [4] trained an inverse dynamics model to label the state-only demonstrations with inferred actions. Nair et al. [17] proposed a method for manipulating ropes to match a single human-specified image sequence, in which an inverse dynamics model is trained in a self-supervised manner and used to generate control signals. Kimura et al. [12] utilized a state transition predictor to fit the state transition probability in the expert data, which is further used to compute a predefined reward function. Liu et al. [14] constructed a policy prior using the inverse dynamics and the state transition predictor, but the policy prior was only used for regularizing the

Table 2: Eventual performance against different methods on 6 easy-to-hard continuous control benchmarks. The means and the standard deviations are evaluated over more than 5 random seeds.

	InvertedPendulum	InvertedDoublePendulum	Hopper	Walker2d	HalfCheetah	Ant
Random	25.28 ± 5.53	78.28 ± 10.73	13.09 ± 0.10	7.07 ± 0.13	74.48 ± 12.39	713.59 ± 203.92
BCO	$\mathbf{1000.00 \pm 0.00}$	415.04 ± 148.46	1430.16 ± 398.81	261.36 ± 25.17	-13.66 ± 149.94	397.79 ± 239.16
GAIfO	$\mathbf{1000.00 \pm 0.00}$	7818.07 ± 1778.67	3068.10 ± 26.32	3865.20 ± 341.90	8953.35 ± 1079.41	5122.29 ± 807.19
GAIfO-DP	$\mathbf{1000.00 \pm 0.00}$	7305.01 ± 1591.23	3031.84 ± 152.13	4003.06 ± 241.34	8675.42 ± 807.29	$\mathbf{5535.9 \pm 62.74}$
DPO (w/o PG)	$\mathbf{1000.00 \pm 0.00}$	3545.70 ± 738.16	629.84 ± 344.07	334.23 ± 85.42	-472.00 ± 132.81	-196.96 ± 124.26
DPO (w PG)	$\mathbf{1000.00 \pm 0.00}$	$\mathbf{7846.40 \pm 1541.20}$	$\mathbf{3165.72 \pm 68.44}$	$\mathbf{4407.53 \pm 266.72}$	$\mathbf{10501.96 \pm 438.01}$	5338.48 ± 107.2
Expert (SAC)	1000.00 ± 0.00	9358.87 ± 0.10	3402.94 ± 446.48	5639.32 ± 29.97	13711.64 ± 111.47	5404.55 ± 1520.49

policy network. However, as shown in this paper, the policy can be exactly decoupled as these two parts, which can be uniformly optimized through policy gradient without keeping an extra policy. Edwards et al. [2] estimated $Q(s, s')$ for RL tasks which employs a similar policy form as Eq. (6) and updates the state transition predictor through a deterministic policy gradient similar to DDPG [13]. To sort out the difference between these methods and ours, we summarize the key factors in Tab. 1.

5 Experiments

We conduct four sets of experiments to investigate the following research questions:

RQ1 Is decoupled policy structure superior than state-to-action structure on SOIL tasks?
RQ2 Does DPO achieve higher efficiency or better performance than baselines on SOIL tasks?
RQ3 Can agent reach where it plans and does the proposed regularization help to mitigate the compounding error?
RQ4 How can DPO be applied on real-world data?

To answer RQ1, we conduct toy experiments with a simple 2D grid world environment and compare both qualitative and quantitative results of DPO against BCO and GAIfO. Regarding RQ2, we empirically evaluate DPO on easy-to-hard continuous control benchmarking tasks. And for RQ3, we evaluate the difference between the predicted states that the agent plans to reach and the consecutive state that the agent actually achieves in the environment for the proposed regularization. Finally, we try to imitate real-world traffic surveillance recordings in a simulated environment to investigate RQ4, which shows the potential to use real-world data for simulating human behaviors. Due to the space limit, we leave experiment details, additional results and ablation study in Appendix.

5.1 Understanding the Decoupled Structure

In this paper we design decoupled policy optimization (DPO) to perform SOIL tasks, and in previous sections we propose that the key technical contribution of DPO is the decoupled structure of policy that models the explicit state transition information and the latent action information from demonstrations, which solves the ambiguity and enhance the learning efficiency. Therefore, in this set of experiments, we aim to demonstrate how DPO is superior than state-to-action policy methods (RQ1). We first generate expert demonstrations in a 2D 6×6 grid world environment, in which the agent starts at the upper left corner and aims to reach the upper right corner. In each grid the agent has $k \times 4$ actions, which means that the agent has k possible actions to reach the neighboring block and in our experiment we choose $k = 5$ to enlarge the action scale.

(a) Rollout density.

(b) Loss curves.

Figure 4: Toy example.

The density of the expert trajectories and the trajectories sampled by different methods are shown in Fig. 4(a). We show that both BCO and GAIfO have troubles in direct learning the implicit action from state-only behaviors. Notably, GAIfO only imitates the major trajectory and omit the other choice and BCO also stucks in the middle right. By contrast, DPO recovers the expert demonstrations much better, benefiting from the decoupled structure that first determining the target and then taking the action to achieve it. To further illustrate the learning efficiency advantage of DPO, we further illustrate the JS divergence curves of DPO and BCO during training in Fig. 4(b). Besides, we show the policy loss for BCO, the state predictor (SP) loss for DPO, and the inverse dynamics (ID) loss for both methods. Except that the JS divergence of DPO decreases quicker than BCO, it is also observable that DPO relies less on the inverse dynamics than BCO, since the inverse dynamics loss of

Figure 5: Learning curves on 6 easy-to-hard continuous control benchmarks, where the solid line and the shade represent the mean and the standard deviation of the averaged return over more than 5 random seeds. We pre-train BCO and DPO for 50k steps and show it in figures.

DPO converges to a higher level. We further provide a theoretic analysis to the dependence of inverse dynamics by BCO and DPO in Appendix B.

5.2 Comparative Evaluations

We compare the qualitative results of DPO against other baseline methods on easy-to-hard continuous control benchmarking environments (RQ2), including InvertedPendulum, InvertedDoublePendulum, Hopper, Walker2d, HalfCheetah and Ant. In each environment, besides GAIfO and BCO, we also evaluate GAIfO with decoupled policy (denoted as GAIfO-DP). For DPO we compare the reward augmented version of DPO (denoted as DPO w PG)[1] with the supervised learning version of DPO, i.e., $\lambda_G = 0$ (denoted as DPO w/o PG). For fairness, we re-implement all the algorithms based on a Pytorch code framework[2] and adopt Soft Actor-Critic (SAC) [5] as the RL learning algorithm for GAIfO and DPO. For all environments, we first train an SAC agent to collect 4 state-only trajectories and then train agents with such data. All algorithms are evaluated by a deterministic policy. The eventual results are summarized in Tab. 2, and the learning curves are shown in Fig. 5. It is worth noting that for DPO, we choose the best performance among the experiments that use multi-step or cycle regularization, and we put the full experiment results in Appendix C.

One can easily observe that on simple environments, BCO is able to achieve a good performance, and GAIfO also does well on harder tasks. Even so, DPO can still gain the best or comparable performance against its counterparts. Particularly, without augmented reward, DPO is able to reach the optimality with the highest sample efficiency on simple tasks like InvertedPendulum. By contrast, on higher-dimensional tasks such as Hopper, Walker2d, HalfCheetah and Ant, it is difficult to construct accurate inverse dynamics that covers the support of the expert hyper-policy from scratch. However, by combining generative adversarial policy gradients, the agent finally recovers a good policy from the expert hyper-policy. This is particularly evident on HalfCheetah where DPO behaves poorly at the beginning but improves fast as the training proceeds. Besides, as illustrated in Fig. 5, DPO benefits from better sample efficiency in most of the environments, but the improvements are limited on the hardest tasks. We think that this may be due to larger state spaces (111 dimensions for Ant) that makes it difficult to recover a good state predictor or an inverse dynamics model. In all experiments, GAIfO-DP achieves similar results as GAIfO, indicating that the network structure does not count much for the performance.

5.3 Compounding Error Reduction

In this section, we aim to study whether the agent can effectively reach the target as it plans (RQ3). Therefore, we analyze the distance of the reaching states and the predicted consecutive states, and

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[1]Without ambiguity we simply denote DPO for this version of algorithm in the following sections.
[2]https://github.com/KamyarGh/rl_swiss

Figure 6: Compounding error of the predicted consecutive states and the real states the agent reaches when rollout in the environments.

draw the mean square error (MSE) along the training procedure in Fig. 6. We also compare our regularization including multi-step optimization (denoted as M.S.-k, where k is the number of rollout steps) and cycle training style (denoted as Cycle). Note that DPO needs at least 1-step rollout for training the state transition predictor. As shown in Fig. 6, the agent still has gaps to get to where it plans to, and the mismatch always deteriorates on harder tasks. Combining regularization can always achieve lower compounding error, and the cycle training is effective in most of the environments. In Appendix C.6, we further illustrate the correlation between the final performance and the distance.

5.4 Learn to Drive from Real-World Traffic Data

The rapid development of autonomous driving has brought a lot of demand for simulating and training an RL agent in the simulator, which requires realistic interactions with various social vehicles [24]. However, driver's detailed actions are not easily to obtain yet we adopt SOIL from a traffic surveillance recording dataset (NGSIM I-80 [6]) that contains kinds of recorded human driving trajectories. We wish to further examine the potential of DPO for decreasing the gap between the real world and simulation (RQ4). We utilize the simulator provided by Henaff et al. [7] as our simulation platform and learn to imitate real-world driving behaviors. We compare DPO against GAIfO and BCO, and choose *Success Rate*, *Mean Distance* and *KL Divergence* as evaluation metrics. Specifically, *Success Rate* is the percentage of driving across the entire area without crashing into other vehicles or driving off the road, *Mean Distance* is the distance traveled before the episode ends, and *KL Divergence* measures the position distribution distance between the expert and the agent.

As shown in Tab. 3, DPO outperforms baseline methods in all three metrics while possessing higher stability. The decoupled policy allows the state predictor to focus on matching the distribution of expert trajectories, thus achieving smaller deviations from the expert position distribution. Furthermore, since the policy gradient can be computed with non-differentiable inverse dynamics, we can generate stable action sequences [10, 9] by replacing the inverse dynamics model with classical controllers, which can be generalized to realistic applications.

Table 3: Performance on NGSIM I-80 driving task over 5 random seeds.

Method	Success Rate (%)	Mean Distance (m)	KL Divergence
BCO	27.4 ± 1.1	129.8 ± 2.0	24.4 ± 2.2
GAIfO	77.5 ± 0.8	188.3 ± 1.1	11.5 ± 3.9
DPO	$\mathbf{80.3 \pm 0.5}$	$\mathbf{192.7 \pm 0.6}$	$\mathbf{9.5 \pm 1.8}$
Expert	100	210.0	0

6 Conclusion

In this paper, we characterized the optimality and investigate the ambiguity problem in state-only imitation learning, and accordingly proposed Decoupled Policy Optimization (DPO), which splits the state-to-action mapping policy into a state-to-state mapping state transition predictor and a state-pair-to-action mapping inverse dynamics model. Furthermore, we employ regularization and generative adversarial methods to mitigate the compounding error caused by the decoupled modules. The flexibility of the decoupled architecture allows a wide range of interesting future works, such as replacing the inverse dynamics with a classic control module to produce stable control signals, learning specific skills with shared state transition and multi-task target learning with shared pre-training skills.

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